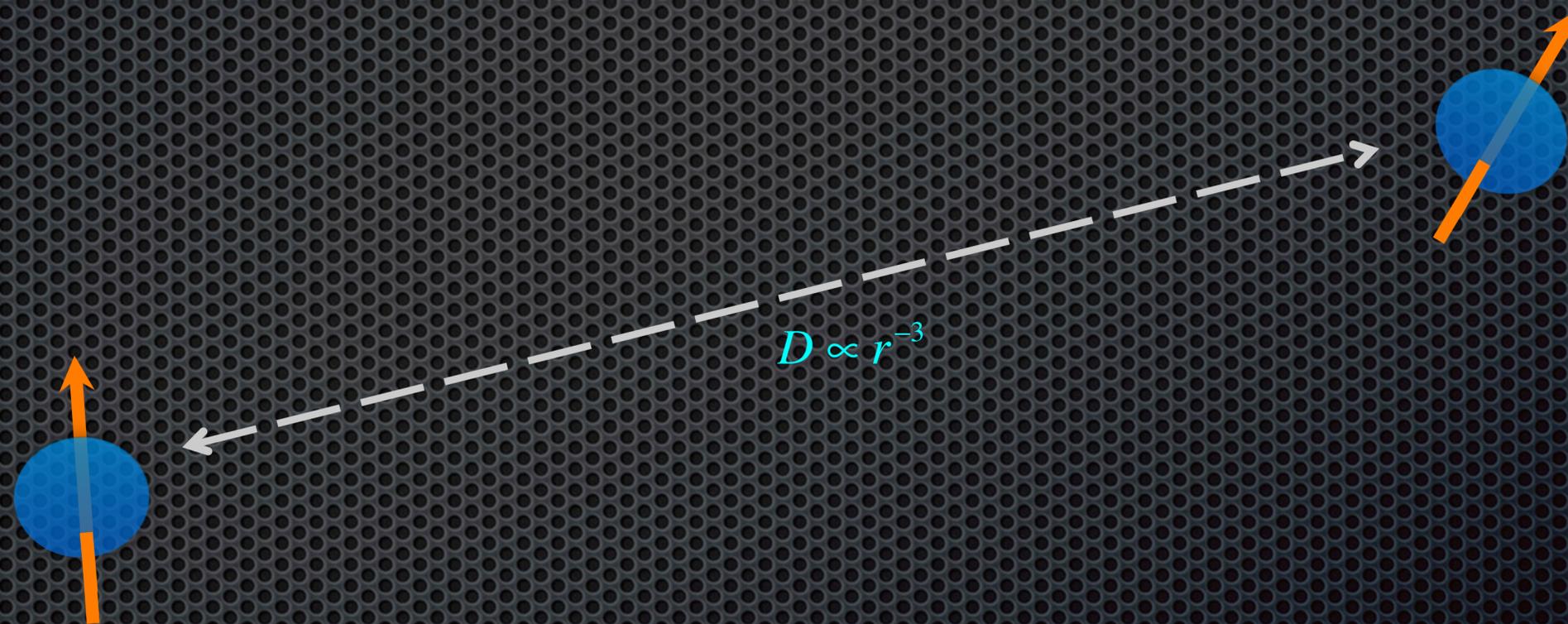


Electron Spin Resonance in Biophysical Chemistry



BASIC PRINCIPLES

- SPIN ANGULAR MOMENTUM VECTOR $\hat{S} \hbar$
 $\hat{I} \hbar \rightarrow \hbar = \frac{h}{2\pi}$

(INTRINSIC SPIN; PURELY QM !!)

- MAGNETIC MOMENT

Bohr magneton = $\frac{e\hbar}{2m}$

\downarrow charge \downarrow $\left. \begin{matrix} \beta_e \\ \beta_N \\ \beta_B \end{matrix} \right\}$
 \uparrow proton or ele. mass

Gyromagnetic ratio \downarrow

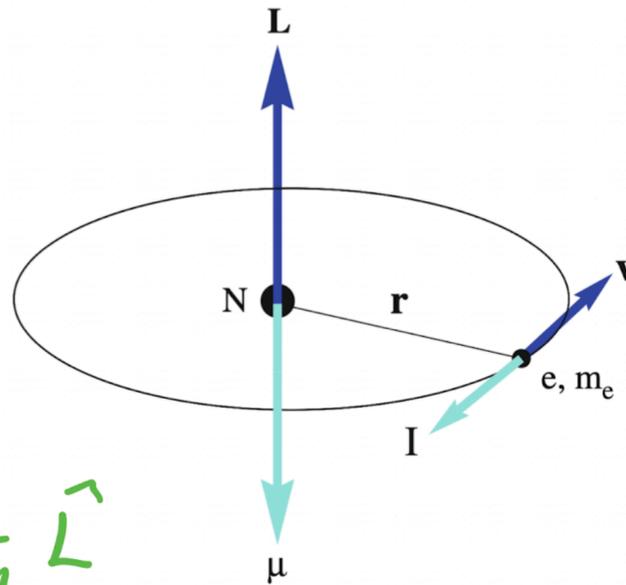
$$\vec{\mu} = -\gamma \hbar \hat{S} = -g \beta \hat{S}$$

\uparrow g factor (Dimensionless, intrinsic)

phys. meaning
↓

$$\rightarrow |\mu| = \frac{g\beta}{\hbar} = \frac{ge}{2m} = \frac{\text{mag. moment } \mu}{\text{Int. Spin ang. momentum. } \hbar \hat{S}}$$

Fig. 1.1 Classical model illustrating relationship between angular momentum $L = m_e \cdot v \cdot r$ of electron, e , moving around a nucleus N and magnetic moment μ .



$$\mu = I \cdot A = \dots = -\frac{e}{2m} \hat{L}$$

TABLE 28.1 Parameters for Spin-Active Nuclei

Nucleus	Isotopic Abundance (%)	Spin	Nuclear g Factor g_N	Magnetogyric Ratio $\gamma/10^7$ (rad T ⁻¹ s ⁻¹)
¹ H	99.985	1/2	5.5854	26.75
¹³ C	1.108	1/2	1.4042	6.73
³¹ P	100	1/2	2.2610	10.84
² H	0.015	1	0.8574	4.11
¹⁴ N	99.63	1	0.4036	1.93

$$\frac{m_p}{m_e} = \frac{1.67 \times 10^{-24} \text{ g}}{9.1 \times 10^{-28} \text{ g}} \sim 1835$$

$$g_e = 2.0023, \quad g_N = 5.5854$$

$$\beta_e = 9.274 \times 10^{-24} \text{ J/T}$$

$$\beta_N = 5.0504 \times 10^{-27} \text{ J/T}$$

$$\therefore \frac{\mu_e}{\mu_N} \sim 658 \Rightarrow \mu_e \approx 658 \mu_N$$

\hookrightarrow better sensitivity per spin.

$$\cdot \hat{J}_z |\alpha\rangle = +\frac{1}{2} |\alpha\rangle$$

$$\hat{J}_z |\beta\rangle = -\frac{1}{2} |\beta\rangle$$

$\cdot m_s$: Electron spin Q.N.

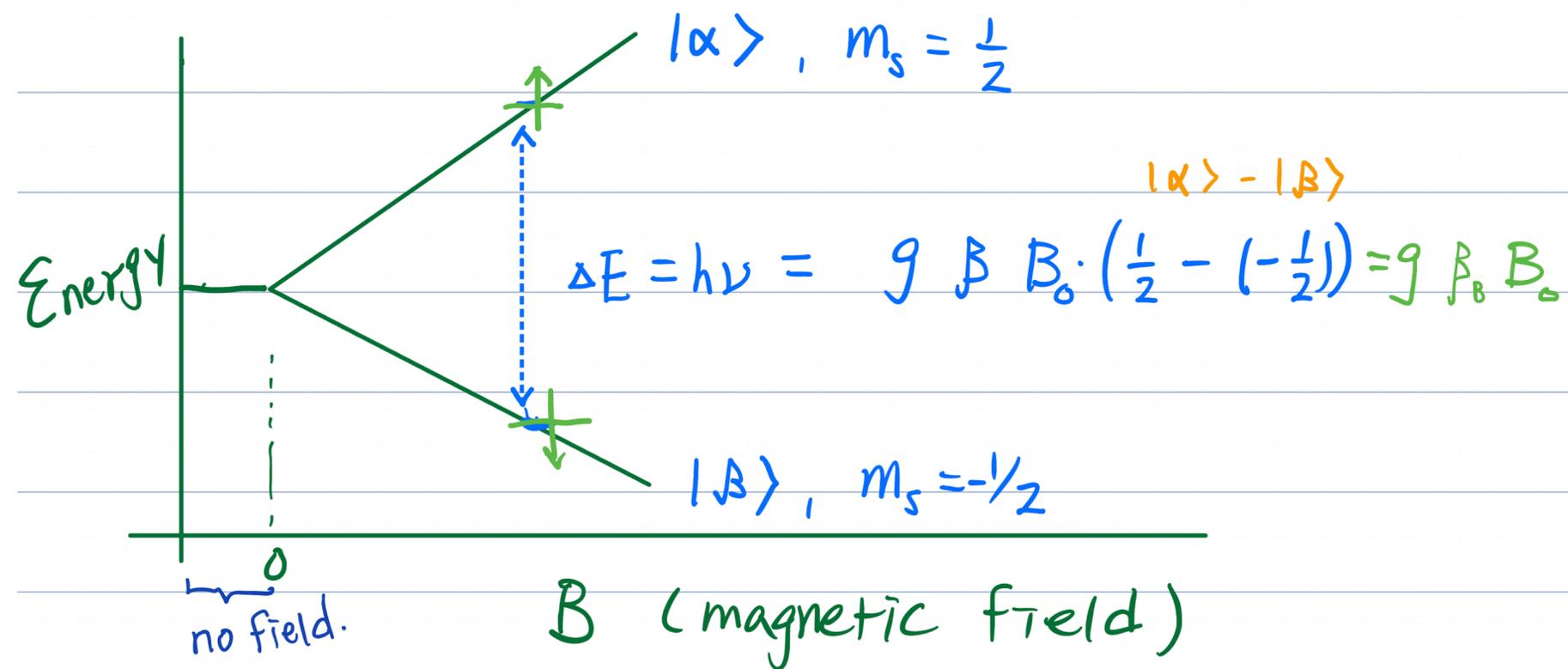
$$\text{e.g. } S = \frac{1}{2} \Rightarrow m_s = \pm \frac{1}{2}$$

• WHEN WE APPLY A STEADY MAGNETIC FIELD B ON A SPIN, THE INTERACTION BETWEEN B AND μ CAN BE EXPRESSED IN TERMS OF HAMILTONIAN:

$$\hat{H} = -\vec{\mu} \cdot \vec{B}_0$$

→ If we only consider B in z direction, ^(or H)

$$\langle \hat{H} \rangle = E = \mu_B \hbar B_0 m_s = g \beta B_0 m_s$$



→ In order to induce transition between $|\alpha\rangle$ and $|\beta\rangle$, we apply an oscillating electromagnetic field to provide energy of frequency ν to satisfy the resonance condition,

(Zeeman effect)

→ In terms of angular frequency ω [r s^{-1}]

$$\therefore \frac{\omega}{2\pi} = \nu \Rightarrow \omega = \gamma B_0 \propto B_0$$

Larmor
frequency.

[s^{-1}]. e.g. $\frac{1}{\mu\text{s}} \rightarrow \text{MHz}$.

Note:

$$\begin{cases} 2\pi\nu = \frac{g\beta}{\hbar} B_0 \\ h\nu = g\beta B_0 \end{cases}$$

• To induce the transition: tune ω as B_0 fixed. or vice versa.

→ modern NMR = radio freq. pulse techniques.

e.g. $^1\text{H} \Rightarrow 500 \text{ MHz} \rightarrow 12 \text{ Tesla}$.

$$\text{e.g. } \frac{B_0(\text{NMR})}{B_0(\text{EPR})} \sim \frac{\omega_N \cdot \gamma_e}{\gamma_N \cdot \omega_e} = 658 \cdot \frac{0.5 \text{ GHz}}{9 \text{ GHz}} \sim 37 \therefore B_0(\text{EPR}) \sim \frac{12}{37} = 0.33 \text{ Tesla}$$

e.g. Why not using NMR source (e.g. 500 MHz) to pump e^- spin?

ESR and NMR are very different methods!

	electron	proton	ratio
Rest mass	$m_e = 9.1094 \times 10^{-28} \text{ g}$	$m_p = 1.6726 \times 10^{-24} \text{ g}$	5.446×10^{-4}
Charge	$e = -4.80286 \times 10^{-10} \text{ ESU}$	$e = 4.80286 \times 10^{-10} \text{ ESU}$	-1
Spin angular momentum	$h/4\pi$	$h/4\pi$	1
Magnetic dipole moment	$\mu_S = g_e \beta_e \mathbf{S}$ $g_e = 2.002322$ $\beta_e = eh/4\pi m_e c =$ $9.274 \times 10^{-24} \text{ J/T}$	$\mu_N = g_N \beta_N \mathbf{S}$ $g_N = 5.5856$ $\beta_N = eh/4\pi m_N c =$ $5.0504 \times 10^{-27} \text{ J/T}$	658

$$\Rightarrow \mu_e \approx 658 \mu_N$$

↳ better sensitivity per spin.

- **Frequency:** Factor 1000 larger in EPR ! (*GHz instead of MHz*)
- **Relaxation Times:** Factor 1000 000 smaller in EPR ! (*ns instead of ms*) = much higher technical requirements, but unique sensitivity to molecular motion
- **Sensitivity :** Factor 1 000 000 better than in NMR !! (*1nM instead of 1mM*) *An ideal case, though*

$$1000 \text{ (freq)} \times 658 \sim 10^6$$

The Basic ESR Experiment (conventional ESR)

- ESR is done from 1 to 300+GHz, up to 2000+ GHz
 - Machines are classified according to their **source frequency** :
L (1.5), **S** (3.0), **C** (6.0), X (9), **Ku** (17), **K** (23), **Q** (36), **V** (50), **W** (95), **D**(140), **G**(180)
- Use **microwave transmission lines**
- Do spectroscopy with a few microwatts to a few milliwatts of power
- Solid state [**Gunn diode** or DRO] or tube [**klystron**] sources
- **Temperatures** from 4K (heme and non-heme iron) to 310K+ (in vivo/vitro)
- **Sensitivity** : Increases as (frequency)², but limited by sample size, field homogeneity and component construction problems.
- Practically (at X-band): detect 10^{10} spins, a detectable concentration of **$\sim 10^{-9}M$** . (under the condition of 100 μL)

Band name	Typical frequency ν in GHz	Wavelength λ in mm	Energy $h\nu$ in reciprocal cm	Resonance field B at $g = 2$ in tesla
L-band	1	300	0.033	0.036
S-band	3	100	0.10	0.11
C-band	6	50	0.20	0.21
X-band	10	30	0.33	0.36
P-band	15	20	0.50	0.54
K-band	24	12.5	0.80	0.86
Q-band	35	8.6	1.2	1.25
U-band	50	6.0	1.7	1.78
V-band	65	4.6	2.2	2.32
E-band	75	4.0	2.5	2.68
W-band	90	3.3	3.0	3.22
F-band	110	2.7	3.7	3.93
D-band	130	2.3	4.3	4.64
G-band	180	1.67	6.0	6.43
J-band	270	1.11	9.0	9.64
No name	600	0.50	20	21.4
No name	1000	0.30	33	35.7

Sensitivity

$$\underline{\text{Net Absorption}} \propto N_- - N_+$$

The ratio of populations at equilibrium is given by the Boltzmann distribution

$$\frac{N_+}{N_-} = e^{-\Delta E/k_B T} = e^{-g\mu_B B/k_B T}$$

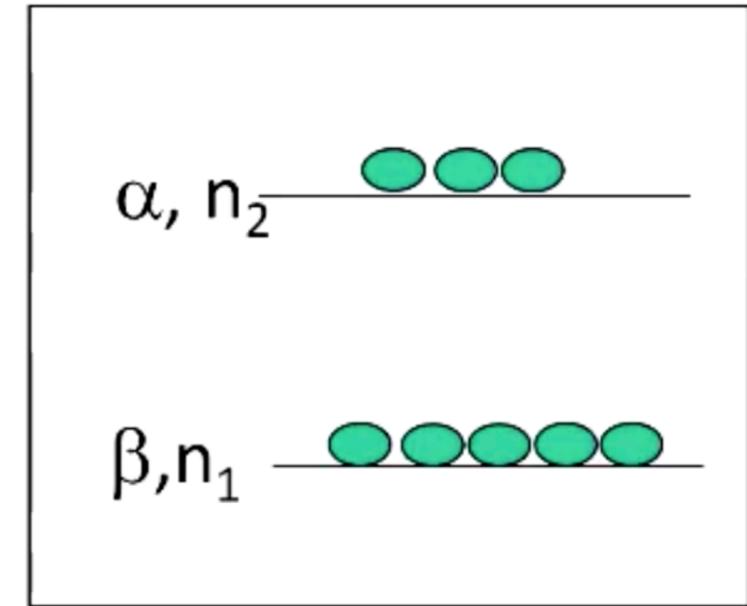
$$\frac{N_+}{N_-} \approx 1 - \frac{g\mu_B B}{k_B T} \quad \longrightarrow \quad N_- - N_+ = N_- \left[1 - \left(1 - \frac{g\mu_B B}{k_B T} \right) \right] = \frac{Ng\mu_B B}{2k_B T}$$

- Net absorption **increases with decreasing T**, and with **increasing magnetic field strength**. (ΔN determines the net absorption.)
- Higher frequency uses smaller waveguides, thus smaller sample volume, canceling the advantages (possibly).
- X-band can detect 10^{12} spins (10^{-12} moles) at room T. (on the order of 0.1 G wide)

The fractional excess population is:

$$\rightarrow \frac{n_2}{n_1} = e^{-\Delta E/kT}, \quad \Delta E = g\beta B_0$$

$$\rightarrow \frac{\Delta n}{n} = \frac{n_1 - n_2}{n_1 + n_2} = \frac{1 - e^{-\Delta E/kT}}{1 + e^{-\Delta E/kT}}$$



$$M_0 \propto n_1 - n_2$$

B_0 (T)

~ 0.3

~ 3

~ 9.6

e
 ^1H

$\Delta n/n$	300 K	77 K	1.5 K
9.5 GHz 14.5 MHz	0.0008 0.0012×10^{-3}	0.002 0.00395×10^{-3}	0.1508 0.2320×10^{-3}
95 GHz 145 MHz	0.0076 0.0116×10^{-3}	0.0253 0.0387×10^{-3}	0.9087 2.3196×10^{-3}
263 GHz 400 MHz	0.0210 0.0320×10^{-3}	0.0700 0.1066×10^{-3}	0.9996 6.3989×10^{-3}

• IN AN EQUILIBRIUM SPIN SYSTEM $N = N_\alpha + N_\beta$

→ BOLTZMANN LAW:

$$\frac{N_\beta}{N_\alpha} = \exp(-\Delta E/kT) \quad \text{for} \quad \Delta E = h\nu = g\beta B_0$$

$$\Rightarrow \frac{N_\beta}{N_\alpha} \approx 1 - \frac{\Delta E}{kT}$$

$$\therefore N_\alpha - N_\beta = N_\alpha \left[1 - \left(1 - \frac{\Delta E}{kT} \right) \right] = \frac{N_\alpha \Delta E}{kT}$$

$$\approx \frac{N}{2} \frac{\Delta E}{kT} \propto \frac{h\nu_0}{T} \quad \text{or} \quad \frac{\beta B_0}{T}$$

① $T \downarrow$ or $\nu_0 \uparrow$ or $B_0 \uparrow \Rightarrow \Delta N \uparrow$

② $\nu_e \sim 658 \nu_{1H}$ (at the same B_0)

EXAMPLE PROBLEM 28.1

- Calculate the two possible energies of the ^1H nuclear spin in a uniform magnetic field of 5.50 T.
- Calculate the energy ΔE absorbed in making a transition from the α to the β state. If a transition is made between these levels by the absorption of electromagnetic radiation, what region of the spectrum is used?
- Calculate the relative populations of these two states in equilibrium at 300. K.

Solution

- a. The two energies are given by

$$\begin{aligned} E &= \pm \frac{1}{2} g_N \beta_N B_0 \\ &= \pm \frac{1}{2} \times 5.5854 \times 5.051 \times 10^{-27} \text{ J/T} \times 5.50 \text{ T} \\ &= \pm 7.76 \times 10^{-26} \text{ J} \end{aligned}$$

- b. The energy difference is given by

$$\begin{aligned} \Delta E &= 2(7.76 \times 10^{-26} \text{ J}) \\ &= 1.55 \times 10^{-25} \text{ J} \end{aligned}$$

$$\sim 10^{-3} \text{ cm}^{-1}$$

$$\nu = \frac{\Delta E}{h} = \frac{1.55 \times 10^{-25}}{6.626 \times 10^{-34}} = 2.34 \times 10^8 \text{ s}^{-1}$$

This is in the range of frequencies called radio frequencies.

- c. The relative populations of the two states are given by

$$\frac{n_\beta}{n_\alpha} = \exp\left(-\frac{E_\beta - E_\alpha}{k_B T}\right) = \exp\left(\frac{-2 \times 7.76 \times 10^{-26} \text{ J}}{1.381 \times 10^{-23} \text{ J K}^{-1} \times 300. \text{ K}}\right) = 0.999963 \quad \#$$

$$\frac{n_\alpha - n_\beta}{\frac{1}{2}(n_\alpha + n_\beta)} \approx \frac{(1 - 0.999963) n_\alpha}{n_\alpha} = 3.7 \times 10^{-5} \quad \text{or} \quad \frac{n_\alpha - n_\beta}{n_\alpha + n_\beta} \approx \frac{n_\alpha(1 - 0.999963)}{2n_\alpha}$$

$$= 1.85 \times 10^{-5}$$

From this result, we see that the populations of the two states are the same to within a few parts per million. Note that observing the appropriate rules for significant figures, we would obtain a ratio of 1.00.

$$\rightarrow E_\beta - E_\alpha \ll kT, \text{ but } n_\alpha \approx n_\beta$$

\Rightarrow upward transition rate \approx downward.

Structure and Stability of Nitroxides

Nitroxides are compounds containing the $>\text{N}^{\bullet}\text{O}$ group which has an unpaired electron. The unpaired electron is located in a $2p_{\pi}$ (π^*) orbital of the nitrogen and the oxygen atom. Since there is also an N-O σ -bond and two electrons that fill a π -bonding orbital between these atoms, the effective N-O bond order is 1.5 (two center- three electron- bonding, 2c-3e). The structure of this group can be considered as a superposition of two mesomeric structures [34]



Scheme 2.1 Mesomeric formula of the nitroxide group.

The contributions of both structures to the ground state may be different, depending on the polarity of the medium and conjugation within the molecule. In apolar solvents both structures have the same weight while polar solvents will favor the charged mesomeric structure, leading to a higher charge density on the nitrogen (which can be observed as increased nitrogen hyperfine splitting in EPR spectra). The electronic structure is influenced in a similar way by π -complex formation with aromatic rings. Depending on the structure, the spin density on oxygen is $\rho_{\text{O}}=0.58-0.72$ and on nitrogen it is $\rho_{\text{N}}=0.42-0.28$ [35]. The dipole moment of the N-O bond is 2.7 D and the distance is 1.26-1.29 Å. The 2c-3e N-O bond has an energy of 419 kJ/mol, midway between the energy of an N-O single bond (230 kJ/mol) and N=O double bond (600 kJ/mol) [36]. As a result of the electron delocalization, nitroxides are relatively stable molecules. The energy gain from delocalization has been calculated as 126 kJ/mol [37].

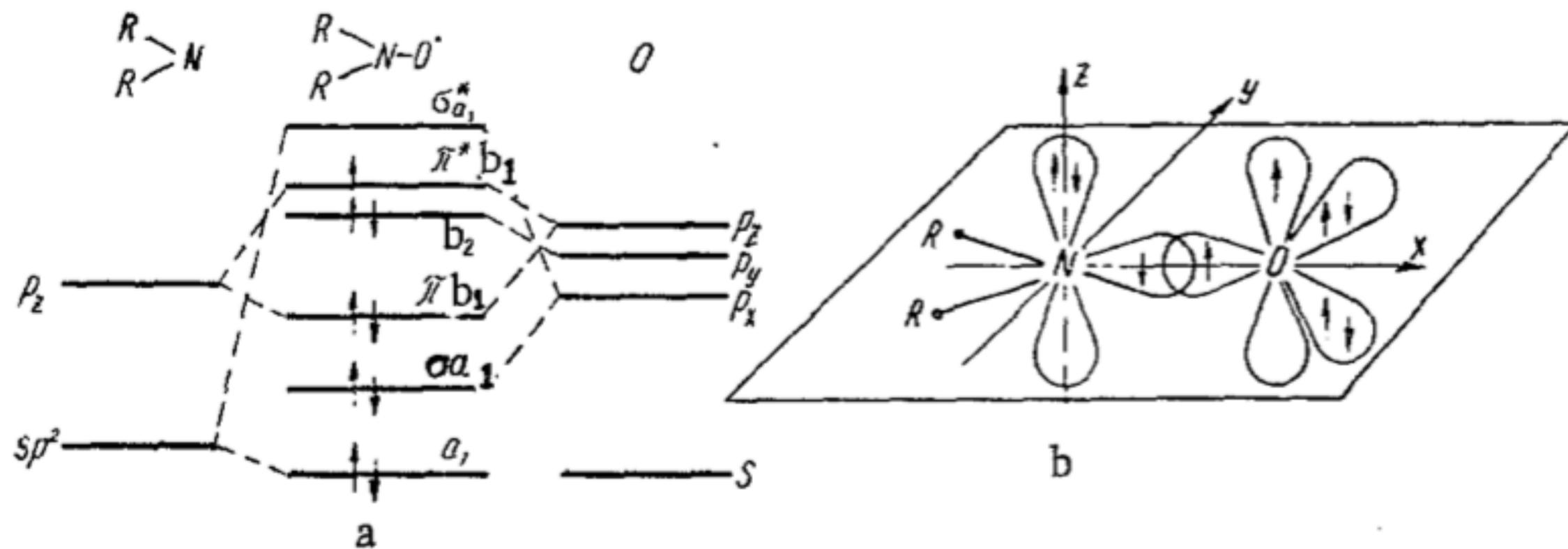
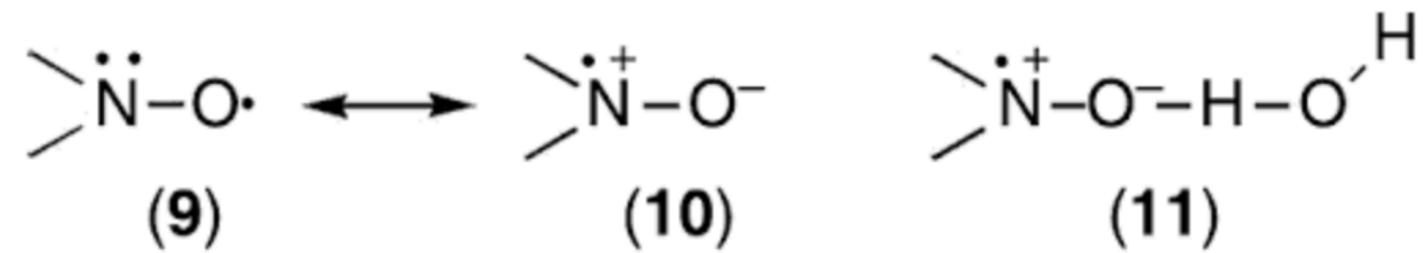


Fig. 2. Schematic representation of the energy levels (a) and electronic configuration (b) of the $>N-O\cdot$ fragment of a free nitroxide radical [15].



derived nitroxides. The nitrogen hfs constants of nitroxides also exhibit a marked solvent dependence, because nitroxides exist as the result of the two **mesomeric** forms **9** and **10**; in apolar solvents, the two forms have the same weight and thus 50% of the spin density resides on the nitrogen atom and the remaining 50% on the oxygen. In contrast, polar solvents will favor form **10** with respect to **9**; as a result, an increase of the nitrogen splitting is observed, which is particularly evident for solvents where hydrogen bonding is possible (see structure **11**, Block 8.1).

The stability of nitroxides may be attributed to three factors: electron delocalization within the molecule, steric shielding of the paramagnetic center and stability towards disproportionation. If H-atoms in α -position to the NO moiety are available, disproportionation reactions will be favored, leading to diamagnetic substances. Thus, the majority of stable nitroxides are secondary amine N-oxides without α -hydrogen atoms. Bulky substituents on the α -carbon atoms do not only prevent disproportionation but also the tendency towards dimerization, particularly in the solid state. Thus steric hindrance is mainly responsible for kinetic stability. The more pronounced effect for stability is the electronic configuration of the N-O group. General structures for stable nitroxides are shown in Figure 2.9 with the simplest representative di-*tert*-butylnitroxide DTBN (a). The most common derivatives stem from six-membered piperidine rings (b) and five-membered pyrrolidine (c), oxazolidine (d) pyrroline (e) rings. Since chemical structures of nitroxides are relatively complex, trivial names formed by abbreviations are usually employed.

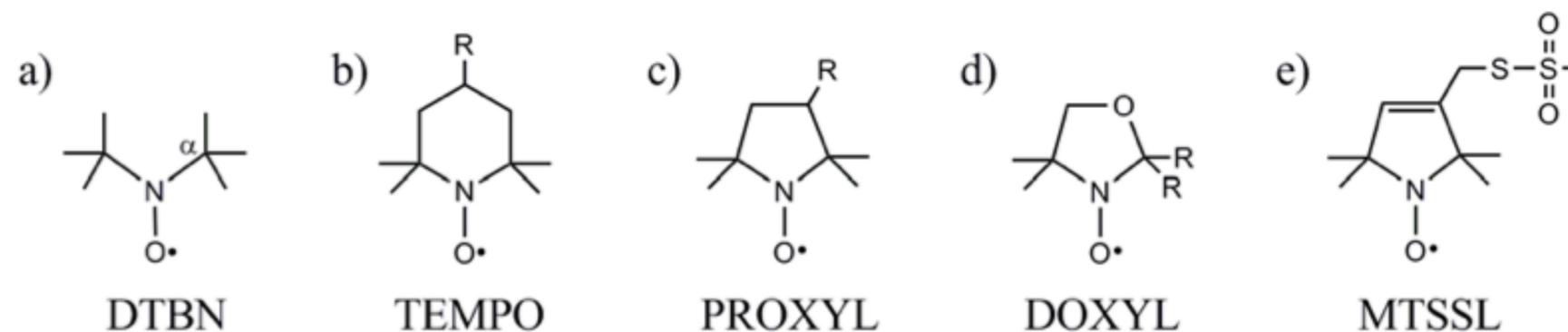
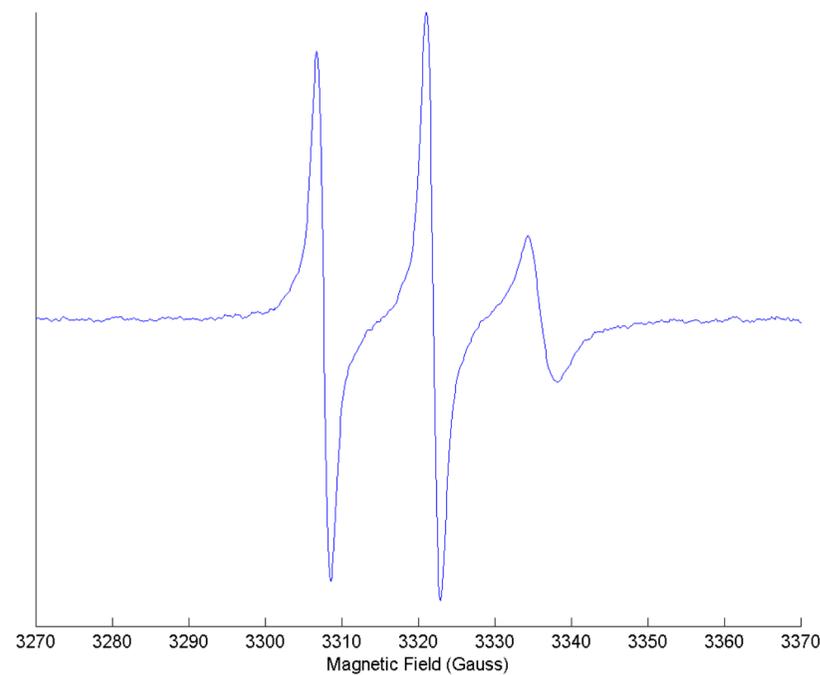


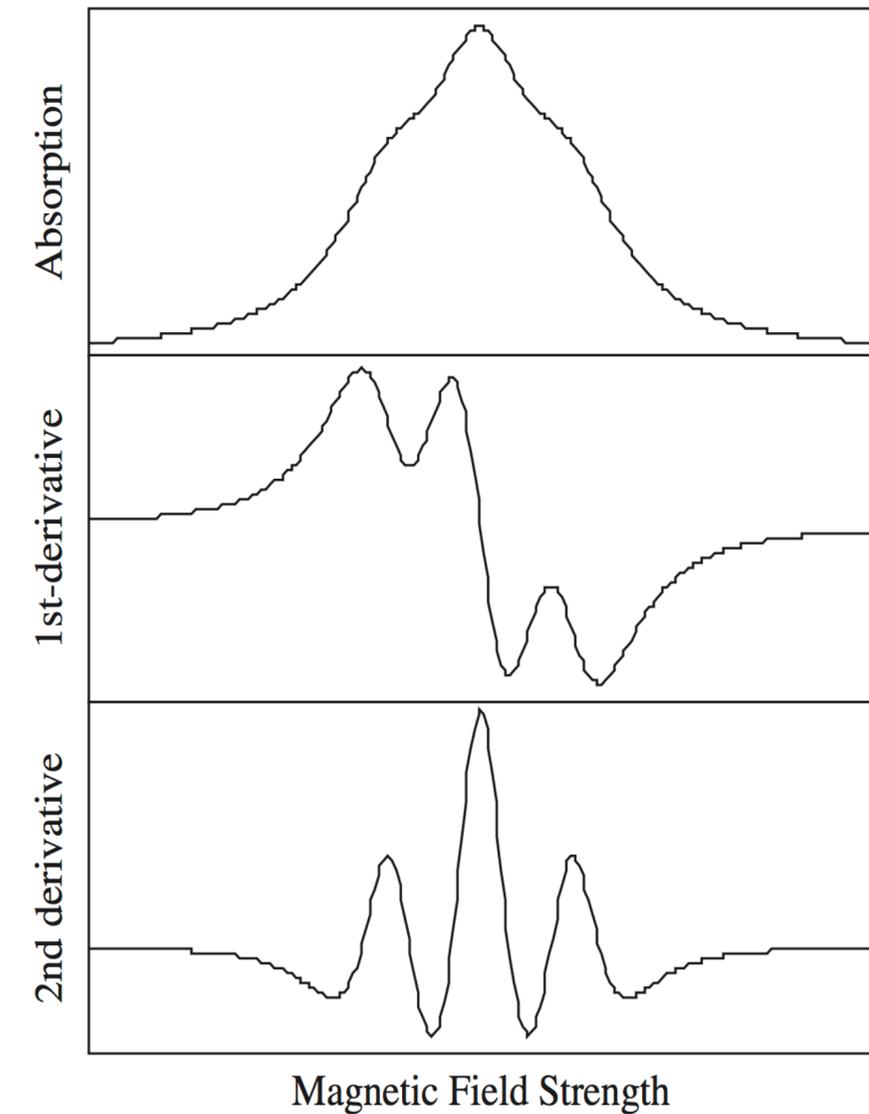
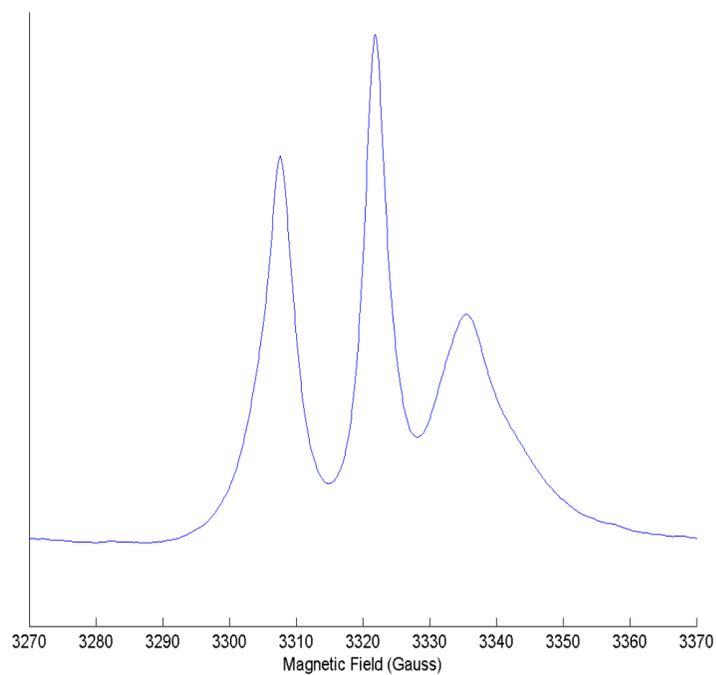
Figure 2.9 The main types of stable nitroxides contain no hydrogen atom at the α -carbon and are cyclic analogs of a) di-*tert*-butyl nitroxide, derivatives of b) piperidine, c) pyrrolidine d) oxazolidine and e) pyrroline. Labeling reaction is possible with suitable functional group R. DTBN: di-*tert*-butyl nitroxide, TEMPO: 2,2,6,6-tetramethylpiperidine-*N*-oxyl, PROXYL: 2,2,4,4-tetramethylpyrrolidine-*N*-oxyl, DOXYL: 4,4-dimethyloxazolidine-*N*-oxyl, MTSSL: (*N*-oxyl-2,2,5,5-tetramethylpyrroline-3-methyl)methane thiosulfonate.

Continuous wave ESR (cw-ESR)

Derivative spectrum



Absorption spectrum



The g -factor: $\Delta E = h\nu = g\beta H$

The field at each spin influenced by local magnetic fields, not just the external field :

$$H_{\text{eff}} = H + H_{\text{local}} \text{ so } H_{\text{eff}} = (1-s)H = (g/g_e)H$$

- This field is induced by H , external field H
- g is an effective Zeeman factor, shifted from the electron g_e
- The shift in g is akin to the chemical shift of NMR
- The local induced field comes from the orbital motion of electrons, spin-orbit coupling mixes J , L and S and shifts g , the shift can be $g < 2$ or $g > 2$. g is thus characteristic of different electronic structures and is also known as the

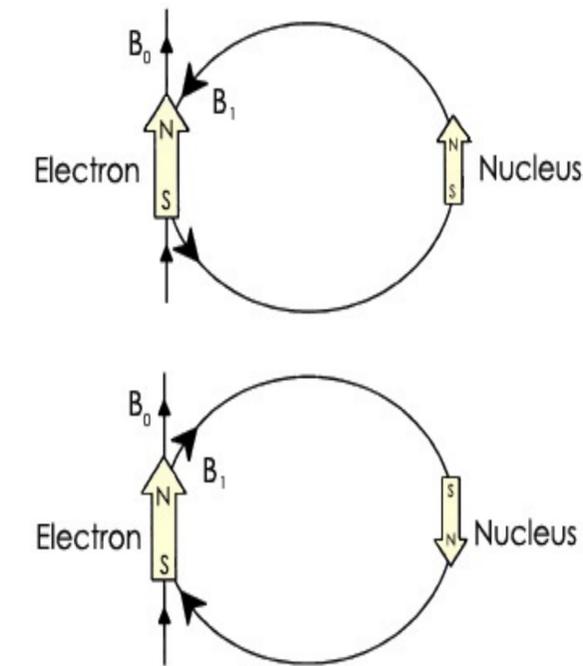
Landé splitting factor:

$$g = 1 + \frac{J(J+1) + S(S+1) - L(l+1)}{2J(J+1)}$$

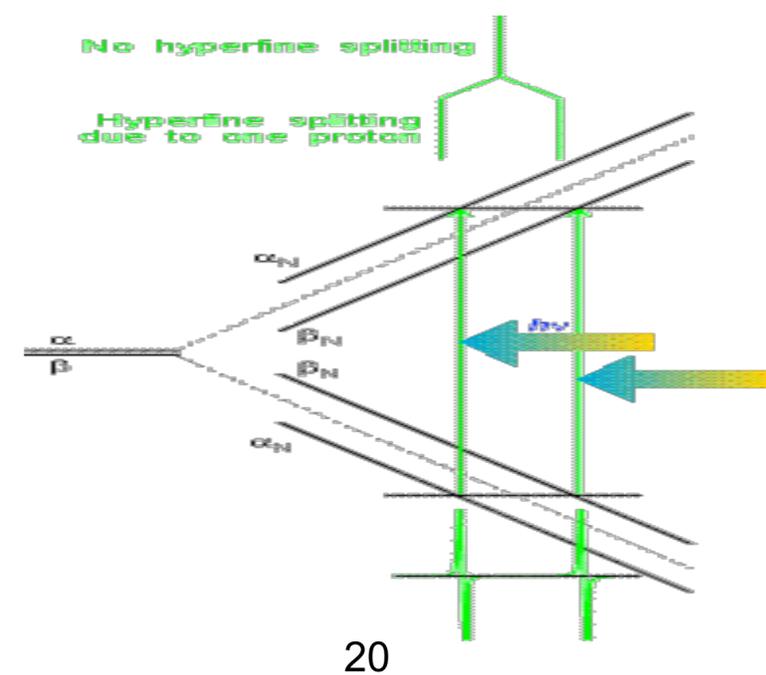
- Light atoms, *i.e.* 'organic' and first row transition metals with a single unpaired electron can have g close to 2.0
- Heavier atoms, and molecules or atoms with more than one unpaired electron can have g -values very different from 2

A - the hyperfine splitting

- The unpaired electron, which gives us the EPR spectrum, is very sensitive to local fields in its surroundings.
- Local fields arising from magnetic nuclei are *permanent and independent of H . ($a \cdot S \cdot I$)*
- Interaction with neighboring nuclear magnetic dipoles gives the *nuclear hyperfine interaction and hyperfine splitting A*
- Corresponds to the NMR coupling constant J
- For several equivalent nuclei n , $(2n_M I_M + 1)$ transitions are observed for a nucleus M with a spin I
- The relative intensities are given by Pascal's triangle for $I = \frac{1}{2}$

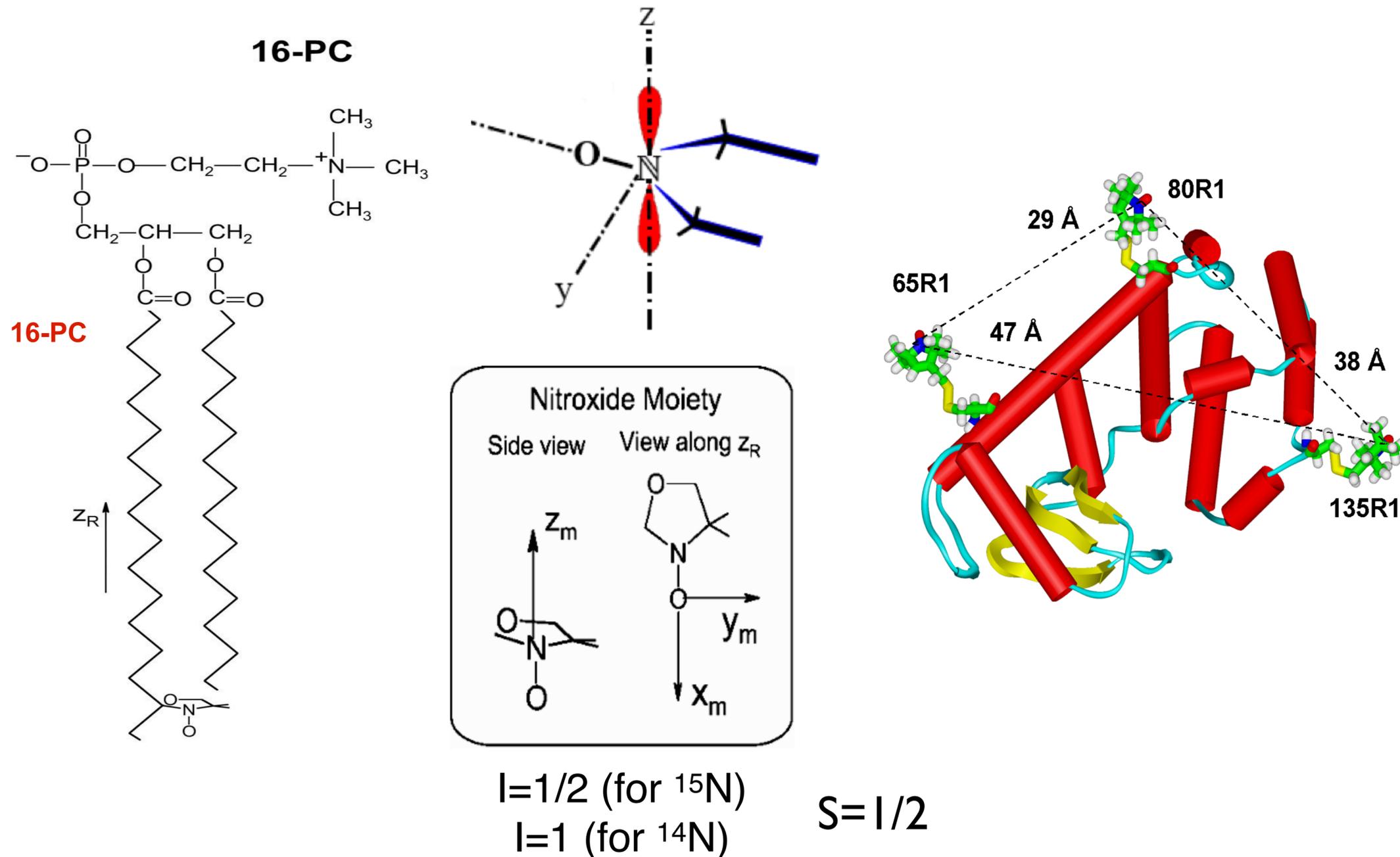


			1		
		1	1		
	1	2	1		
	1	3	3	1	
	1	4	6	4	1
1	5	10	10	5	1



Spin label Electron Spin Resonance

Use spin label to probe the local environment in molecules



$$\text{Hamiltonian} = g\beta H S_z - g_N \beta_N H I_z + a \cdot I \cdot S$$

Electron Nuclear Hyperfine
Zeeman Zeeman

$$\Delta E = h\nu = g\beta H \quad (\text{for } e^-, 1/2 - (-1/2) = 1)$$

$$\frac{\Delta E_e}{\Delta E_n} = \frac{g_e \beta_e H}{g_n \beta_n H} \sim 658 \quad (\text{more sensitive (per spin) than NMR})$$

$$\begin{aligned} \Delta E &= h\nu = g\beta H^* && (m_I=0) \\ &= g\beta H \left(\frac{1}{2} - \left(-\frac{1}{2} \right) \right) + \left(\frac{1}{2} a - \left(-\frac{1}{2} a \right) \right) && (m_I=1) \\ &= g\beta H + a \end{aligned}$$

$$H = H^* - \frac{a}{g\beta} \quad (\text{for } |\alpha_e, m_I = 1\rangle \leftrightarrow |\beta_e, m_I = 1\rangle)$$

(m_I=1)

$$H = H^* + \frac{a}{g\beta} \quad (\text{for } |\alpha_e, m_I = -1\rangle \leftrightarrow |\beta_e, m_I = -1\rangle)$$

(m_I=-1)

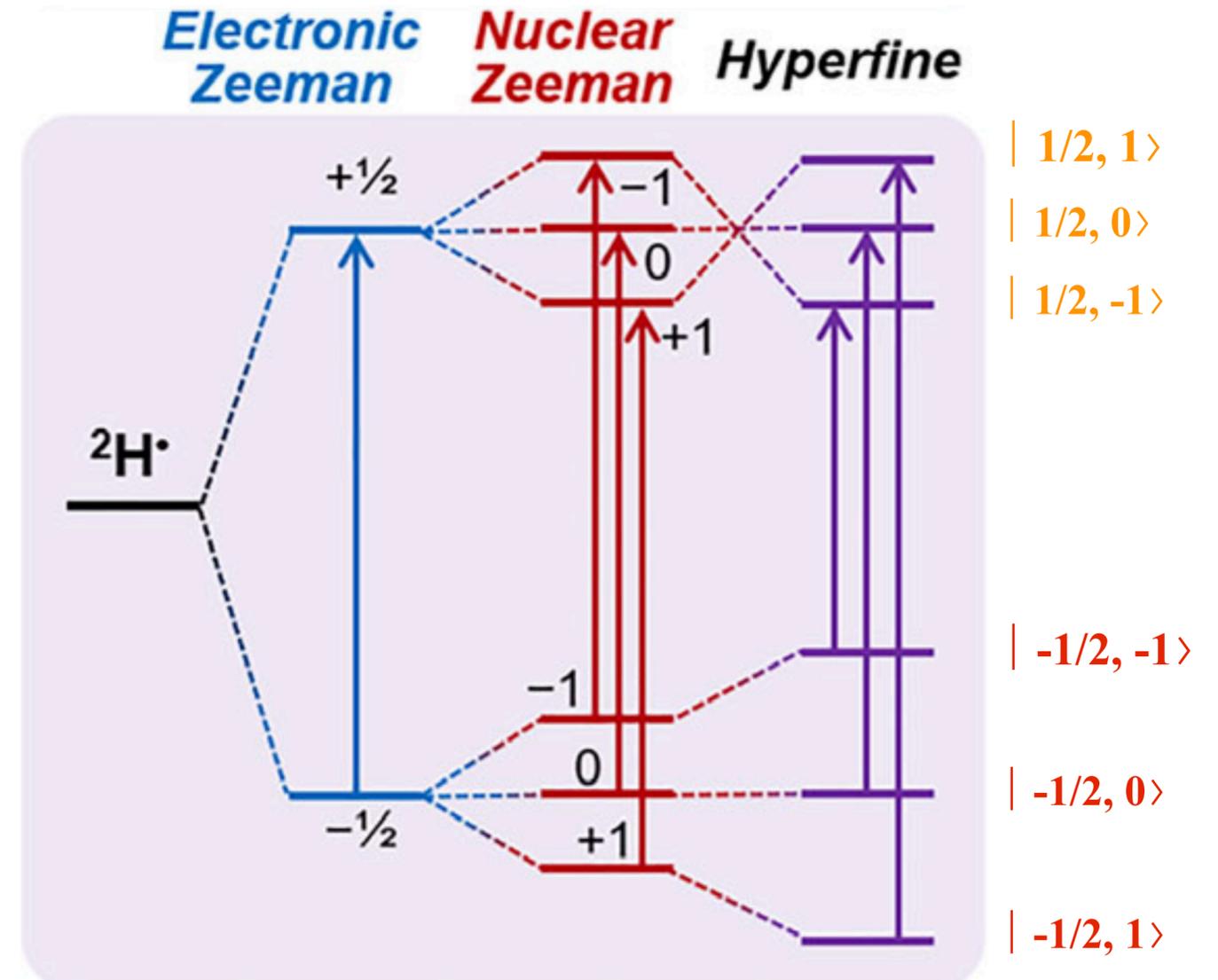
Overall:

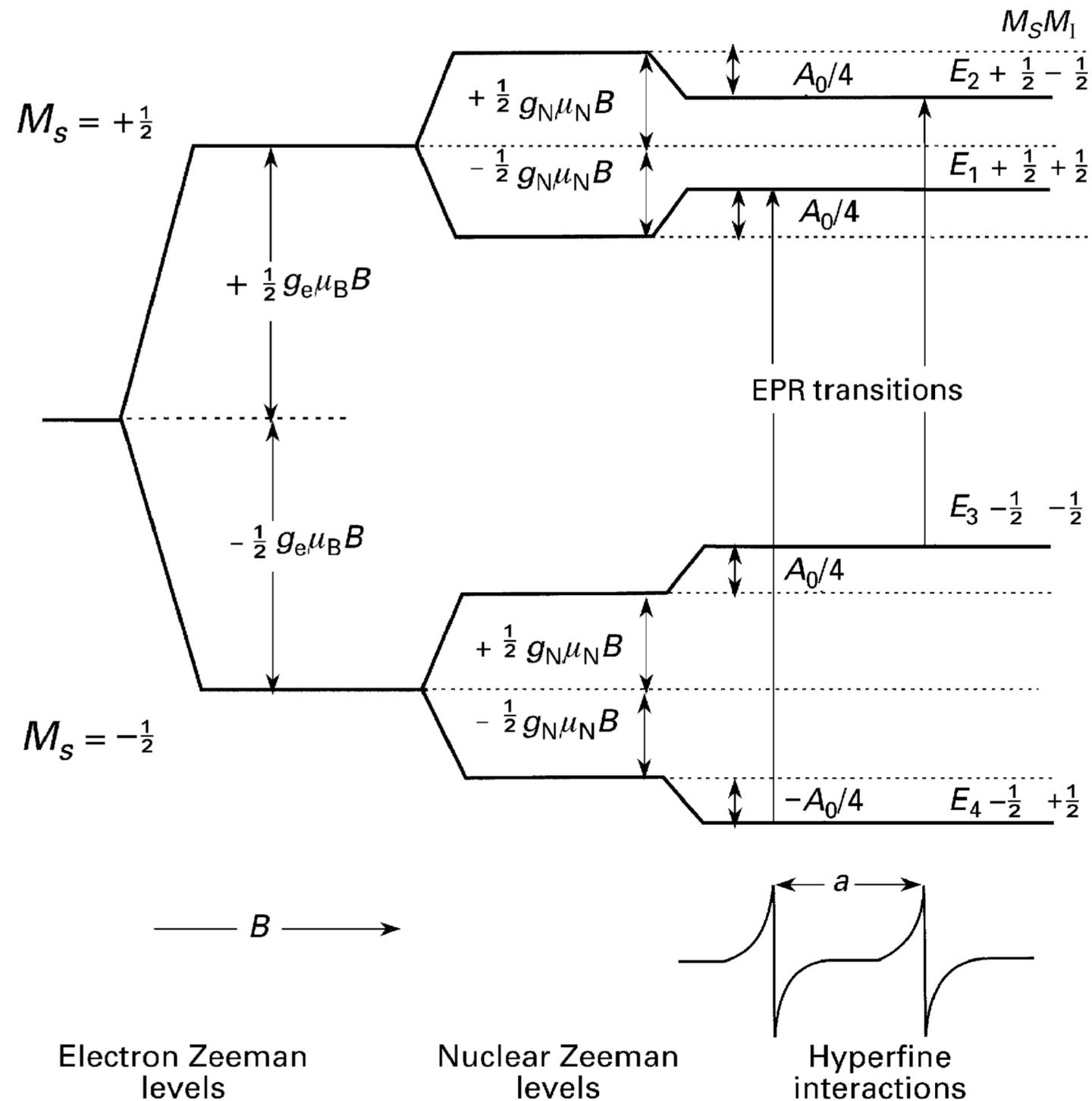
$$H = H^* - \frac{a}{g\beta} m_I$$

$$H = H^* - m_I A \quad \text{for } A = \frac{a}{g\beta}$$

[Gauss]

in terms of angular freq, ω :
 $\omega = \gamma H$ for $\gamma = 2\pi g\beta/h$ (gyromagnetic ratio)





$$E_1 = \frac{1}{2} g_e \mu_B B - \frac{1}{2} g_N \mu_N B + \frac{1}{4} h A_0 \quad \begin{matrix} M_S & M_I \\ +\frac{1}{2} & +\frac{1}{2} \end{matrix}$$

$$E_2 = \frac{1}{2} g_e \mu_B B + \frac{1}{2} g_N \mu_N B - \frac{1}{4} h A_0 \quad \begin{matrix} +\frac{1}{2} & -\frac{1}{2} \end{matrix}$$

$$E_3 = -\frac{1}{2} g_e \mu_B B + \frac{1}{2} g_N \mu_N B + \frac{1}{4} h A_0 \quad \begin{matrix} -\frac{1}{2} & -\frac{1}{2} \end{matrix}$$

$$E_4 = -\frac{1}{2} g_e \mu_B B - \frac{1}{2} g_N \mu_N B - \frac{1}{4} h A_0 \quad \begin{matrix} -\frac{1}{2} & +\frac{1}{2} \end{matrix}$$

$$\Delta M_I = 0 \quad \text{and} \quad \Delta M_S = \pm 1$$

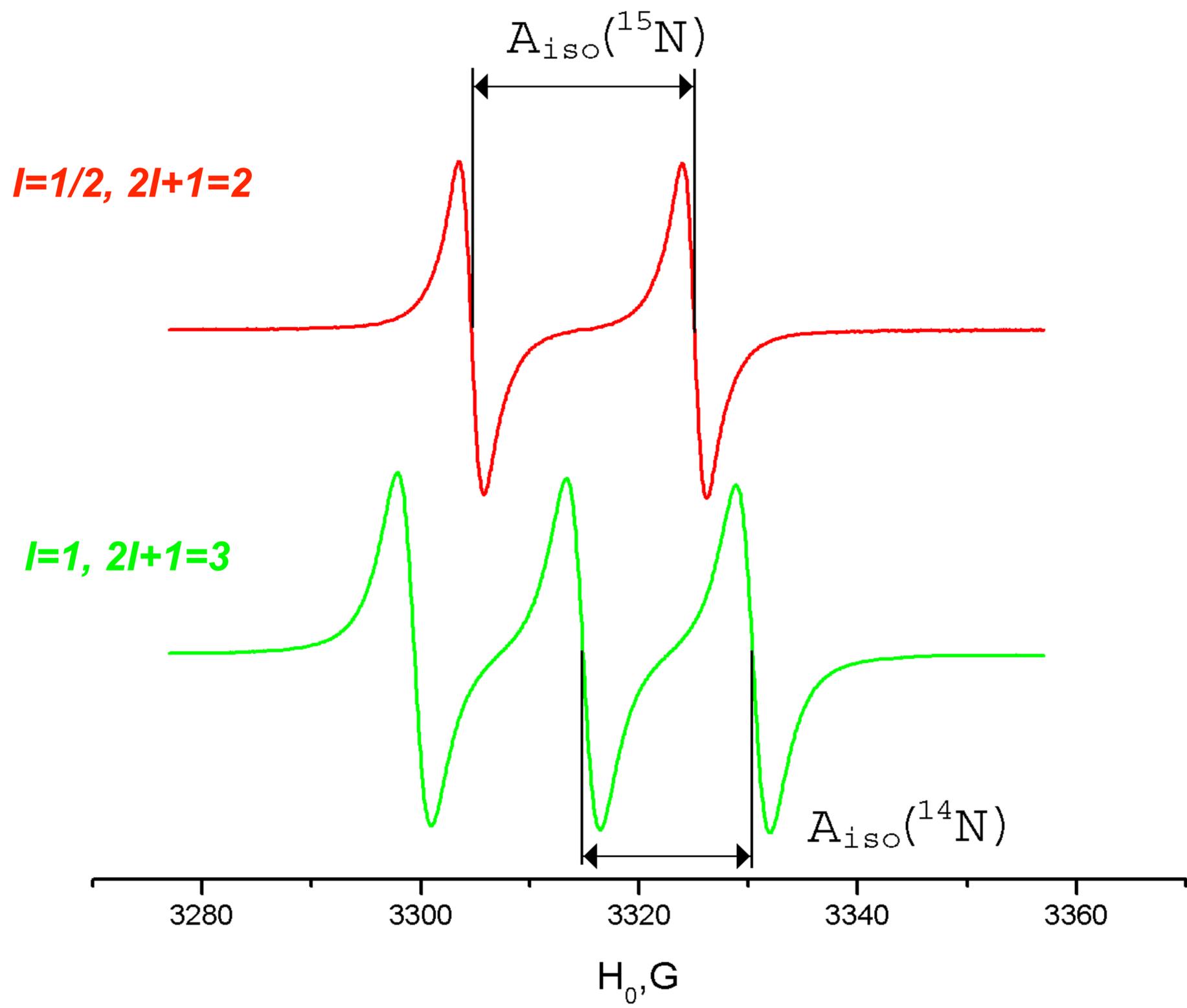
Thus two resonance transitions can occur at

$$\Delta E_A = E_1 - E_4 = g_e \mu_B B + \frac{1}{2} h A_0$$

$$\Delta E_B = E_2 - E_3 = g_e \mu_B B - \frac{1}{2} h A_0$$

$$B_1 = \frac{h\nu}{g_e \mu_B} - \frac{h A_0}{2 g_e \mu_B} = \frac{h\nu}{g_e \mu_B} - \frac{a}{2}$$

$$B_2 = \frac{h\nu}{g_e \mu_B} + \frac{h A_0}{2 g_e \mu_B} = \frac{h\nu}{g_e \mu_B} + \frac{a}{2}$$



Anisotropy in g and A

Many measurements are made in the solid state in EPR spectroscopy.

The ability of EPR to obtain useful information from amorphous (glassy) and polycrystalline (powders) as well as from single crystal materials has attracted much biology and biochemistry research

Usually : g_x, g_y, g_z are not all equal, so g is anisotropic. Same for A_x, A_y, A_z .

For EPR the local symmetry at an unpaired electron center is categorised as :

- **Cubic**. If $x = y = z$ is cubic (*cubic, octahedral, tetrahedral*) No anisotropy in g and A .

- **Uniaxial (Axial)**. If $x = y$, and z is unique.

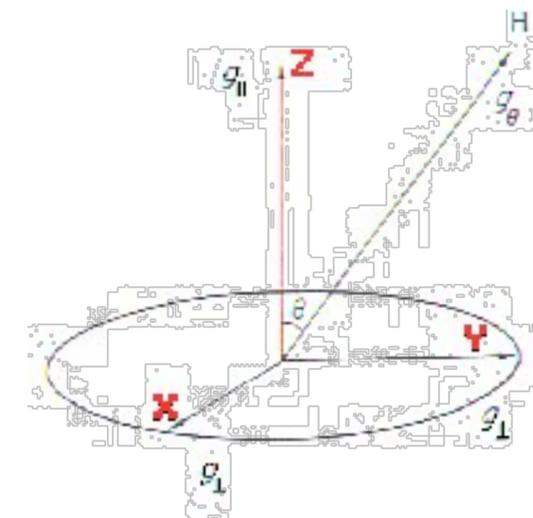
Linear rotation symmetry (at least 3-fold). Two principal values each for g and A . For an arbitrary orientation:

$$g_{\theta}^2 = g_{\perp}^2 \sin^2 \theta + g_{\parallel}^2 \cos^2 \theta$$

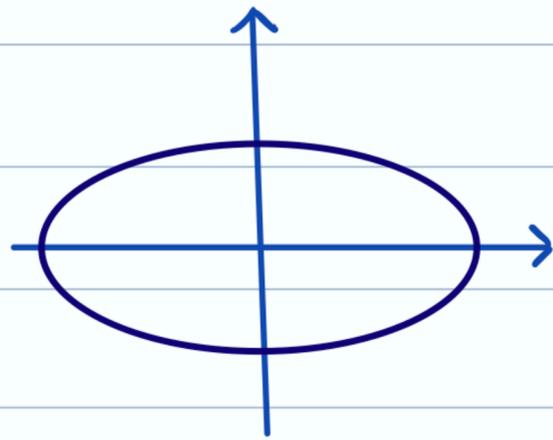
- **Rhombic**. Three unequal components for g and A

For an arbitrary orientation:

$$g^2 = g_{XX}^2 \sin^2 \theta \cos^2 \phi + g_{YY}^2 \sin^2 \theta \sin^2 \phi + g_{ZZ}^2 \cos^2 \theta$$



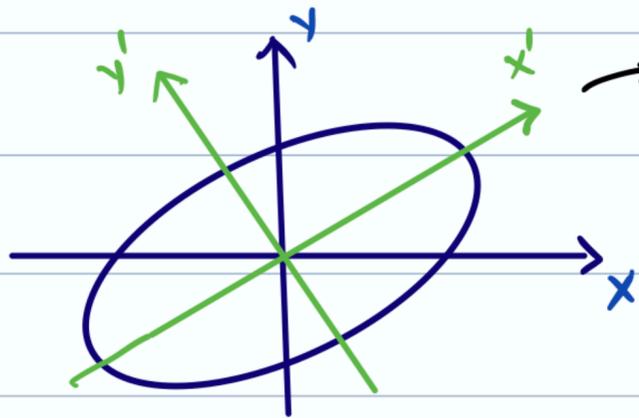
⊙ Principle Axes



$$\rightarrow x^2 + 4y^2 = 1 = (x, y) \begin{pmatrix} 1 & 0 \\ 0 & 4 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

$$= \langle r | B | r \rangle$$

$\underbrace{\hspace{1.5cm}}_{\langle r |}$
 $\underbrace{\hspace{1.5cm}}_B$
 $\underbrace{\hspace{1.5cm}}_{| r \rangle}$



$$\rightarrow \frac{5}{2}x^2 - 3xy + \frac{5}{2}y^2 = 1 = \langle r | \begin{pmatrix} 5/2 & -3/2 \\ -3/2 & 5/2 \end{pmatrix} | r \rangle$$

$\underbrace{\hspace{2.5cm}}_A$

→ To find principle axes

$$\langle r | A | r \rangle = \underbrace{\langle r | R}_{\langle r' |} \underbrace{R^{-1} A R}_{\text{diag}} \underbrace{R^{-1} | r \rangle}_{| r' \rangle} = \langle r' | \begin{pmatrix} 1 & 0 \\ 0 & 4 \end{pmatrix} | r' \rangle$$

$$= \langle r' | B | r' \rangle$$

new coord.
 " $\begin{pmatrix} x' \\ y' \end{pmatrix}$

Construction of g matrix

$$\hat{\mathcal{H}} = \beta_e [B_X \ B_Y \ B_Z] \cdot \begin{bmatrix} g_{\perp} & 0 & 0 \\ 0 & g_{\perp} & 0 \\ 0 & 0 & g_{\parallel} \end{bmatrix} \cdot \begin{bmatrix} \hat{S}_X \\ \hat{S}_Y \\ \hat{S}_Z \end{bmatrix}$$

magnetic moment

$$\hat{\boldsymbol{\mu}} = \beta_e \mathbf{g} \cdot \hat{\mathbf{S}}$$

$$= \beta_e \mathbf{B}^T \cdot \mathbf{g} \cdot \hat{\mathbf{S}}$$

which is taken to interact with the field \mathbf{B} (see Eqs. 1.14).

Alternatively, the product $\mathbf{B}^T \cdot \mathbf{g}$ in Eq. 4.4c may be regarded as a vector resulting from a transformation of the actual field \mathbf{B} to an effective field

$$\mathbf{B}_{\text{eff}} = \mathbf{g}^T \cdot \mathbf{B} / g_e \quad (4.9a)$$

or equivalently

$$\mathbf{B}_{\text{eff}}^T \equiv \mathbf{B}^T \cdot \mathbf{g} / g_e \quad (4.9b)$$

The magnitude of the effective field is given by

$$B_{\text{eff}} = [(\mathbf{g}^T \cdot \mathbf{B})^T \cdot (\mathbf{g}^T \cdot \mathbf{B})]^{1/2} / g_e \quad (4.10a)$$

$$= [\mathbf{B}^T \cdot \mathbf{g} \cdot \mathbf{g}^T \cdot \mathbf{B}]^{1/2} / g_e \quad (4.10b)$$

$$= \{ [\mathbf{n}^T \cdot (\mathbf{g} \cdot \mathbf{g}^T) \cdot \mathbf{n}]^{1/2} / g_e \} B \quad (4.10c)$$

$$\mathbf{n} = \mathbf{B} / B$$

$$= \begin{bmatrix} c_x \\ c_y \\ c_z \end{bmatrix}$$

$$\mathbf{n}^T = [\sin \theta \cos \phi \quad \sin \theta \sin \phi \quad \cos \theta]$$

$$\sqrt{\langle \mathbf{n} | \mathbf{g} \rangle \langle \mathbf{g} | \mathbf{n} \rangle}$$

is the unit vector along \mathbf{B} . In concert with Eq. 1.22b, we define

$$g = [\mathbf{n}^T \cdot (\mathbf{g} \cdot \mathbf{g}^T) \cdot \mathbf{n}]^{1/2} \quad \mathbf{n}^T = [\sin \theta \cos \phi \quad \sin \theta \sin \phi \quad \cos \theta]$$

We adopt the definition $\mathbf{g}\mathbf{g} \equiv \mathbf{g} \cdot \mathbf{g}^T$, and now explore some of the properties of this parameter matrix.² Even if \mathbf{g} is asymmetric, **$\mathbf{g}\mathbf{g}$ is always symmetric**. Thus we need write explicitly only the diagonal and upper off-diagonal elements. In any arbitrary cartesian coordinate system x, y, z fixed in the crystal, $\mathbf{g}\mathbf{g}$ is not diagonal, so that

$$g^2 = [c_x \quad c_y \quad c_z] \cdot \begin{bmatrix} (\mathbf{g}\mathbf{g})_{xx} & (\mathbf{g}\mathbf{g})_{xy} & (\mathbf{g}\mathbf{g})_{xz} \\ & (\mathbf{g}\mathbf{g})_{yy} & (\mathbf{g}\mathbf{g})_{yz} \\ & & (\mathbf{g}\mathbf{g})_{zz} \end{bmatrix} \cdot \begin{bmatrix} c_x \\ c_y \\ c_z \end{bmatrix} \quad (4.15)$$

Following the procedure outlined in Section A.5.2, we now turn to the general case of the calculation of matrix $\mathbf{g}\mathbf{g}$ from sets of measurements, for which

$$\begin{aligned} g^2 &= (\mathbf{g}\mathbf{g})_{xx} \sin^2 \theta \cos^2 \phi + 2(\mathbf{g}\mathbf{g})_{xy} \sin^2 \theta \cos \phi \sin \phi \\ &\quad + (\mathbf{g}\mathbf{g})_{yy} \sin^2 \theta \sin^2 \phi + 2(\mathbf{g}\mathbf{g})_{xz} \cos \theta \sin \theta \cos \phi \\ &\quad + 2(\mathbf{g}\mathbf{g})_{yz} \cos \theta \sin \theta \sin \phi + (\mathbf{g}\mathbf{g})_{zz} \cos^2 \theta \end{aligned} \quad (4.16a)$$

The $(\mathbf{g}\mathbf{g})_{ij}$ elements can be determined from experiment by successive rotations of the crystal with \mathbf{n} fixed (or alternatively rotations of the field, i.e., of \mathbf{n} , with the crystal fixed) in the xz , yz , and xy planes. For the xz plane ($\phi = 0$), if θ is the angle between \mathbf{B} and the z axis, $c_x = \sin \theta$, $c_y = 0$, and $c_z = \cos \theta$. Then

$$g^2 = [\sin \theta \quad 0 \quad \cos \theta] \cdot \begin{bmatrix} (\mathbf{g}\mathbf{g})_{xx} & (\mathbf{g}\mathbf{g})_{xy} & (\mathbf{g}\mathbf{g})_{xz} \\ & (\mathbf{g}\mathbf{g})_{yy} & (\mathbf{g}\mathbf{g})_{yz} \\ & & (\mathbf{g}\mathbf{g})_{zz} \end{bmatrix} \cdot \begin{bmatrix} \sin \theta \\ 0 \\ \cos \theta \end{bmatrix} \quad (4.16b)$$

and

$$g^2 = (\mathbf{g}\mathbf{g})_{xx} \sin^2 \theta + 2(\mathbf{g}\mathbf{g})_{xz} \sin \theta \cos \theta + (\mathbf{g}\mathbf{g})_{zz} \cos^2 \theta \quad (4.16c)$$

Similarly, for rotation in the yz plane ($\phi = 90^\circ$), $c_x = 0$, $c_y = \sin \theta$, and $c_z = \cos \theta$ so that

$$g^2 = (\mathbf{g}\mathbf{g})_{yy} \sin^2 \theta + 2(\mathbf{g}\mathbf{g})_{yz} \sin \theta \cos \theta + (\mathbf{g}\mathbf{g})_{zz} \cos^2 \theta \quad (4.17)$$

Likewise, for rotation in the xy plane ($\theta = 90^\circ$), $c_x = \cos \phi$, $c_y = \sin \phi$, and $c_z = 0$ and hence

$$g^2 = (\mathbf{g}\mathbf{g})_{xx} \cos^2 \phi + 2(\mathbf{g}\mathbf{g})_{xy} \sin \phi \cos \phi + (\mathbf{g}\mathbf{g})_{yy} \sin^2 \phi \quad (4.18)$$

$$\begin{aligned}
& \begin{bmatrix} C_{Xx} & C_{Xy} & C_{Xz} \\ C_{Yx} & C_{Yy} & C_{Yz} \\ C_{Zx} & C_{Zy} & C_{Zz} \end{bmatrix} \cdot \begin{bmatrix} (gg)_{xx} & (gg)_{xy} & (gg)_{xz} \\ & (gg)_{yy} & (gg)_{yz} \\ & & (gg)_{zz} \end{bmatrix} \cdot \begin{bmatrix} C_{Xx} & C_{Yx} & C_{Zx} \\ C_{Xy} & C_{Yy} & C_{Zy} \\ C_{Xz} & C_{Yz} & C_{Zz} \end{bmatrix} \\
& \mathbf{C} \qquad \qquad \mathbf{gg} \qquad \qquad \mathbf{C}^T \\
& = \begin{bmatrix} (gg)_X & 0 & 0 \\ & (gg)_Y & 0 \\ & & (gg)_Z \end{bmatrix} \\
& \qquad \qquad \mathbf{d}_{gg}
\end{aligned} \tag{4.19}$$

Idea: single crystal ==> obtain matrix gg ==> solve for C matrix ==> diagonal matrix obtained.

Rotation matrix

$$R = \begin{pmatrix} \cos \alpha \cos \beta \cos \gamma - \sin \alpha \sin \gamma & \sin \alpha \cos \beta \cos \gamma + \cos \alpha \sin \gamma & -\sin \beta \cos \gamma \\ -\cos \alpha \cos \beta \sin \gamma - \sin \alpha \cos \gamma & -\sin \alpha \cos \beta \sin \gamma + \cos \alpha \cos \gamma & \sin \beta \sin \gamma \\ \cos \alpha \sin \beta & \sin \alpha \sin \beta & \cos \beta \end{pmatrix}$$

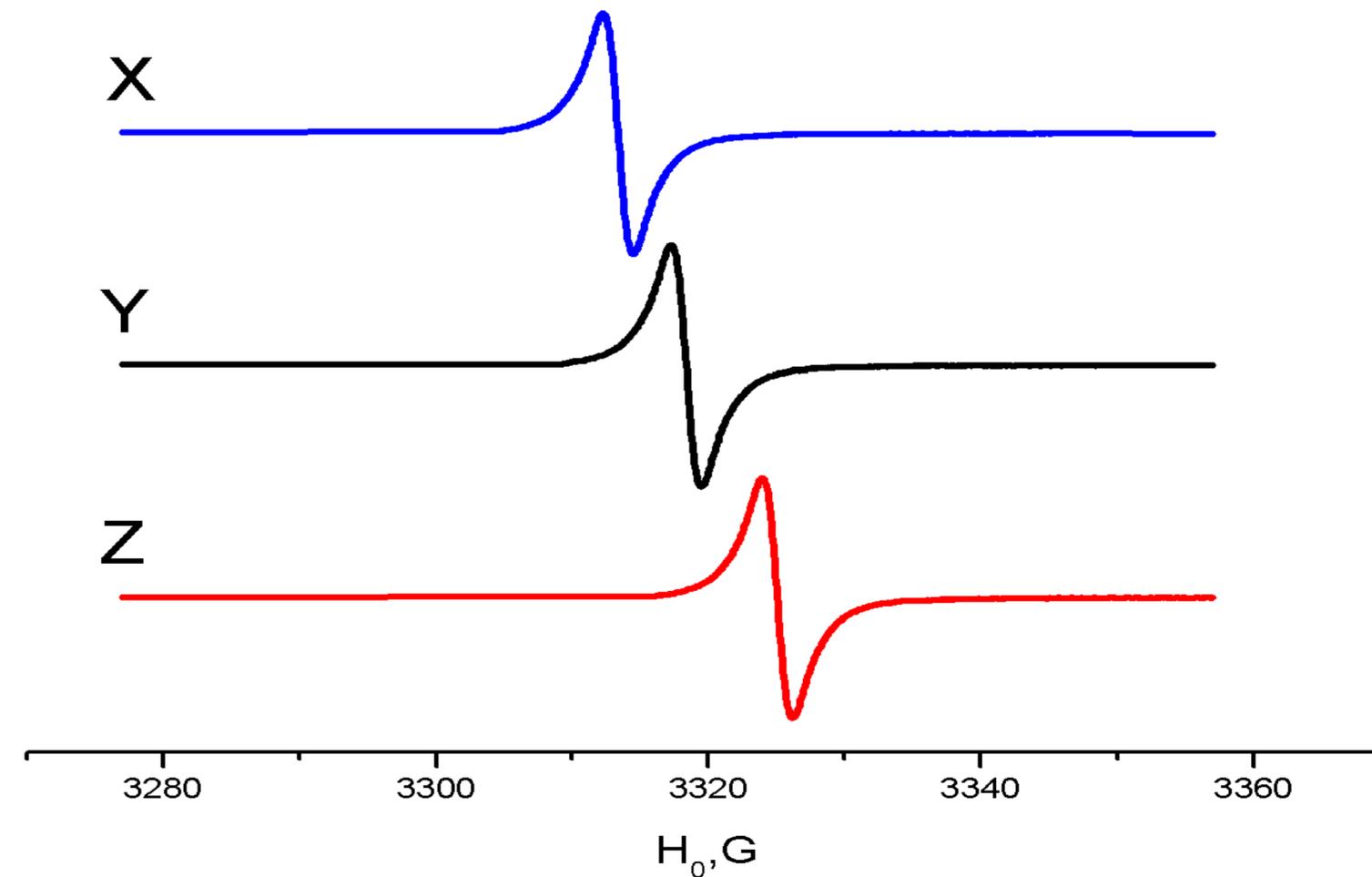
When only g is taken into consideration ...

$$g_x=2.0091, g_y=2.0061, g_z=2.0023$$

The field shift between the X- and Z- orientations is

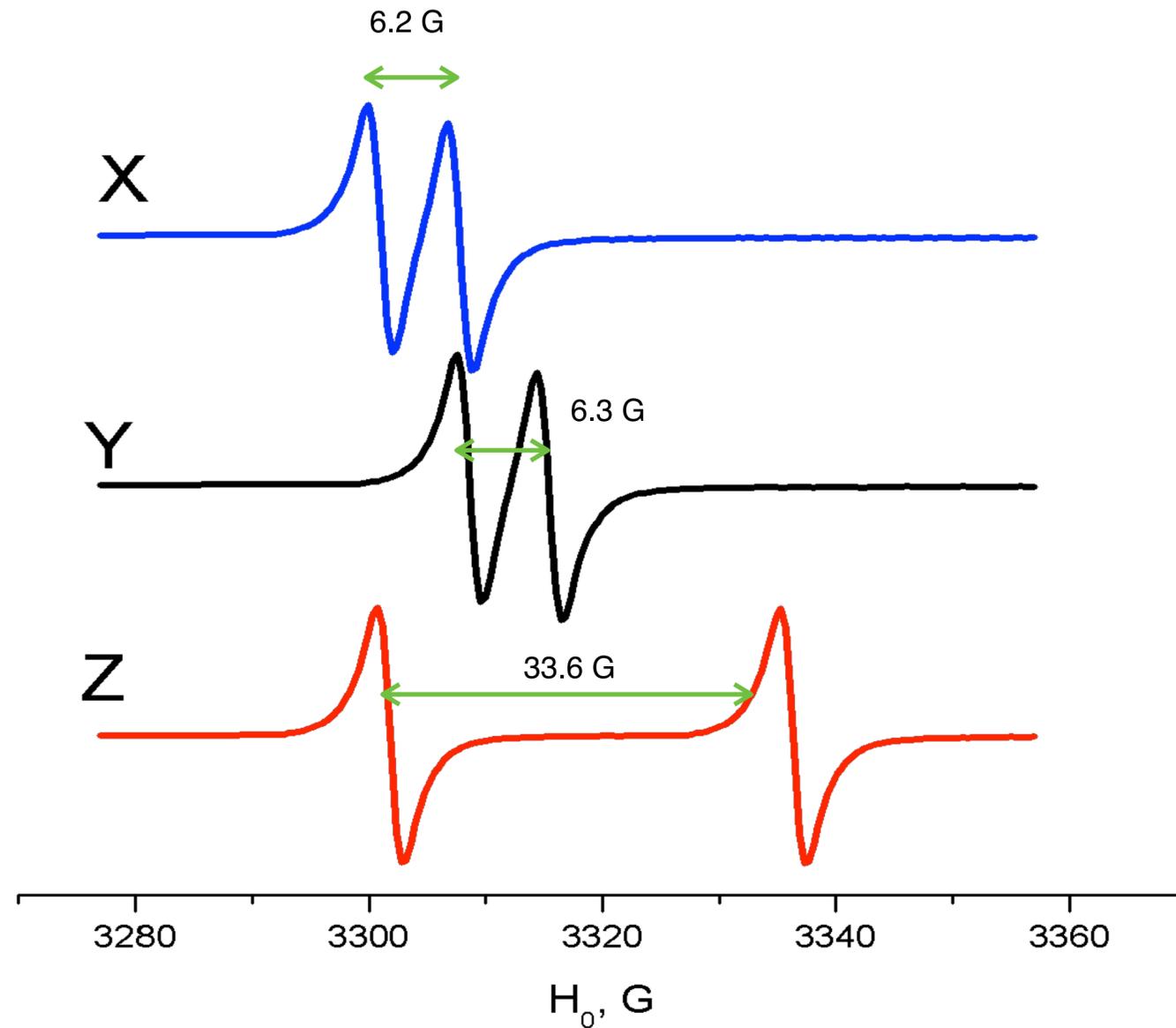
$$\Delta H = h\nu/g_x\beta - h\nu/g_z\beta \cong h\nu\Delta g/4\beta \sim 11\text{ G}$$

$$\Delta E = h\nu = g\beta H$$



$$g_x=2.0091, g_y=2.0061, g_z=2.0023$$

$$I=1/2, A_x=6.2, A_y=6.3, A_z=33.6$$

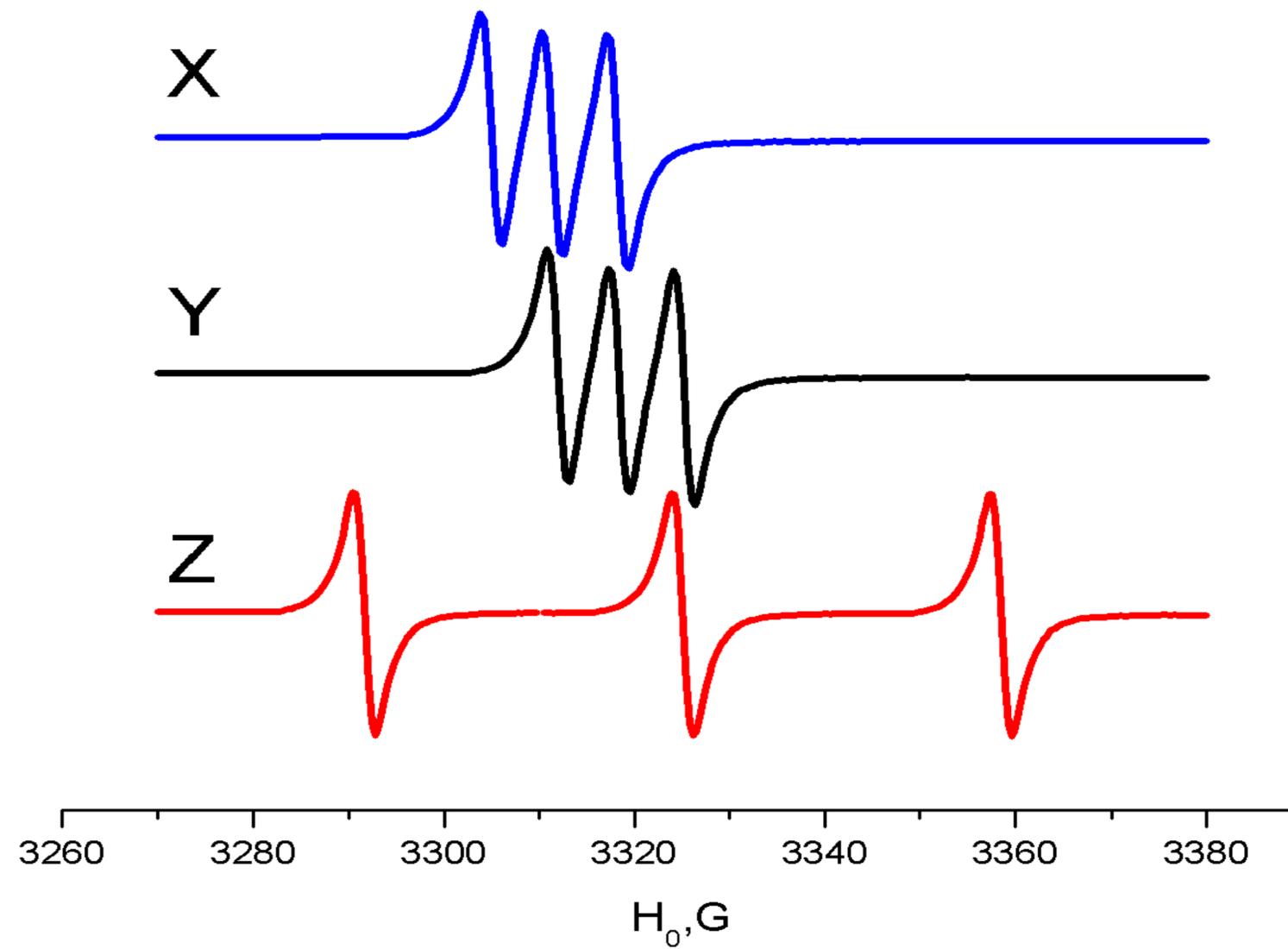


$$H = H^* - \frac{a}{g\beta} m_I$$

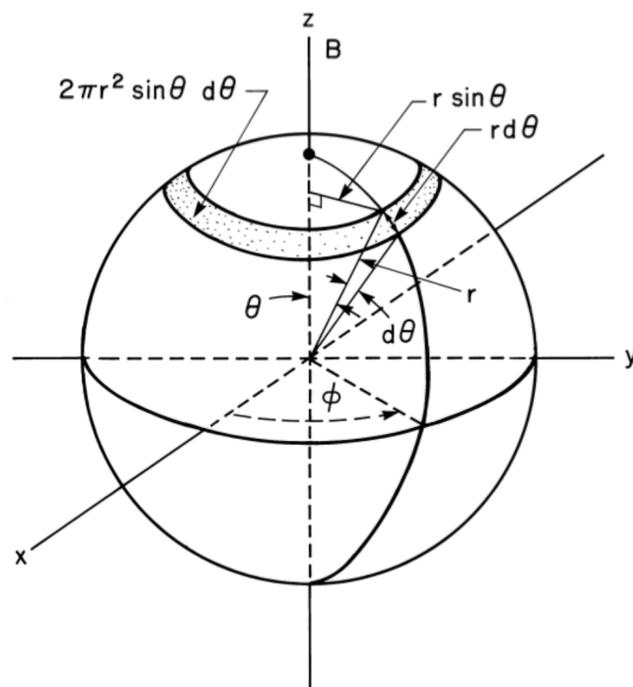
$$= \frac{h\nu}{g\beta} - A m_I$$

$$= \frac{h\nu}{\beta g(\theta, \phi)} - m_I A(\theta, \phi)$$

$$g_x=2.0091, g_y=2.0061, g_z=2.0023$$
$$I=1, A_x= 6.2, A_y = 6.3, A_z=33.6$$



Powder spectra



$S=1/2, l=0, g_x=g_y \ll g_z$ *Axially symmetric g-factor*

$$H_r = \frac{h\nu}{g_{eff} \beta} = \frac{h\nu}{\beta} [g_{\parallel}^2 \cos^2 \theta + g_{\perp}^2 \sin^2 \theta]^{-1/2}$$

θ is the angle between a given symmetry axis and the magnetic field direction

The given solid angle Ω is defined to be the ratio of the surface area A to the total surface area on the sphere: $\Omega = A/4\pi r^2$

$$d\Omega = 2\pi r^2 \sin\theta d\theta / 4\pi r^2 = \sin\theta d\theta / 2$$

$$P(H)dH \propto \sin\theta d\theta \quad P(H) \propto \frac{\sin\theta}{dH / d\theta}$$

$$P(H) \propto \frac{\beta}{h\nu} \frac{(g_{\parallel}^2 \cos^2 \theta + g_{\perp}^2 \sin^2 \theta)^{3/2}}{(g_{\parallel}^2 - g_{\perp}^2) \cos\theta}$$

$$P(H) \propto \frac{\beta}{h\nu} \frac{1}{H_r^3 (g_{\parallel}^2 - g_{\perp}^2) \cos\theta}$$

- The probability $P(H)dH$ of a spin system experiencing a resonant field between H and $H + dH$

The 'effective field' B_{eff} experienced by the electron spin is a superposition of the internal and external fields and the energy of this anisotropic interaction is given by:

$$\text{energy} = H_{EZ} = g_e \frac{\mu_B}{\hbar} \mathbf{B}_{eff} \mathbf{S} = \frac{\mu_B}{\hbar} \mathbf{B}_0^T \mathbf{g} \mathbf{S}, \quad (\text{Note: Hamiltonian} = h\nu = \hbar\omega; \omega [\text{Energy}] = h\nu / \hbar; \mu_B = \beta)$$

$$= \frac{\mu_B}{\hbar} (B_{0,x} \ B_{0,y} \ B_{0,z}) \begin{pmatrix} g_{xx} & & \\ & g_{yy} & \\ & & g_{zz} \end{pmatrix} \begin{pmatrix} S_x \\ S_y \\ S_z \end{pmatrix}$$

(Note: $U^{-1}AU = \text{diag}$; $\langle \text{BIGIS} \rangle = \langle \text{BIU diag}(G) U^{-1}IS \rangle = \langle B_0 | \text{diag}(G) | S_0 \rangle$)

Often used definitions

$$g_{iso} = \frac{1}{3} (g_{xx} + g_{yy} + g_{zz}) = \frac{1}{3} \text{trace}(\mathbf{g})$$

$$\Delta g = g_{zz} - g_{iso} \quad \eta = \frac{g_{yy} - g_{xx}}{\Delta g}$$

a) $g_{xx} = g_{yy} = g_{zz}$ b) $g_{xx} > g_{yy} = g_{zz}$ c) $g_{xx} = g_{yy} > g_{zz}$ d) $g_{xx} > g_{yy} > g_{zz}$

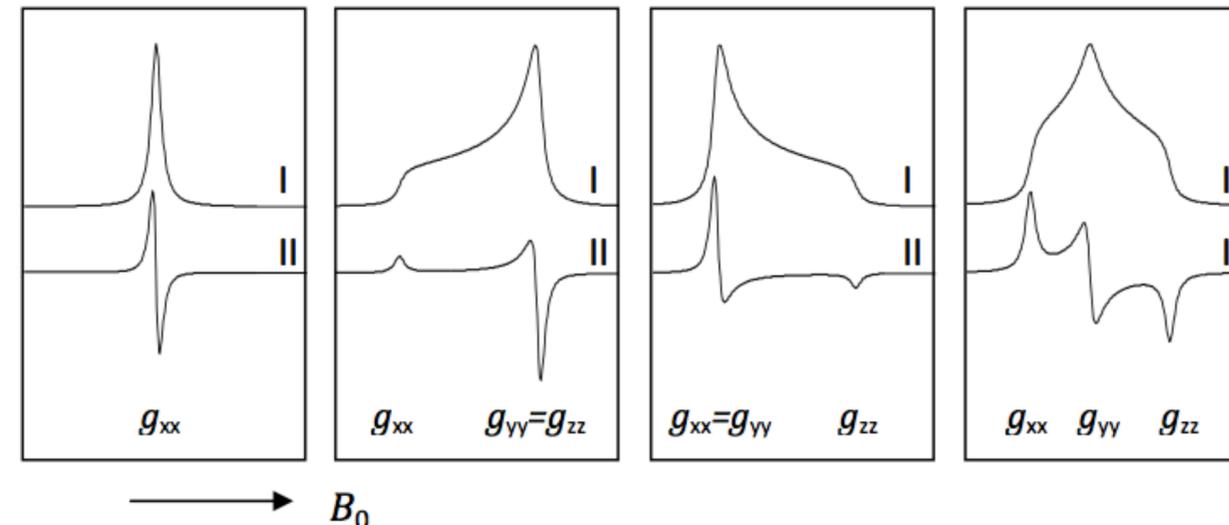
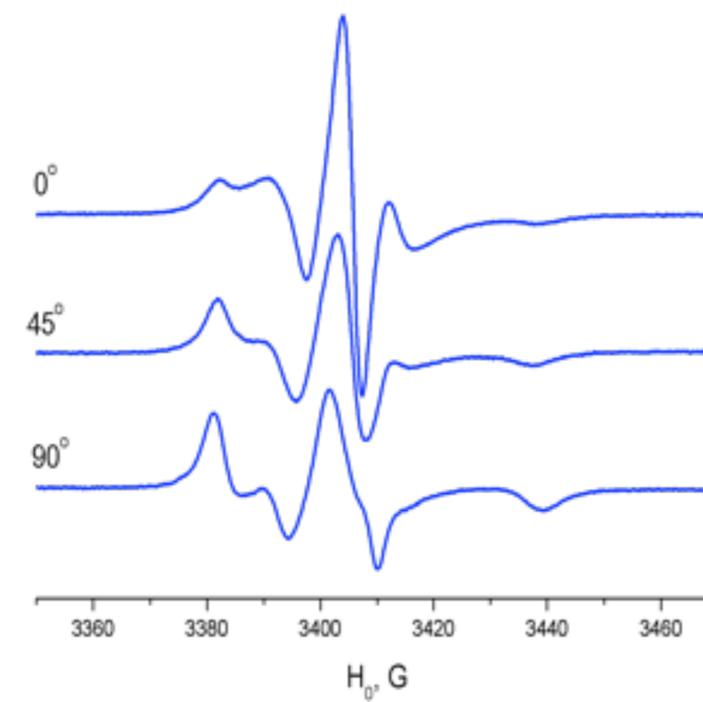
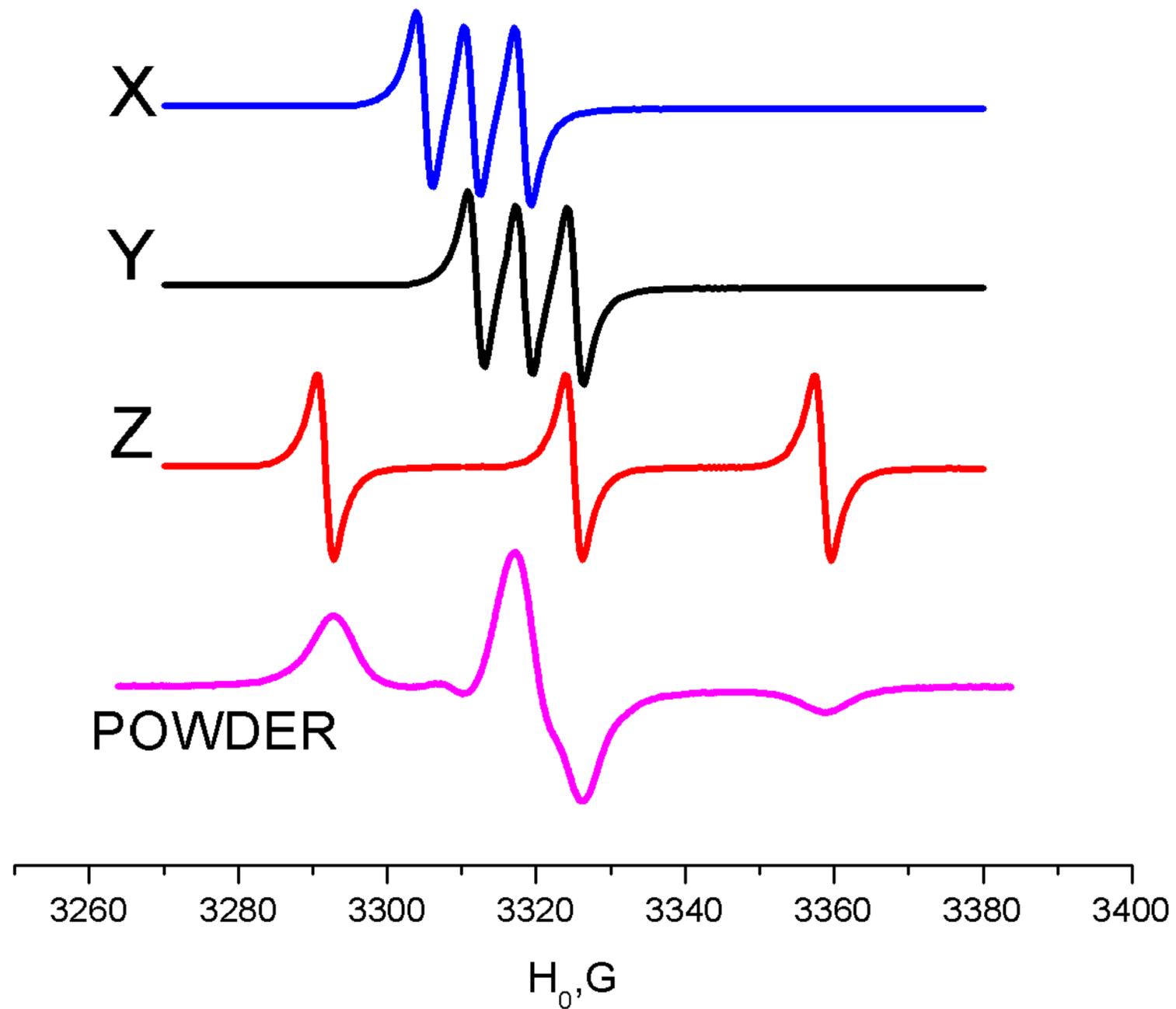


Figure 2.3 Simulated EPR spectra in absorption (I) and first derivative (II) mode for isotropic (a), axial (b,c) and rhombic (d) g-tensor.

On the basis of the element pattern of the \mathbf{g} -matrix several cases of matrix symmetry can be distinguished, namely isotropic, axial, or rhombic. Examples for powder EPR spectra for different \mathbf{g} -anisotropies are shown in Figure 2.3.

$$g_x=2.0091, g_y=2.0061, g_z=2.0023$$
$$I=1, A_x=6.2, A_y=6.3, A_z=33.6$$

9.4 GHz

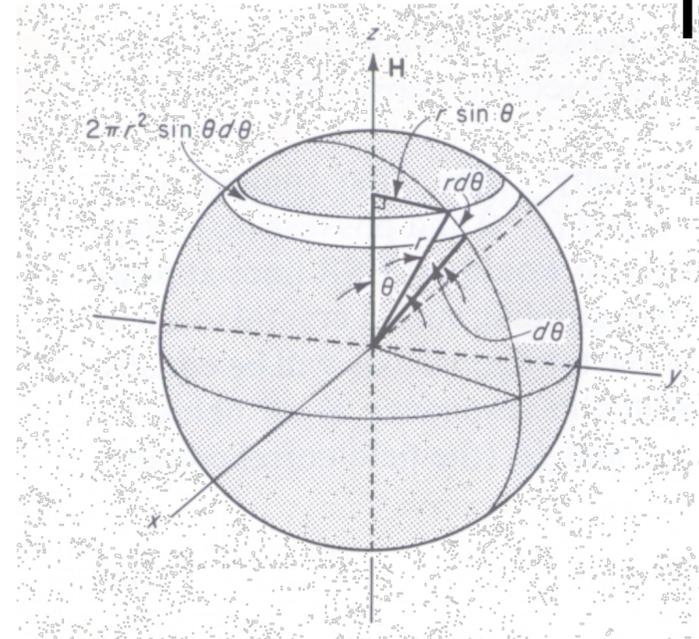
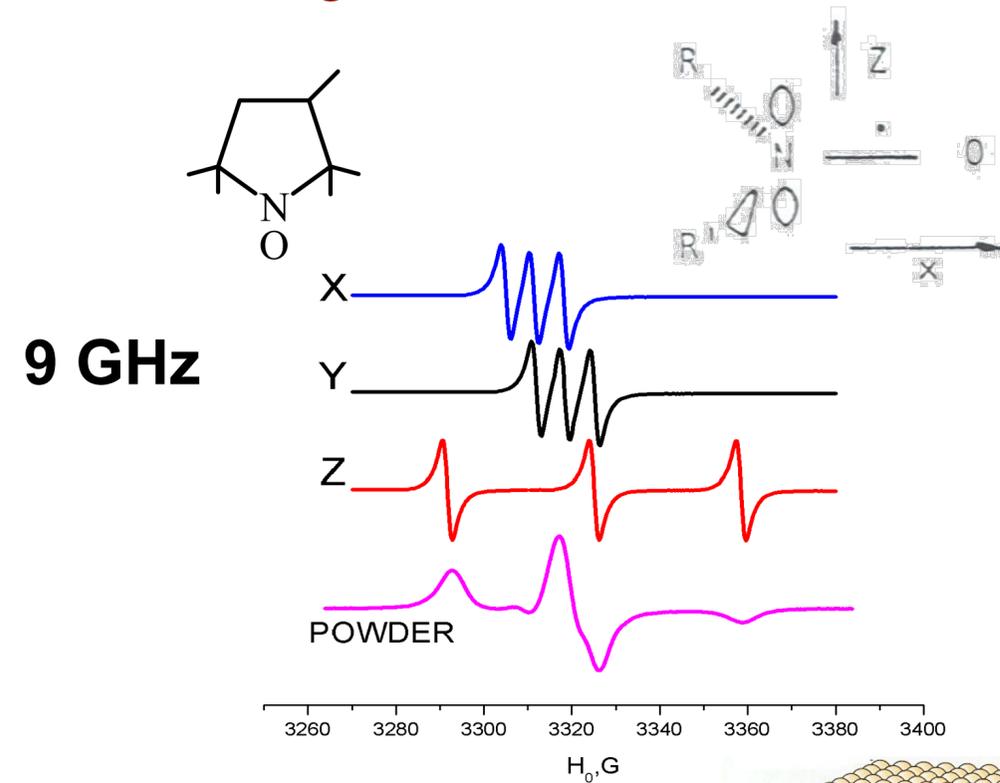


Real data is blurred
due to mosaicity

MOMD: microscopic order – macroscopic disorder.

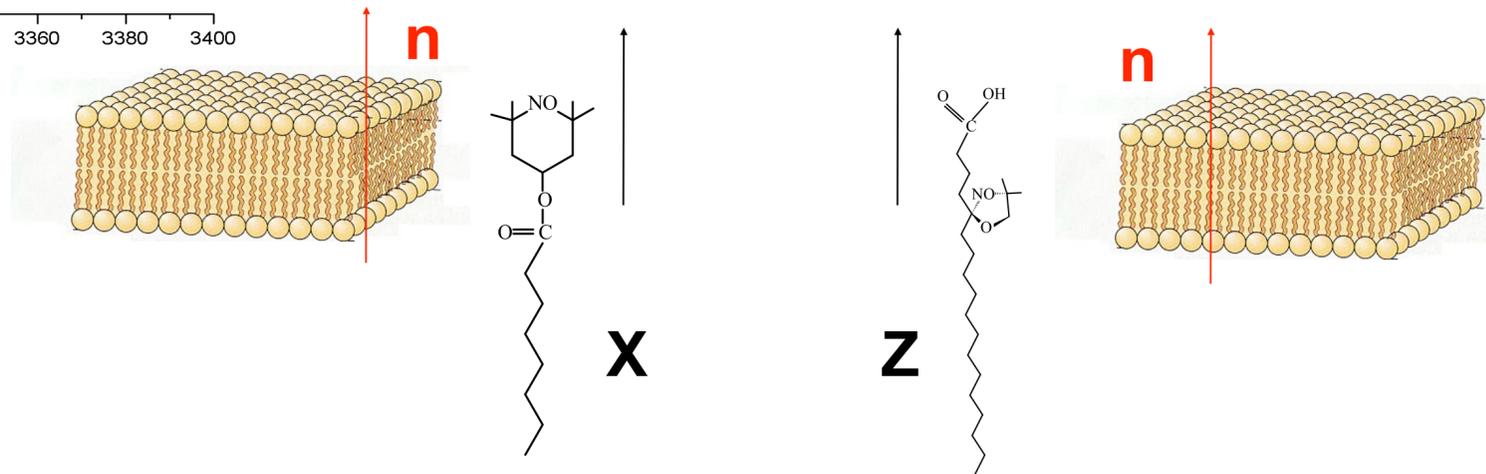
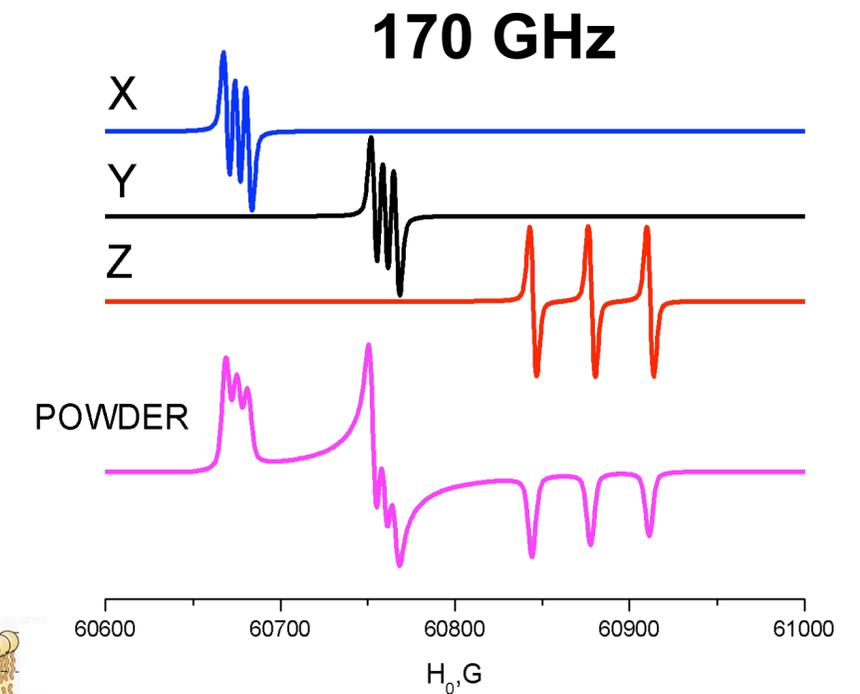
An important case in biology

All orientations of the membrane normal relative to the magnetic field are averaged in vesicles:



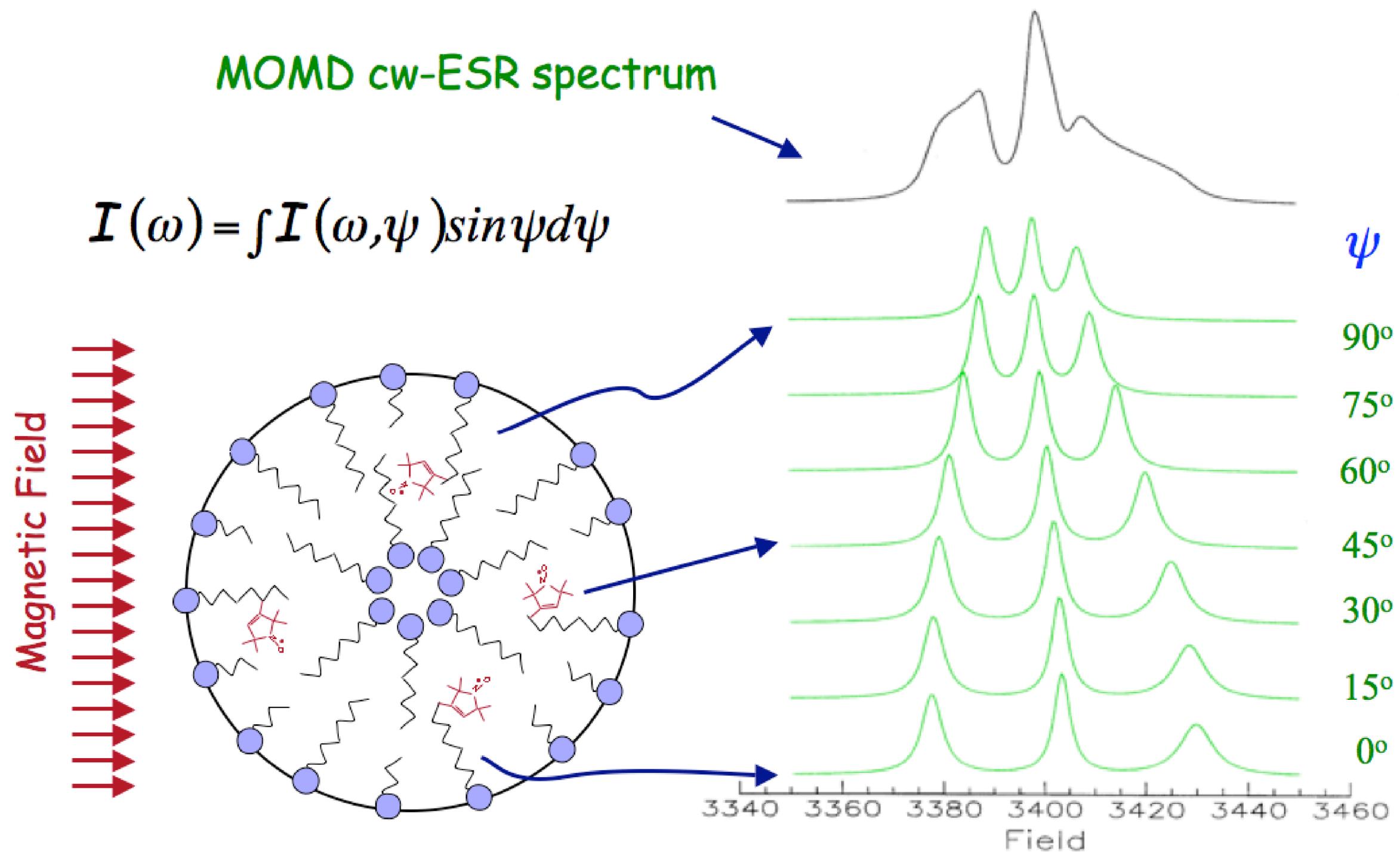
$$g_x=2.0091, g_y=2.0061, g_z=2.0023$$

$$I=1, A_x=6.2, A_y=6.3, A_z=33.6$$



For a macroscopically disordered sample the orientation of the nitroxide moiety manifests itself as a result of anisotropic molecular motion around the principal axis of the molecular frame

Microscopic Ordered and Macroscopic Disorder (MOMD) e.g. Membrane Vesicles



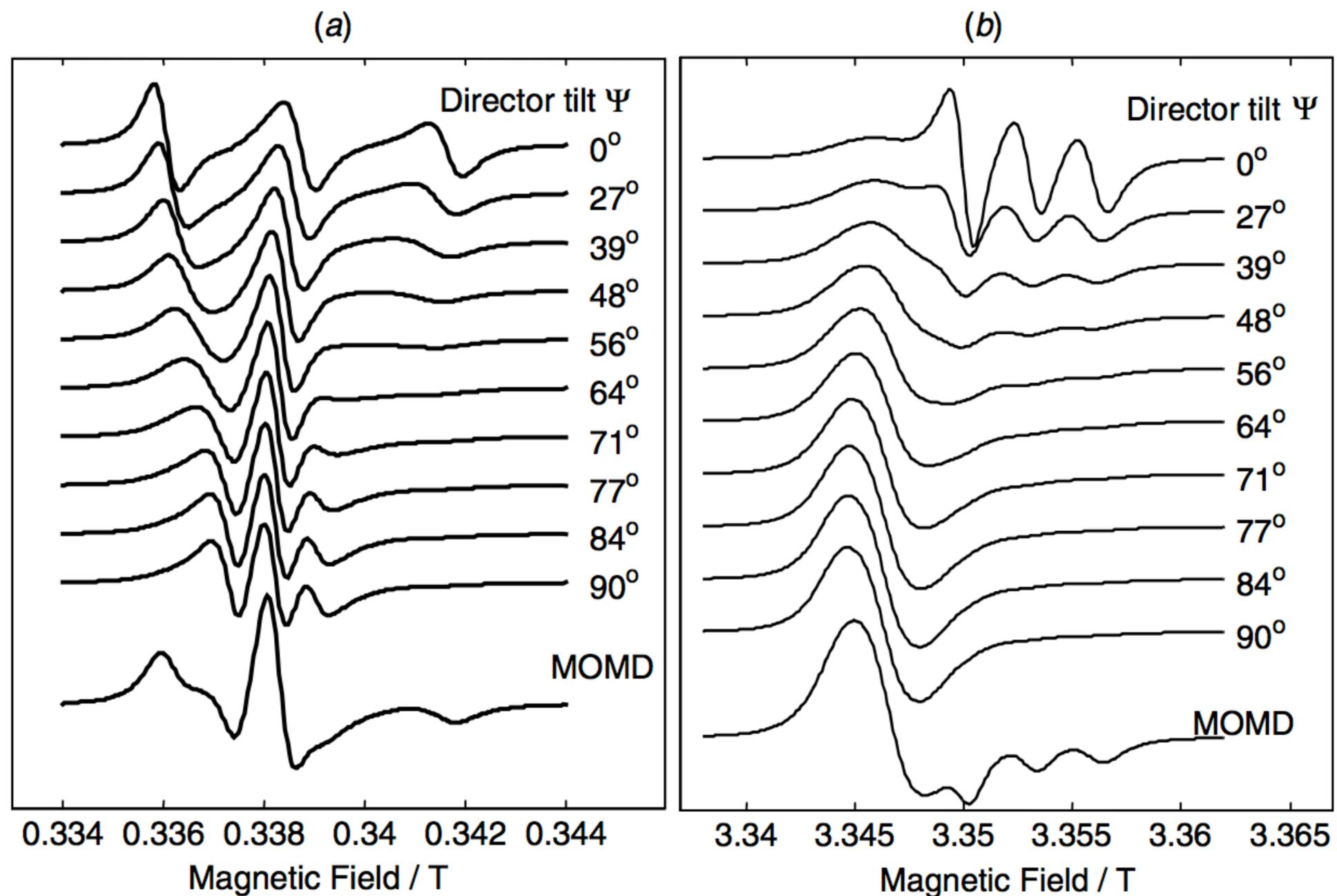


Fig. 12. Components of a MOMD ESR spectrum of a nitroxide spin label, showing the individual spectra from domains with different tilt angles, and integrated MOMD spectrum at the bottom, for 9 GHz (left-hand side) and 94 GHz (right-hand side).

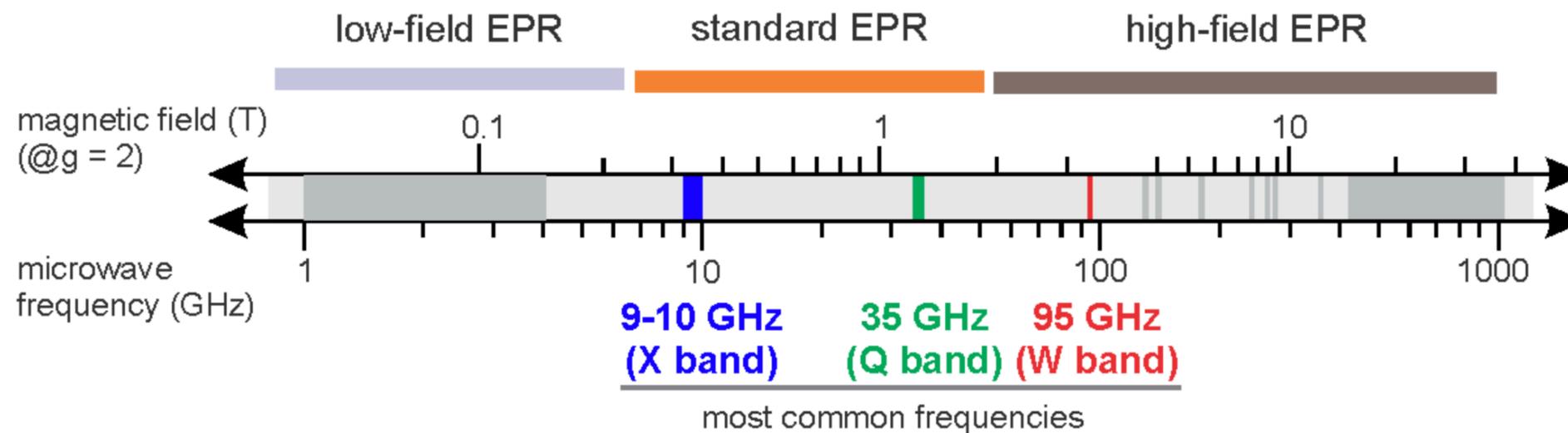
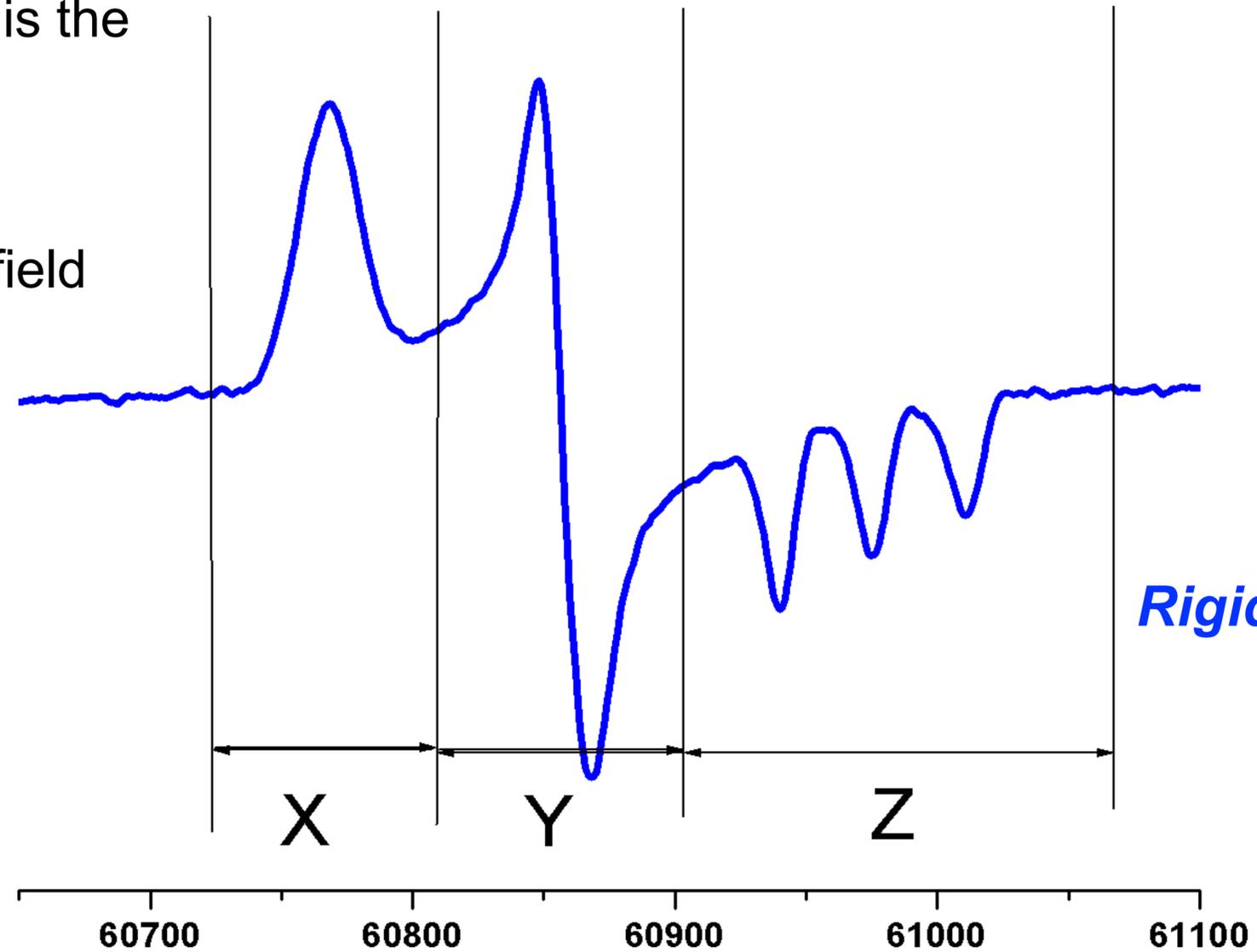
High field EPR spectroscopy is the ***g-resolved spectroscopy***, the regions corresponding different orientations of the magnetic axis relative to the external magnetic field **do not overlap**

$$H = H^* - \frac{a}{g\beta} m_I$$

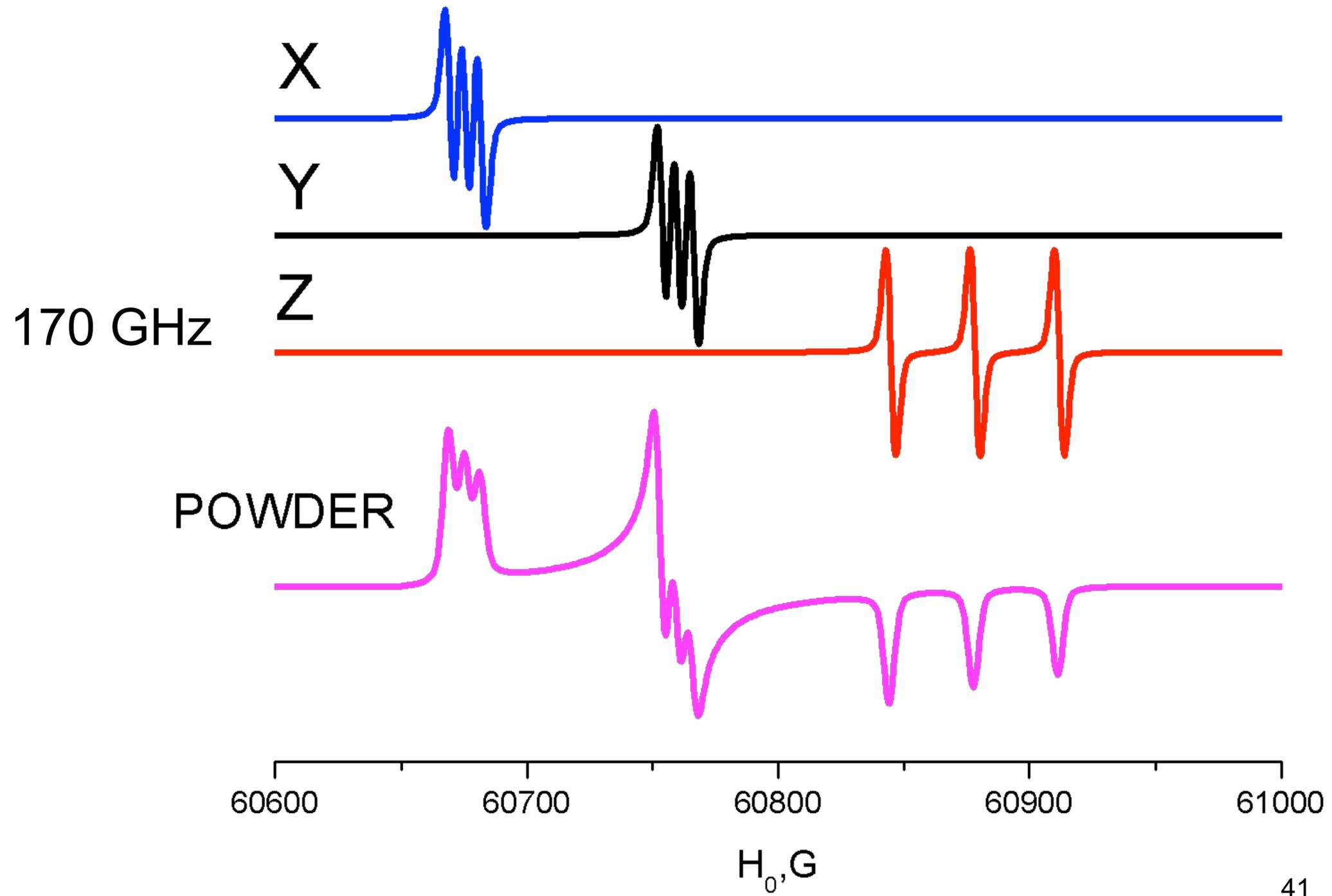
$$= \frac{h\nu}{g\beta} - A m_I$$

$$= \frac{h\nu}{\beta g(\theta, \phi)} - M_I A(\theta, \phi)$$

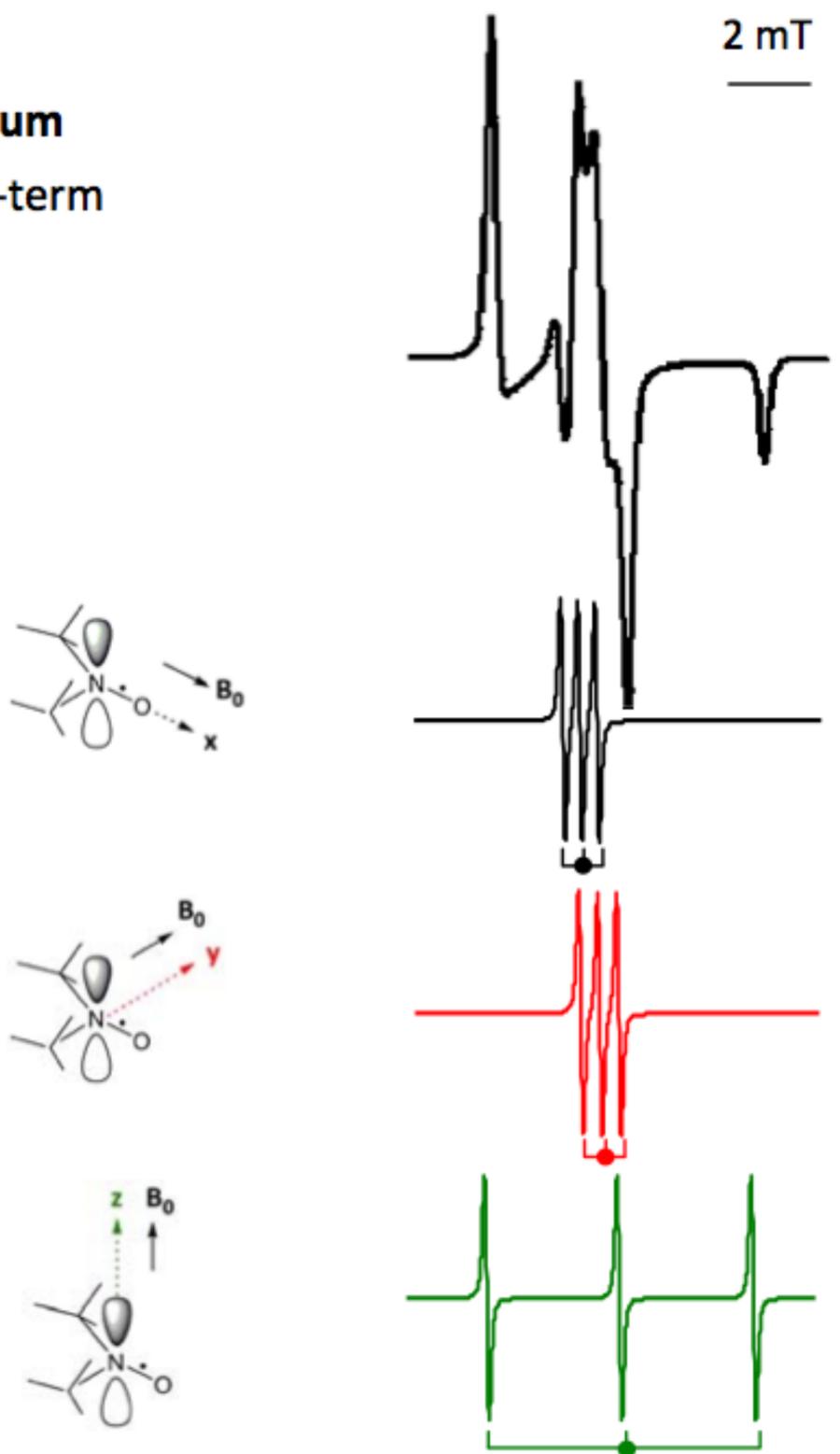
$$H = \frac{h\nu}{g\beta}$$



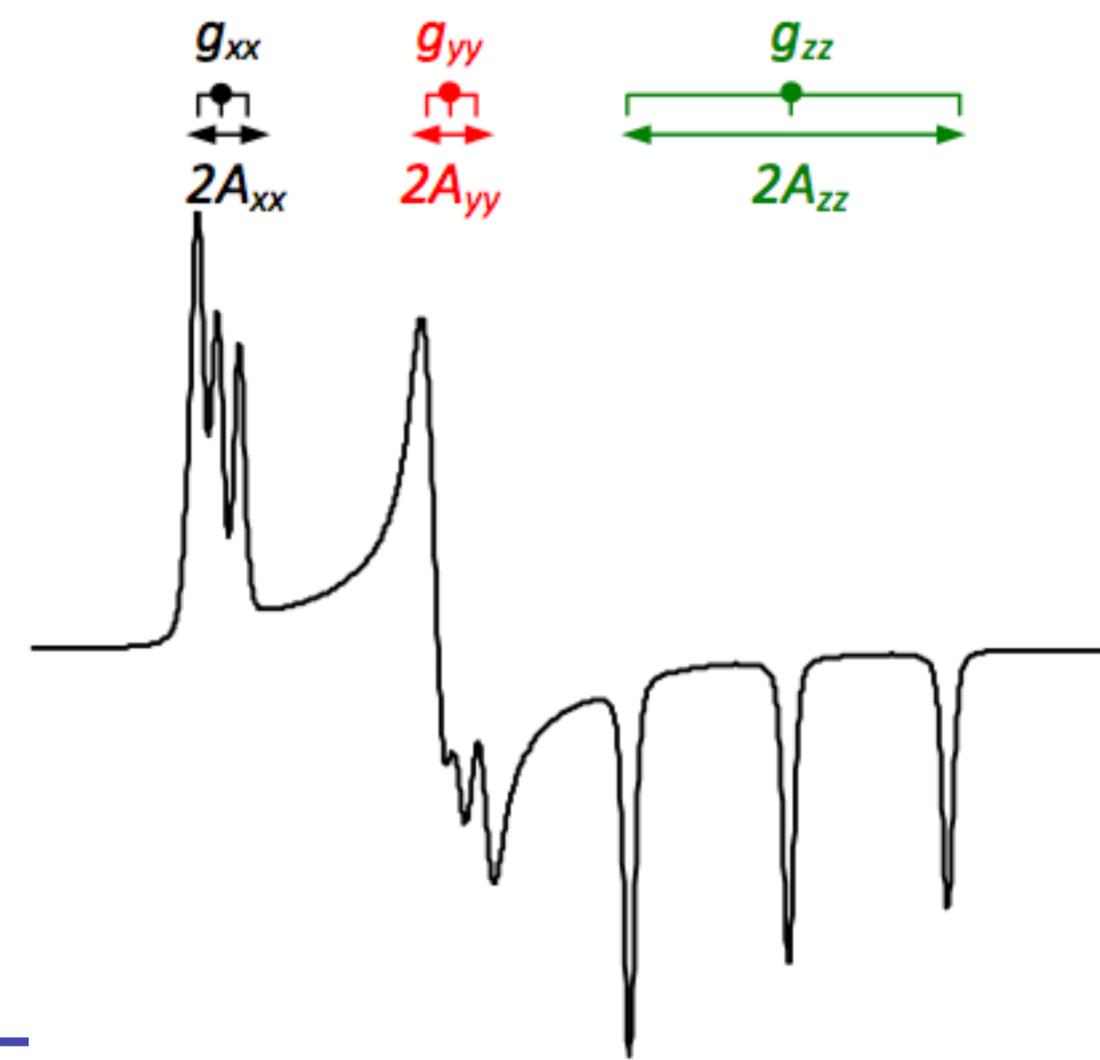
$g_x=2.0091, g_y=2.0061, g_z=2.0023$
 $I=1, A_x= 6.2, A_y = 6.3, A_z=33.6$

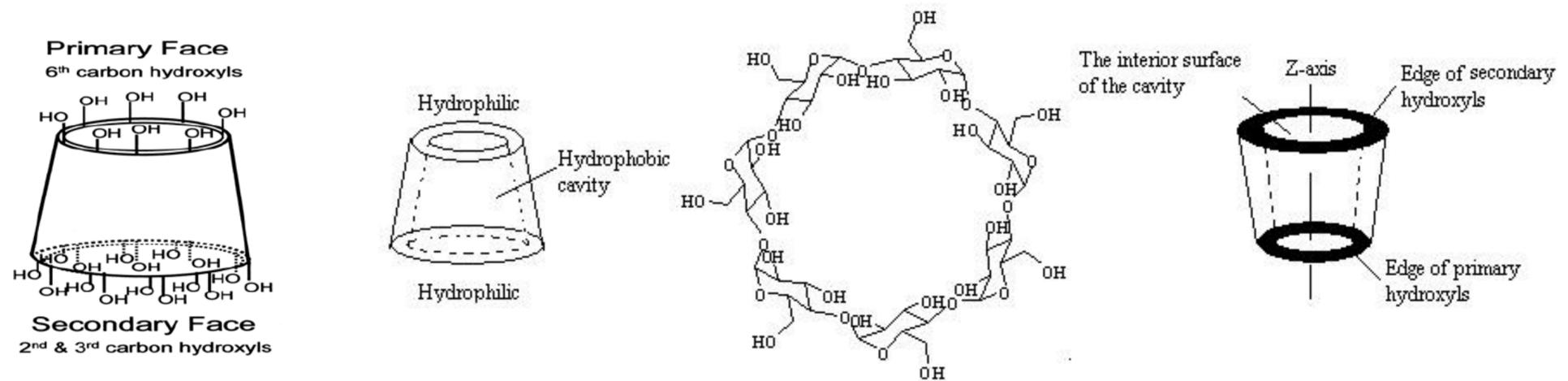


(a) X-band Spectrum
Dominated by HF-term



(b) W-band Spectrum
Dominated by EZ-term





Cyclodextrins (CDs) are cyclic oligomers of D-glucopyranose. Due to the presence of a hydrophobic cavity in the molecule they are able to form guest–host complexes with a variety of organic compounds.

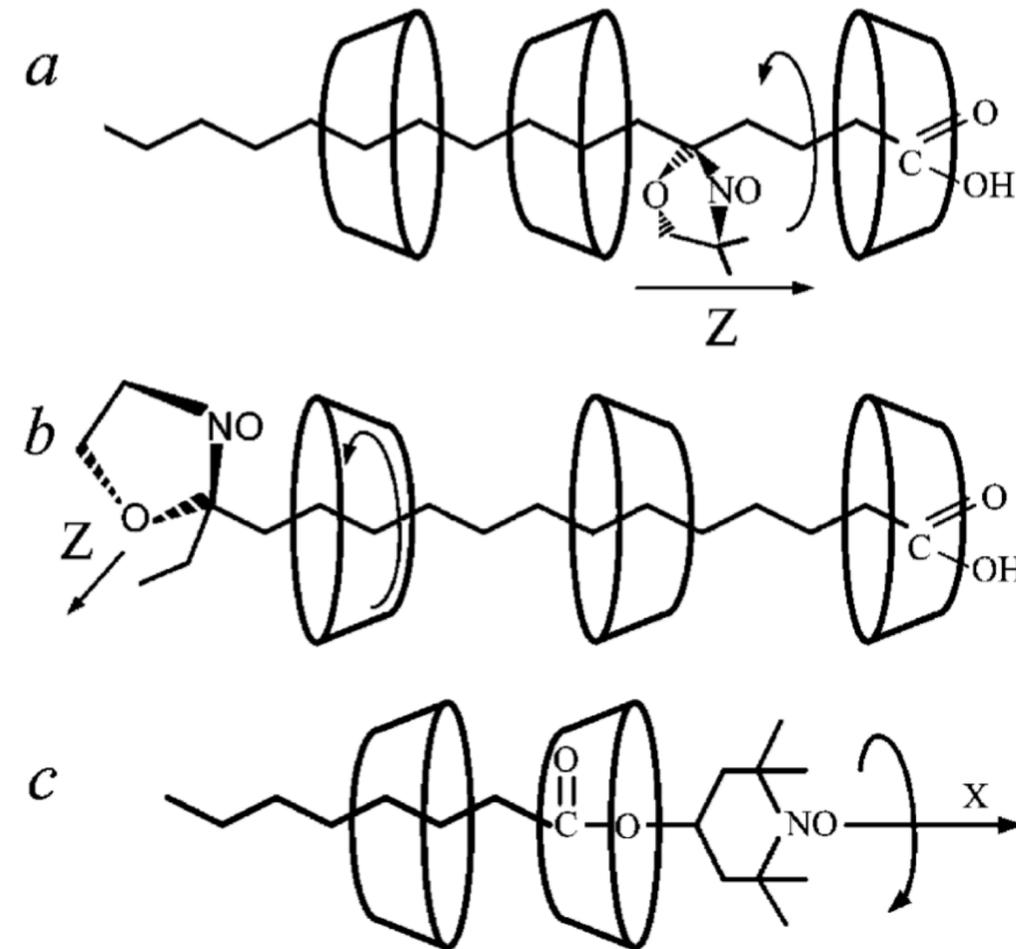
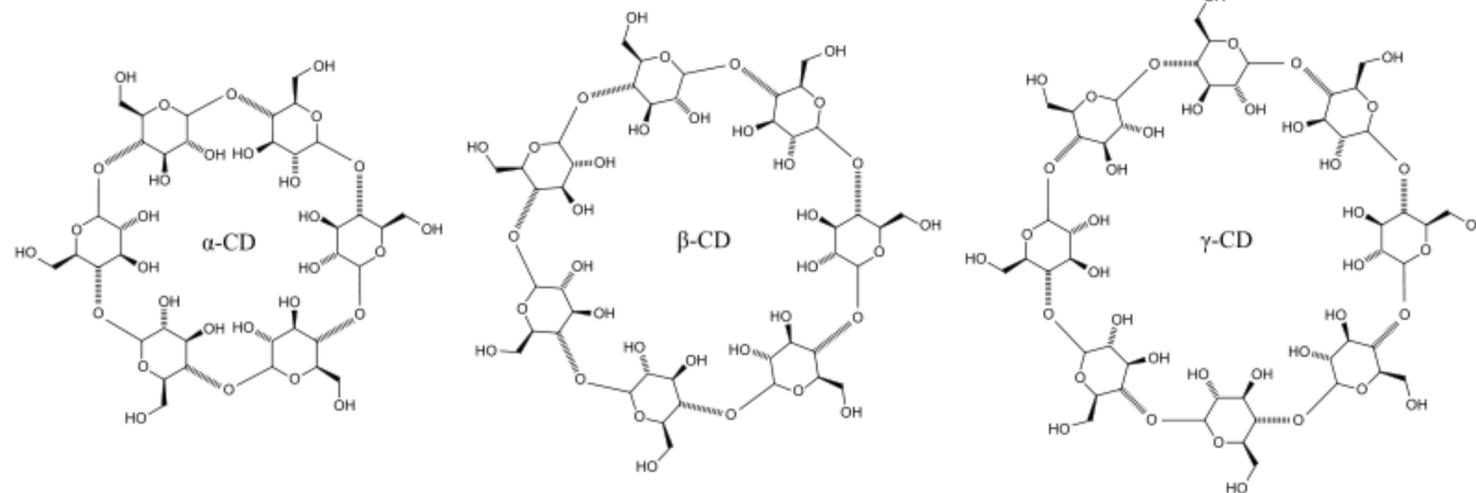


Fig. 7 Schematic drawing of the hypothetical arrangement of cyclodextrin molecules around spin-labeled compound: (a) 5-sasl (b) 16-sasl (c) TEMPOyl-caprylate.

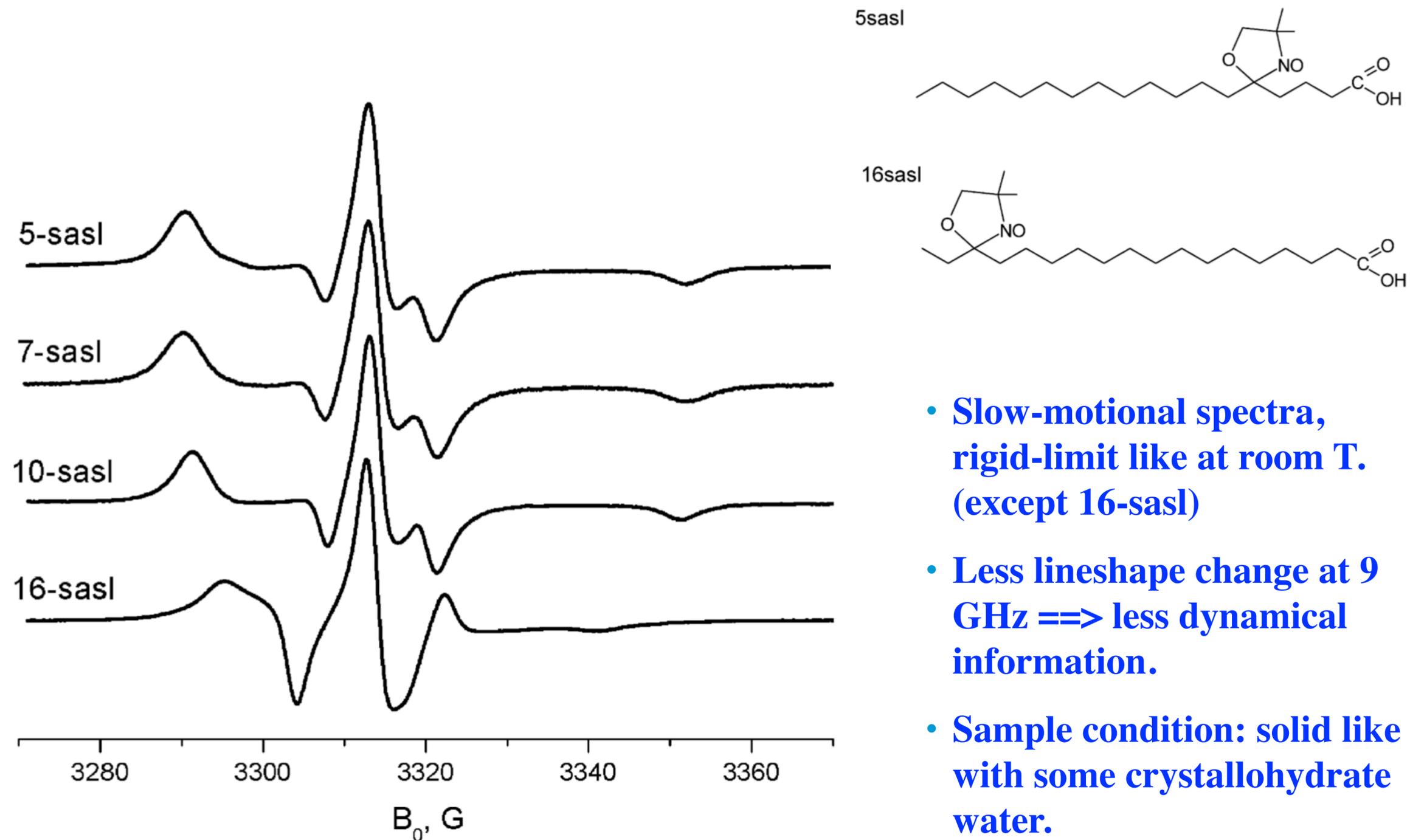


Fig. 4 9 GHz spectra of 5-, 7-, 10- and 16-doxyl stearic acids at 293 K in solid γ -CD.

HFHF ESR provides better orientational resolution.

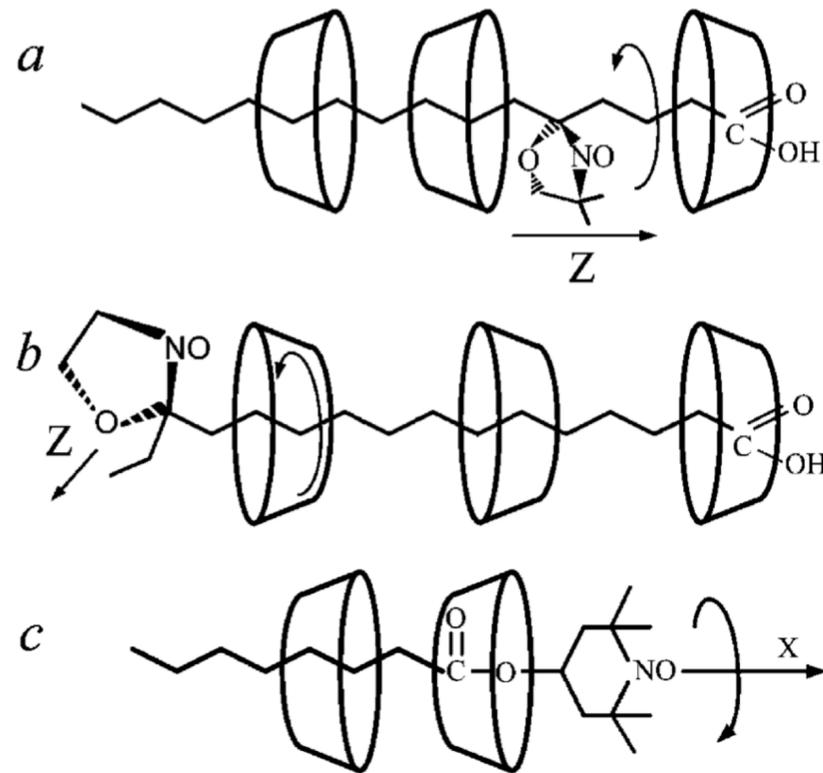


Fig. 7 Schematic drawing of the hypothetical arrangement of cyclodextrin molecules around spin-labeled compound: (a) 5-sasl (b) 16-sasl (c) TEMPOyl-caprylate.

As a result, once motional effects are discernable in the spectrum, one can discern about which axis (or axes) the motion occurs.

At low T it enables the unambiguous determination of the A and the g tensors.

240 GHz, 5-sasl in γ -CD

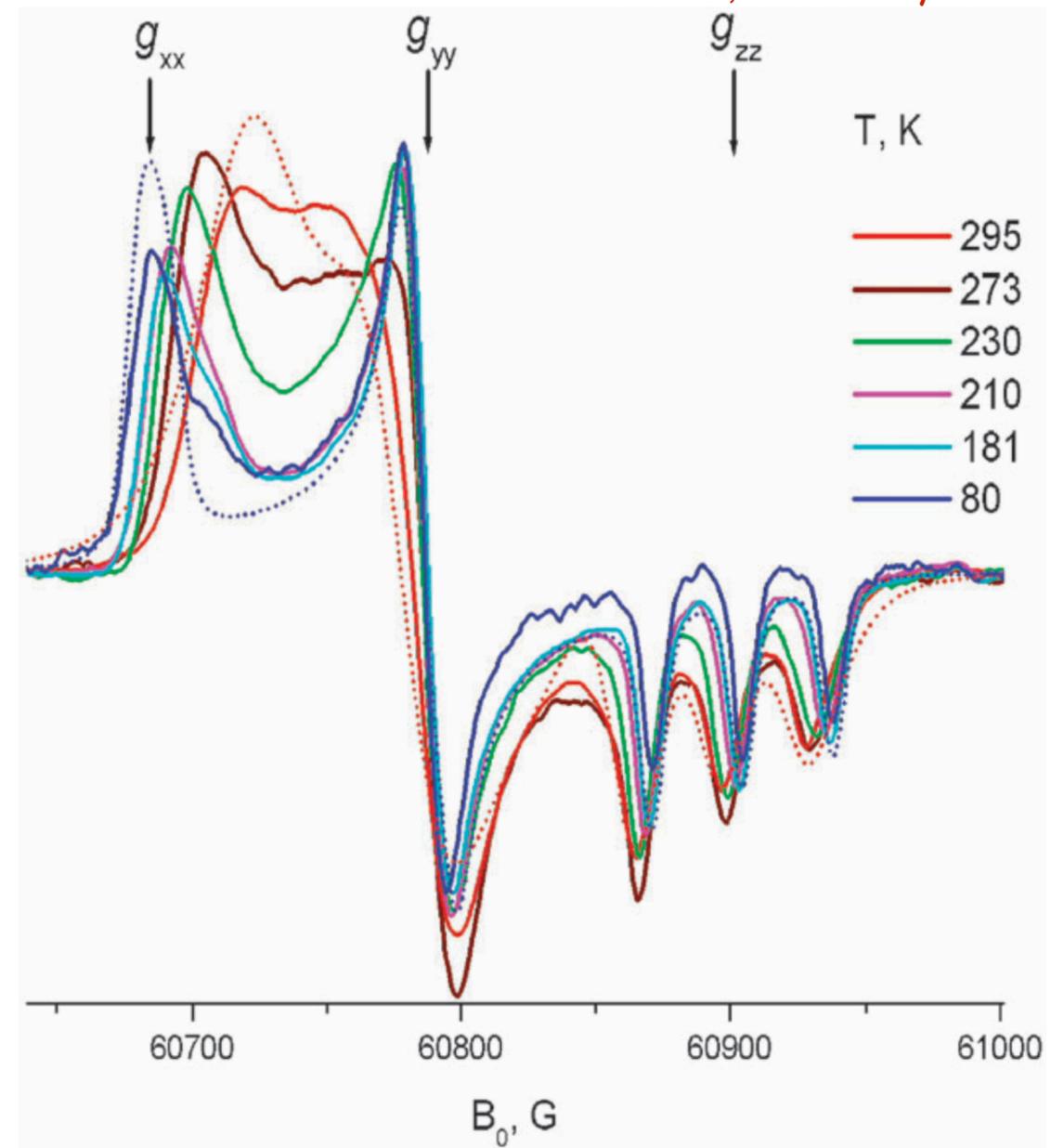


Fig. 5 170 GHz spectra of 5-sasl in solid γ -CD at 80–295 K. Dotted lines show simulations for 80 K (rigid limit) and 295 K.

At high T but in solid state (not tumbling motions), local enhanced rotation improves the spectral resolution; low-field region is blurred by the motion-induced ambiguity effect.

HFHF ESR provides better orientational resolution.

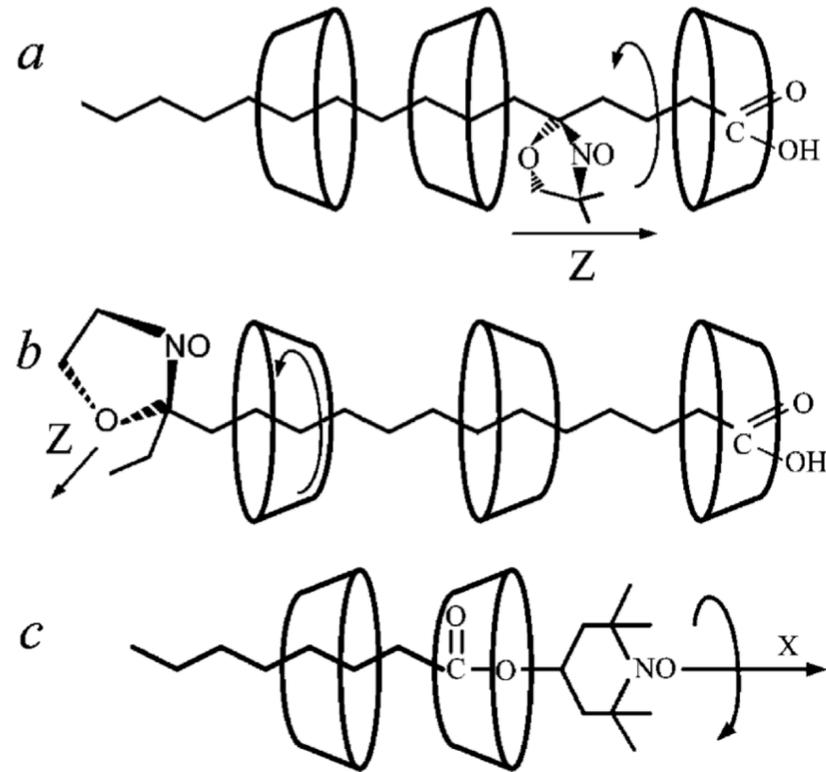
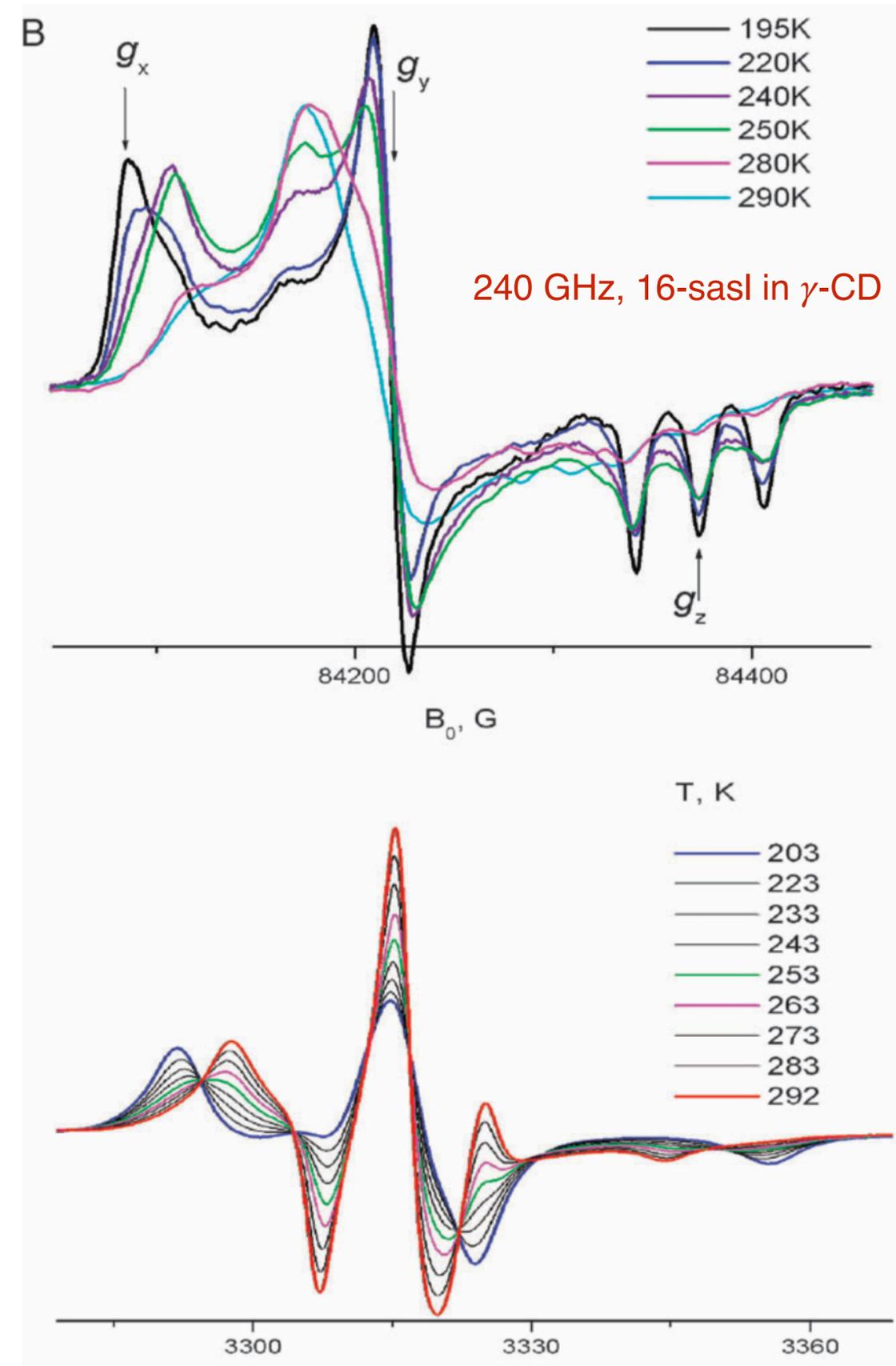
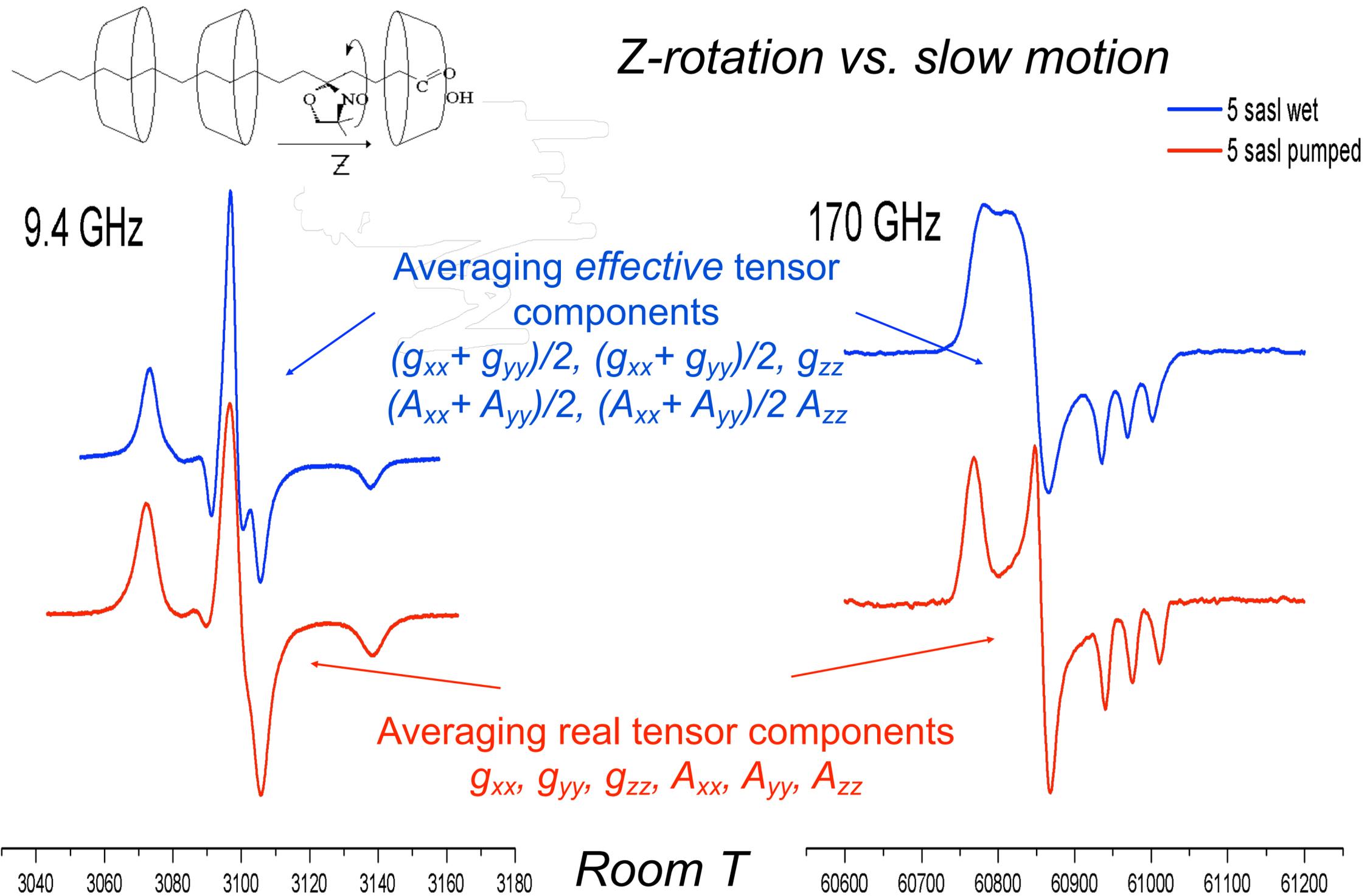


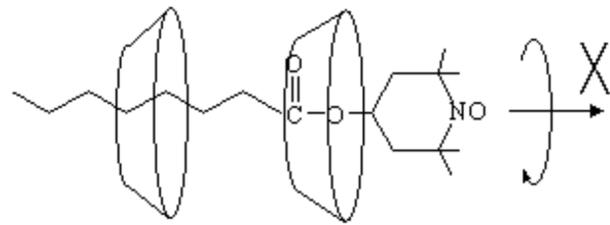
Fig. 7 Schematic drawing of the hypothetical arrangement of cyclodextrin molecules around spin-labeled compound: (a) 5-sasl (b) 16-sasl (c) TEMPOyl-caprylate.

As a result, once motional effects are discernable in the spectrum, one can discern about which axis (or axes) the motion occurs.





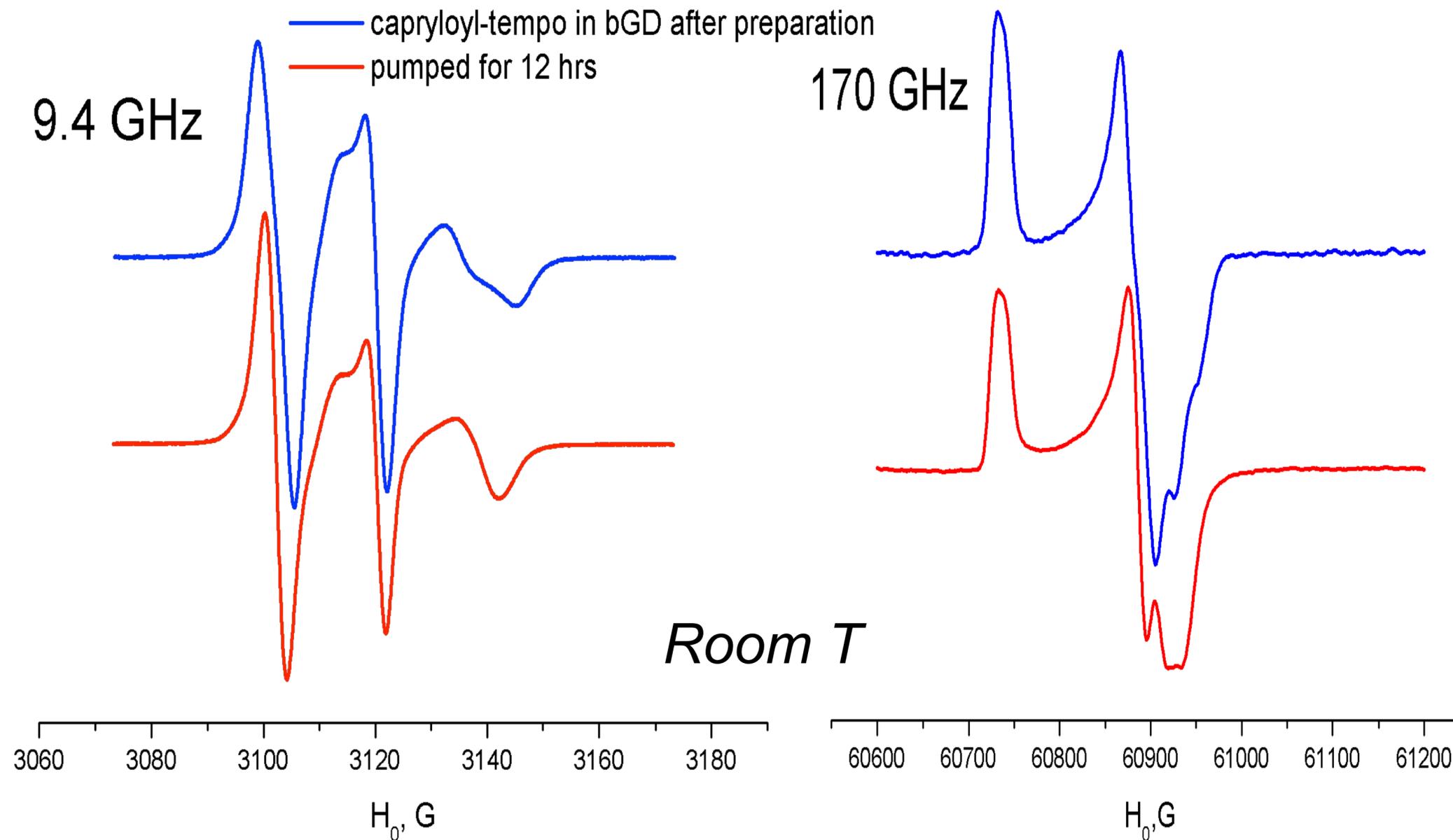
HFHF ESR allowed us to demonstrate Z- and X-axial rotation and determine the relevant rotational diffusion constants and potential barriers. Such determination at 9 GHz is either impossible (Z-rotation) or inaccurate (X-rotation).



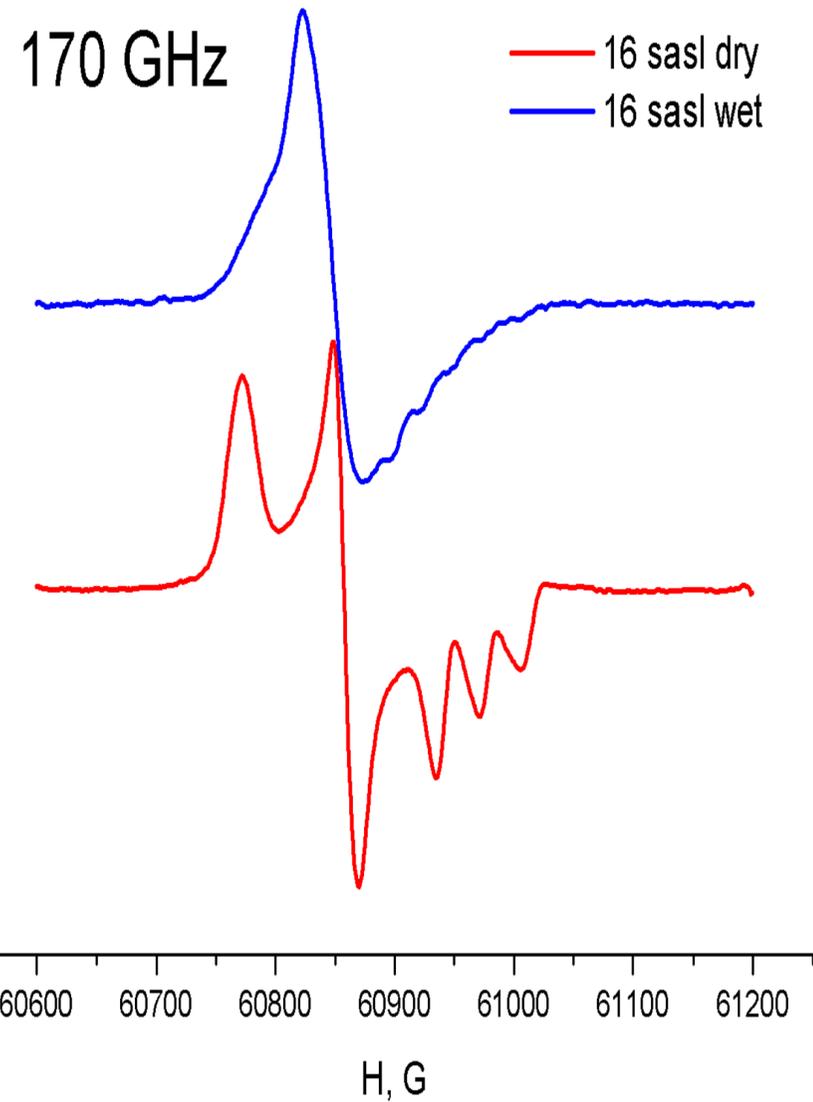
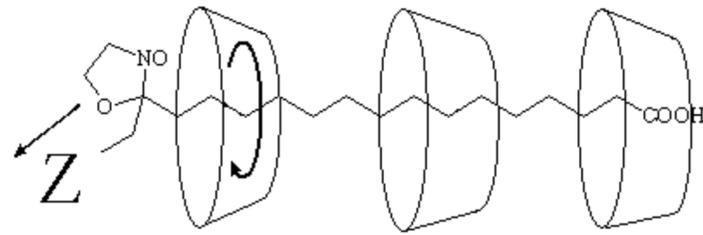
X-rotation

Averaging *effective* tensor components

$$g_{xx}, (g_{yy} + g_{zz})/2, (g_{yy} + g_{zz})/2, \\ A_{xx}, (A_{yy} + A_{zz})/2, (A_{yy} + A_{zz})/2$$



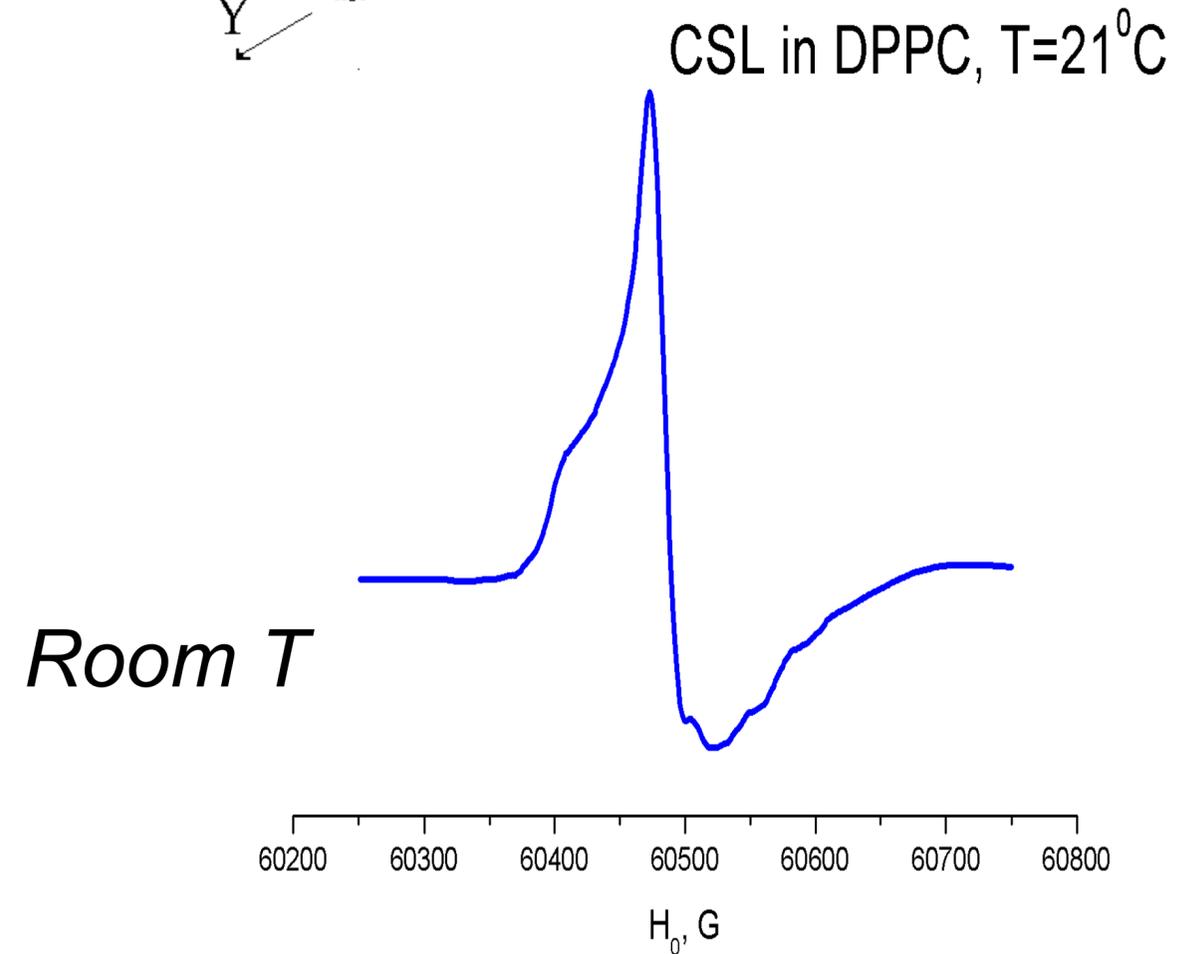
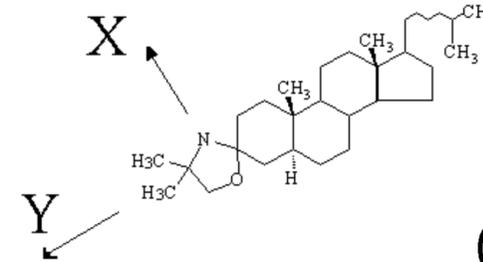
Diffusion tilt angle



Y-rotation

Averaging effective tensor components

$$(g_{xx} + g_{zz})/2, g_{yy}, (g_{xx} + g_{zz})/2, (A_{xx} + A_{zz})/2, A_{yy}, (A_{xx} + A_{zz})/2$$



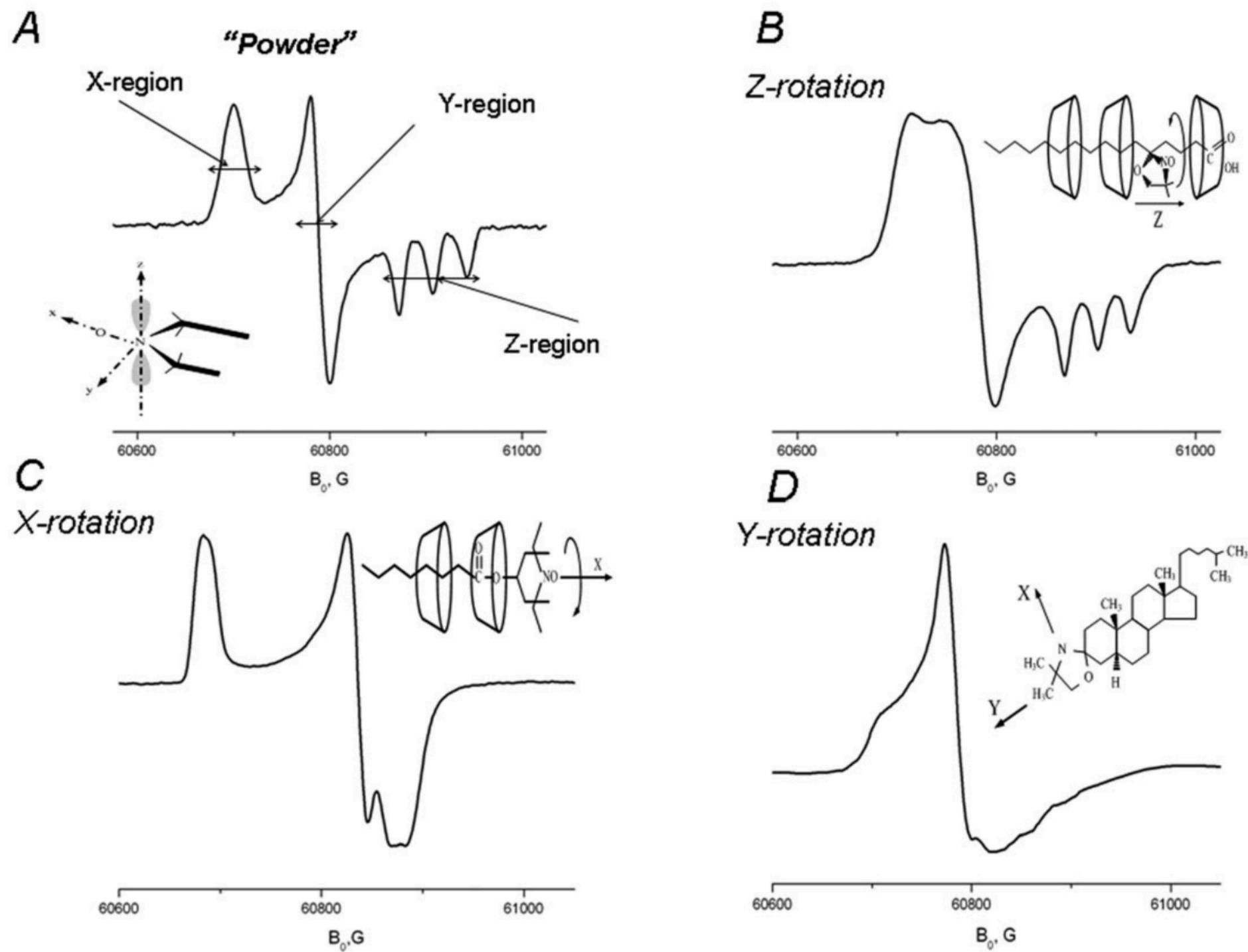


Fig. 3 170 GHz spectra of nitroxide radicals corresponding to different modes of molecular motion: (A) 5-sasl in γ -CD with crystallohydrate water removed by overnight evacuation at 293 K: rigid limit spectrum. (B) 5-sasl in γ -CD crystallohydrate at 292 K. (C) TEMPOyl-caprylate in β -CD at 293 K. (D) CSL spin label in the DPPC membrane at 295 K. Insert A shows the principal magnetic axes of the nitroxide group. Inserts B–D show the corresponding mode of molecular motion.

X-rotation

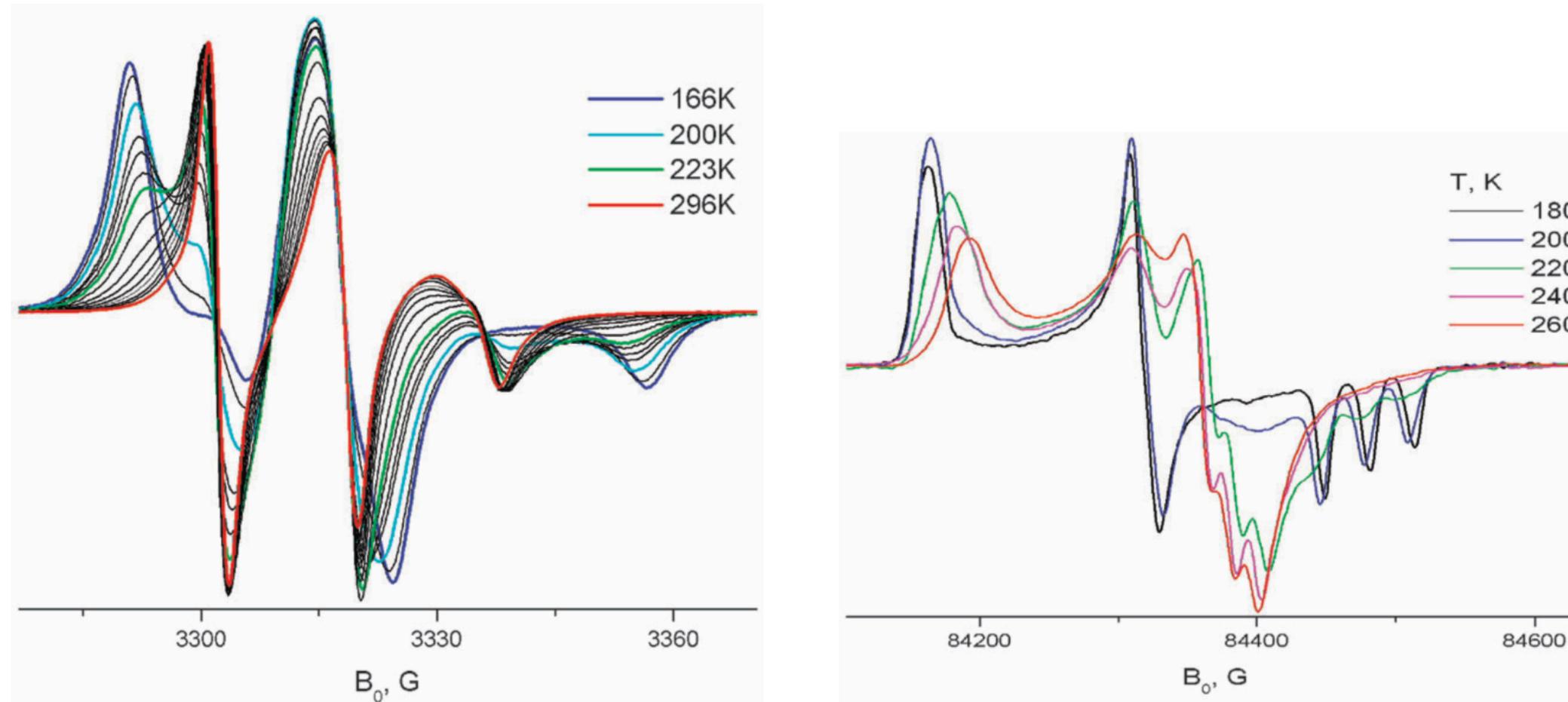
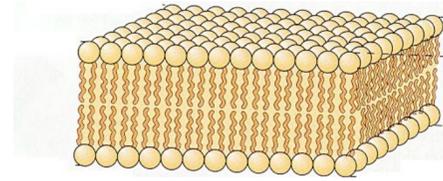


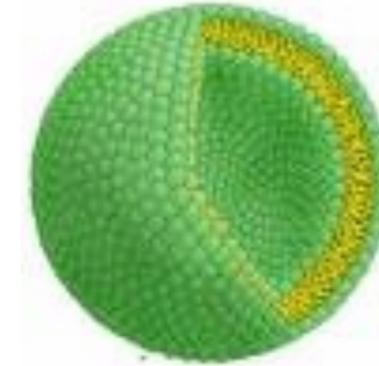
Fig. 15 TEMPOyl caprylate in γ -CD. Temperature dependence at 240 GHz (upper image) and 9 GHz (lower image).

Dynamics vs. Dynamics + Orientational resolution

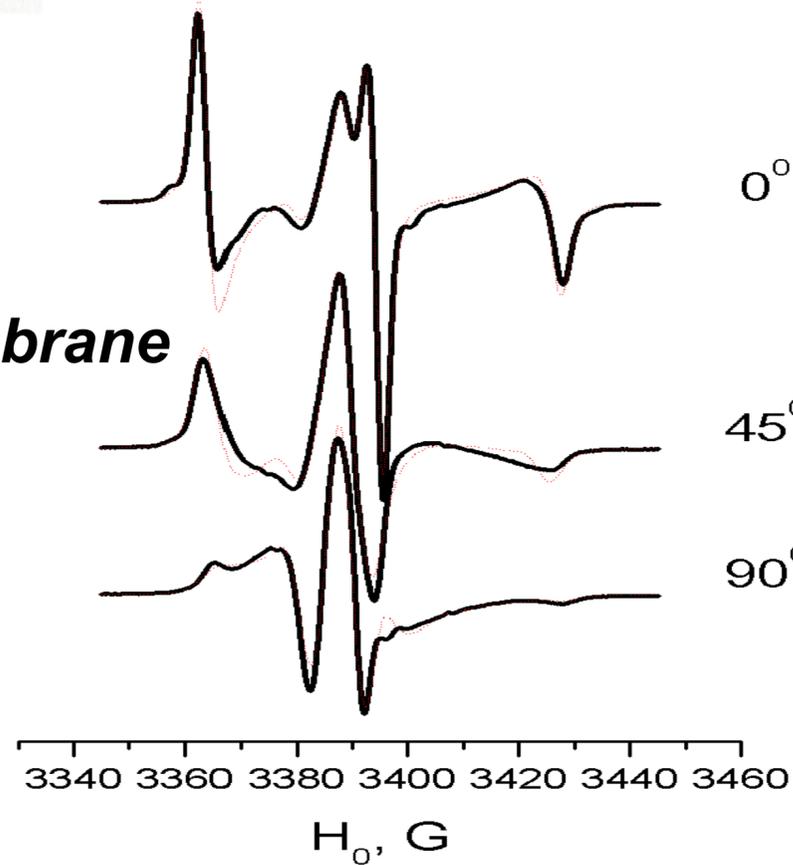
ESR on aligned membranes



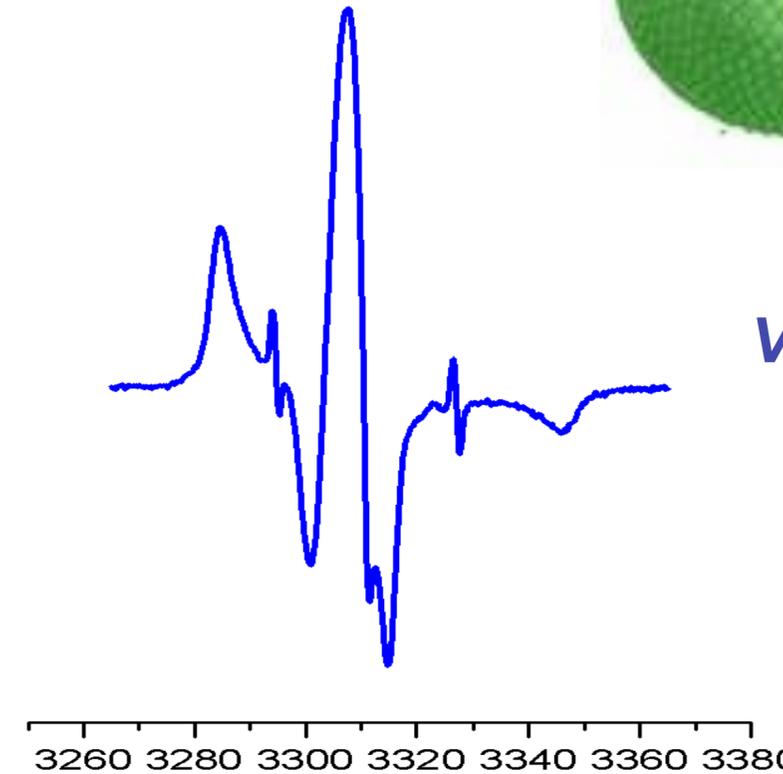
Spin-labeled gramicidin A in DPPC, 22° C



Aligned membrane



Vesicles

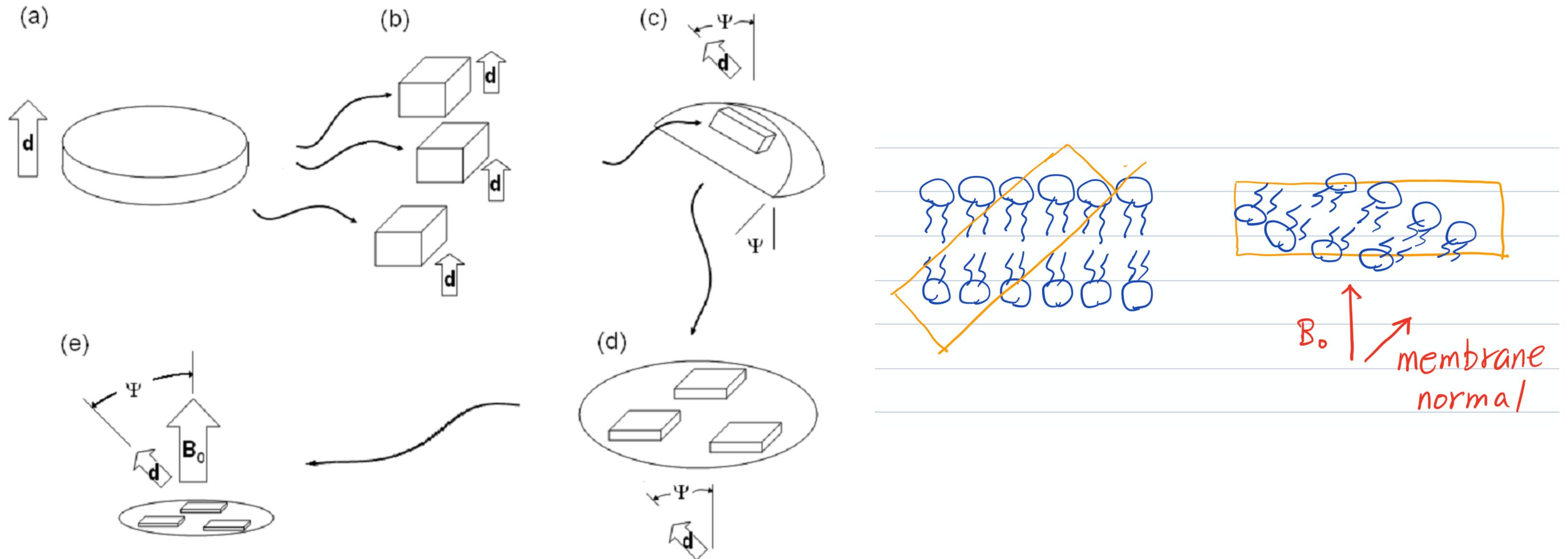


Simulation of angular dependent spectra is much freer of ambiguity, compared to vesicles

Application of aligned membranes allows extracting information on relative orientation of diffusion and magnetic axes, which can not be obtained from vesicles

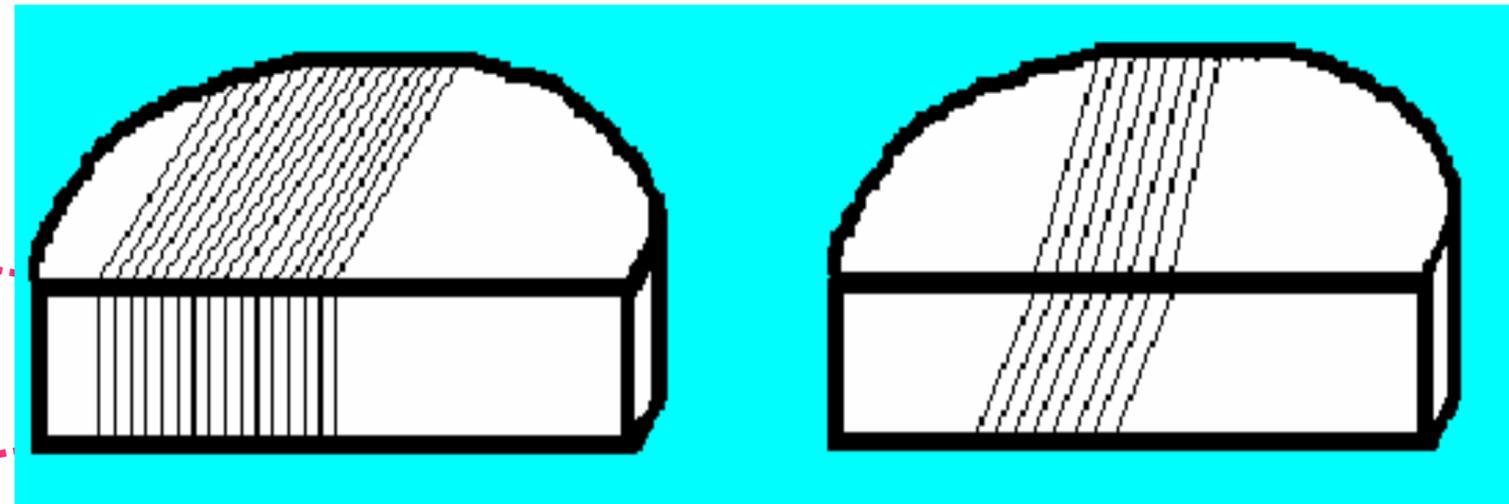
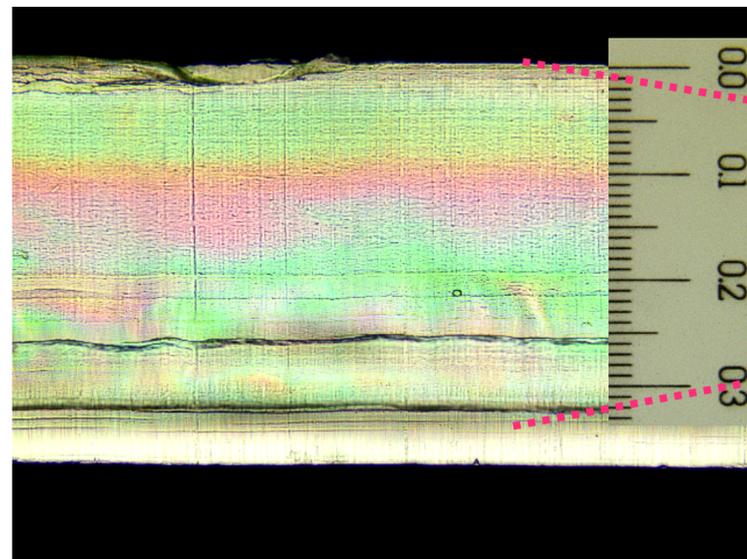
Microtome technique on aligned membranes

High frequency ESR requires very thin (<100 nm) flat samples with B_0 directed perpendicular to the sample in order to minimize dielectric losses



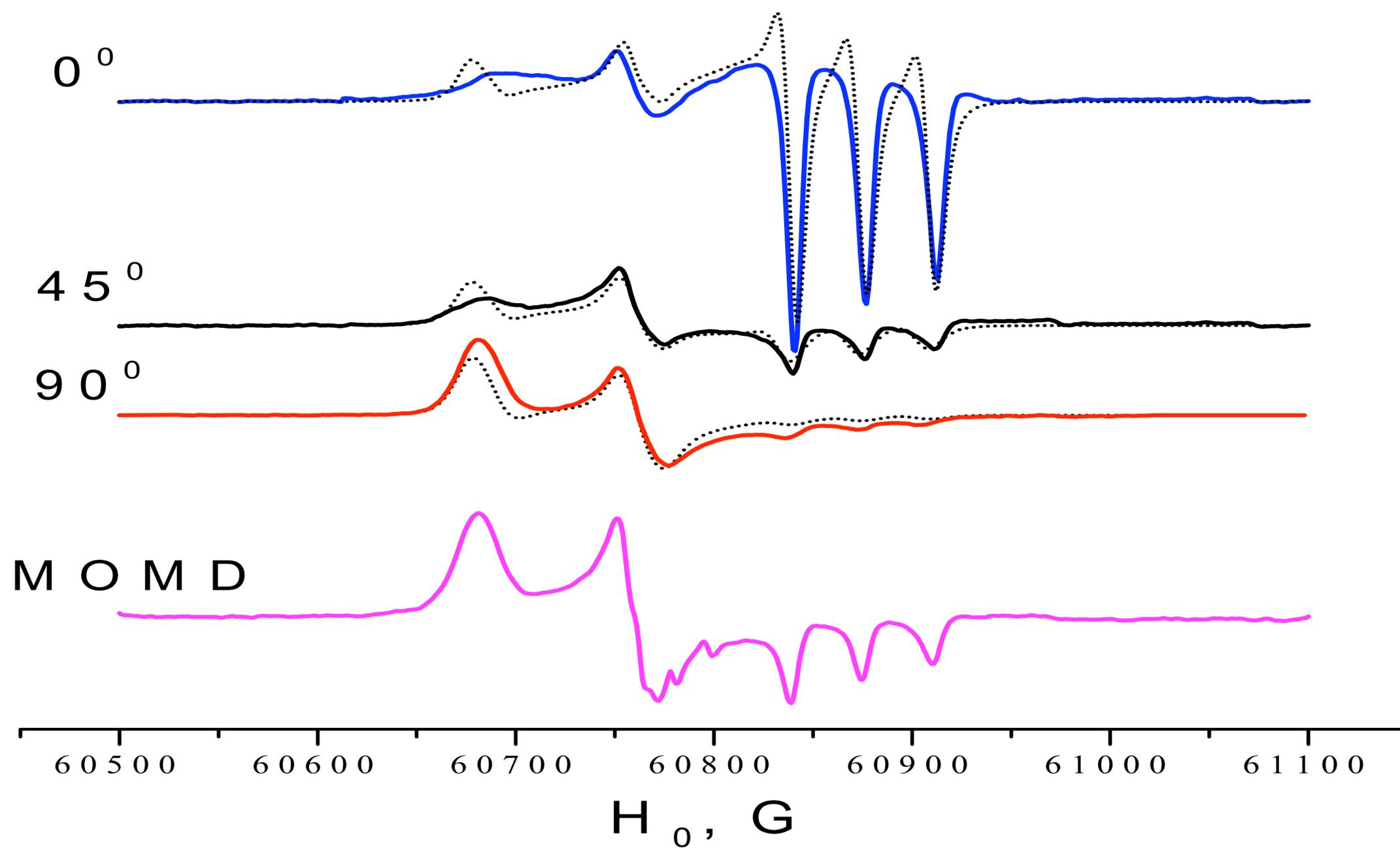
*High-field ESR on aligned membranes
in different orientation of the membrane normal relative to B_0*

ISDU aligned DPPC membrane sample is 300 micrometer thick



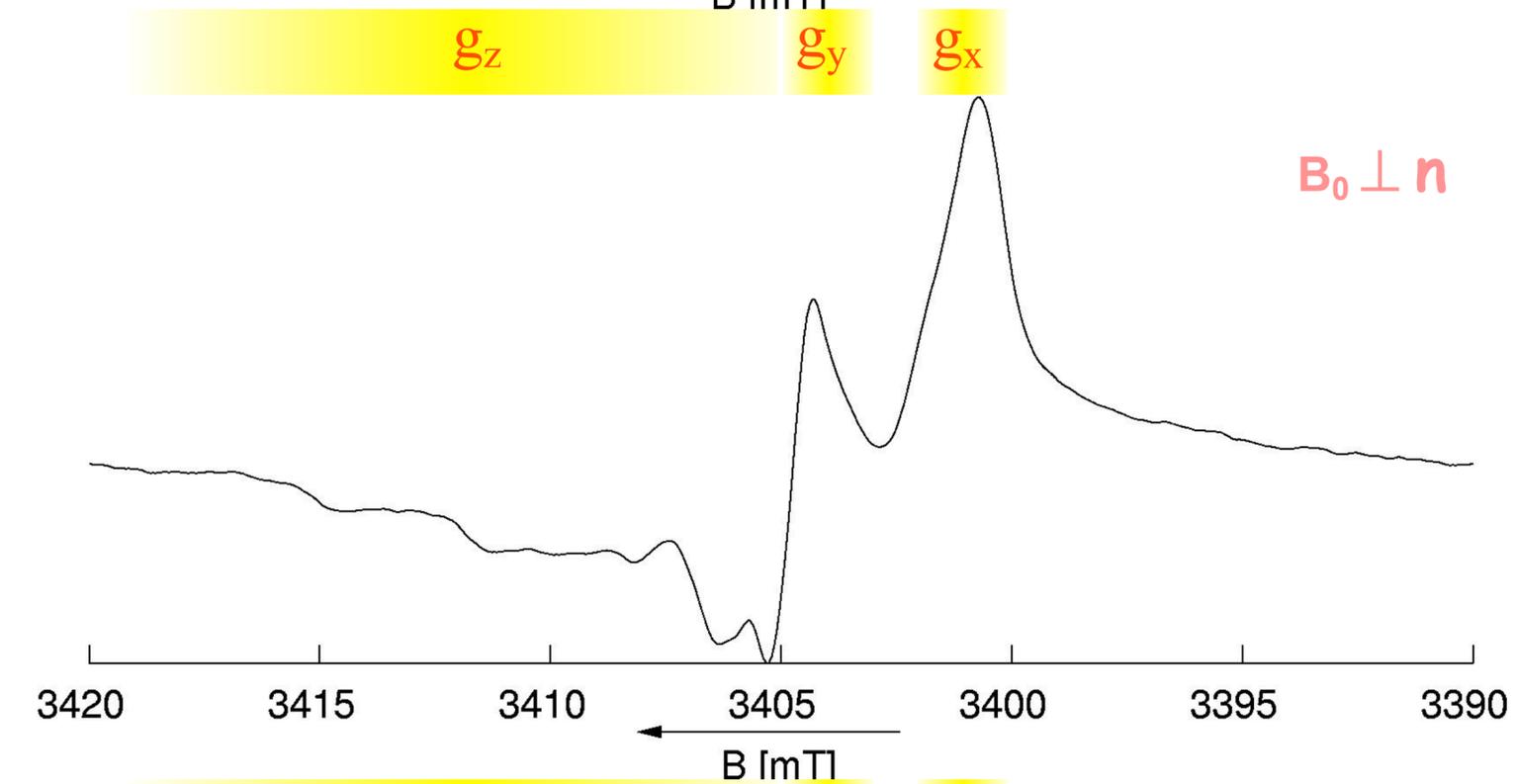
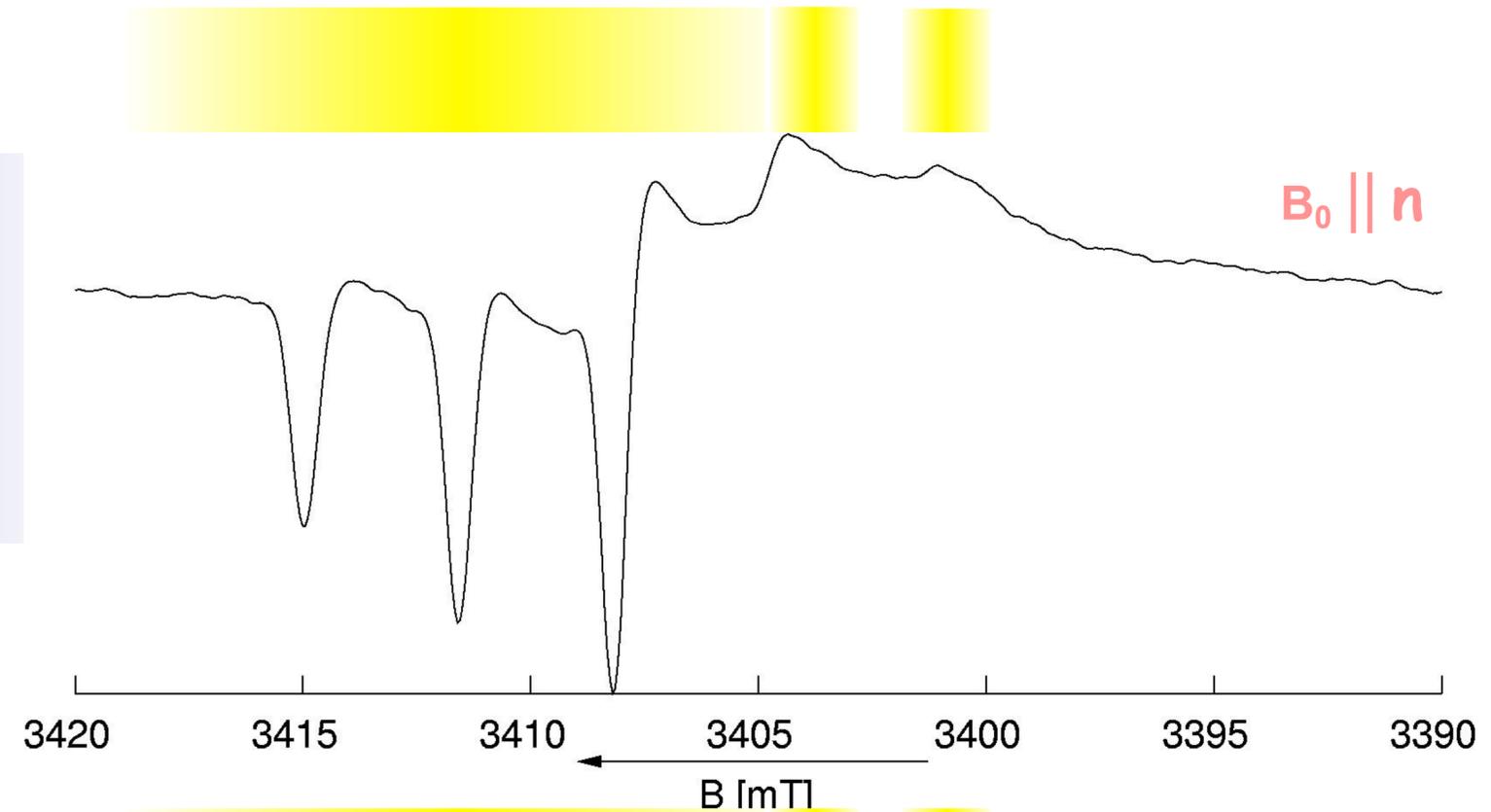
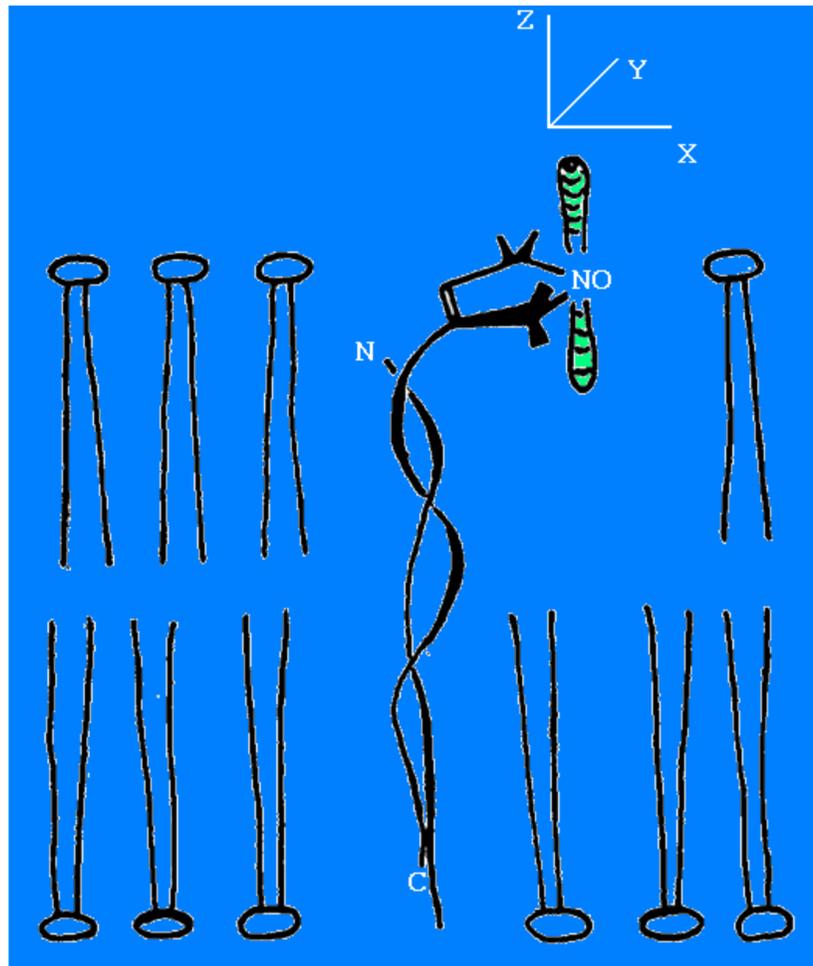
80micrometer slices cut of the sample
are utilized in high-field ESR

Spin labeled Gramicidin A in DPPC at 170 GHz



Spin-labeled Gramicidin A in Oriented Membrane (DPPC)

- Slow motional nitroxyl spectrum at 7°C.
- Orientation selection at 95 GHz (3.2 mm)
- g_z parallel to membrane normal (z-ordered)



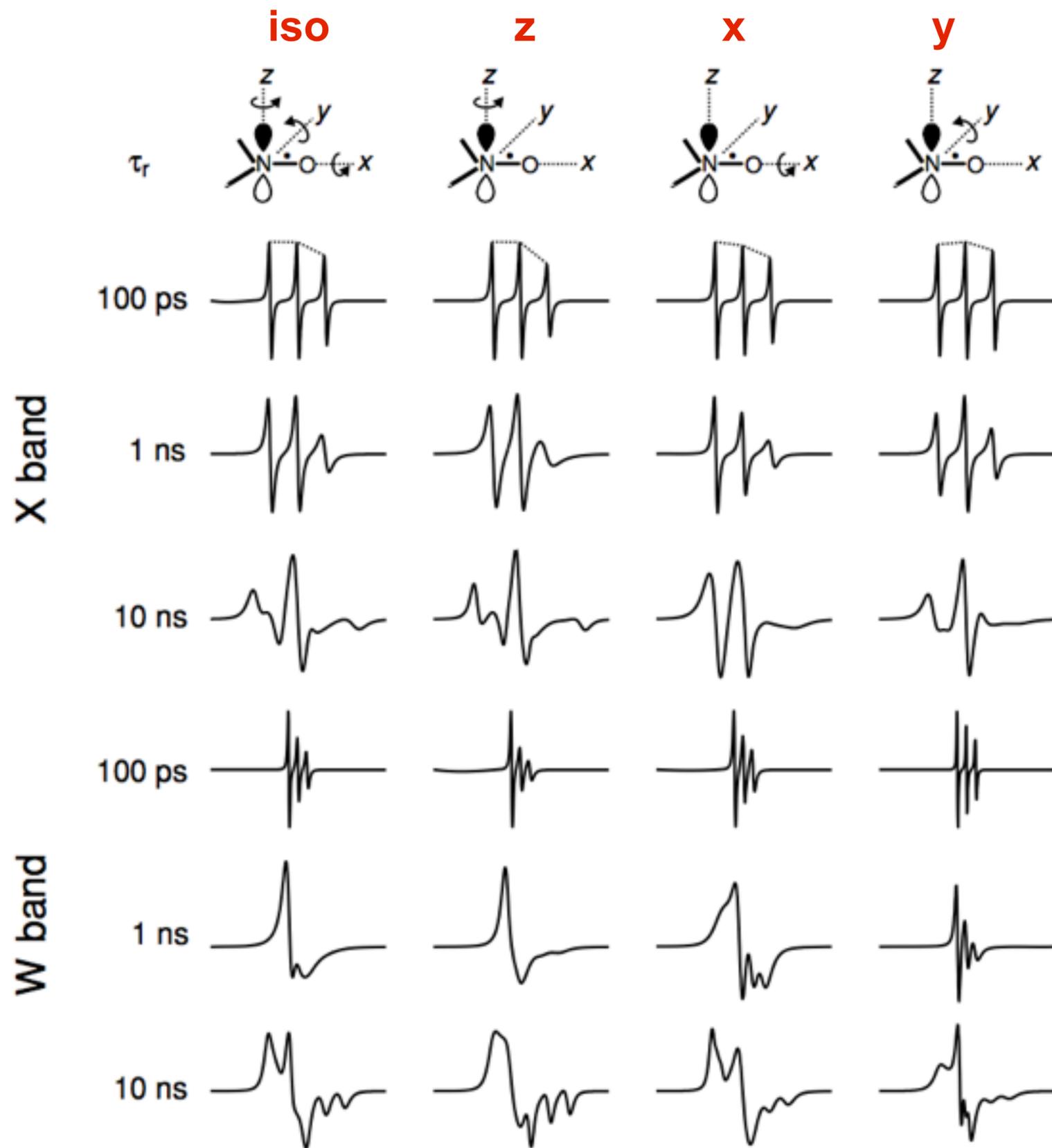
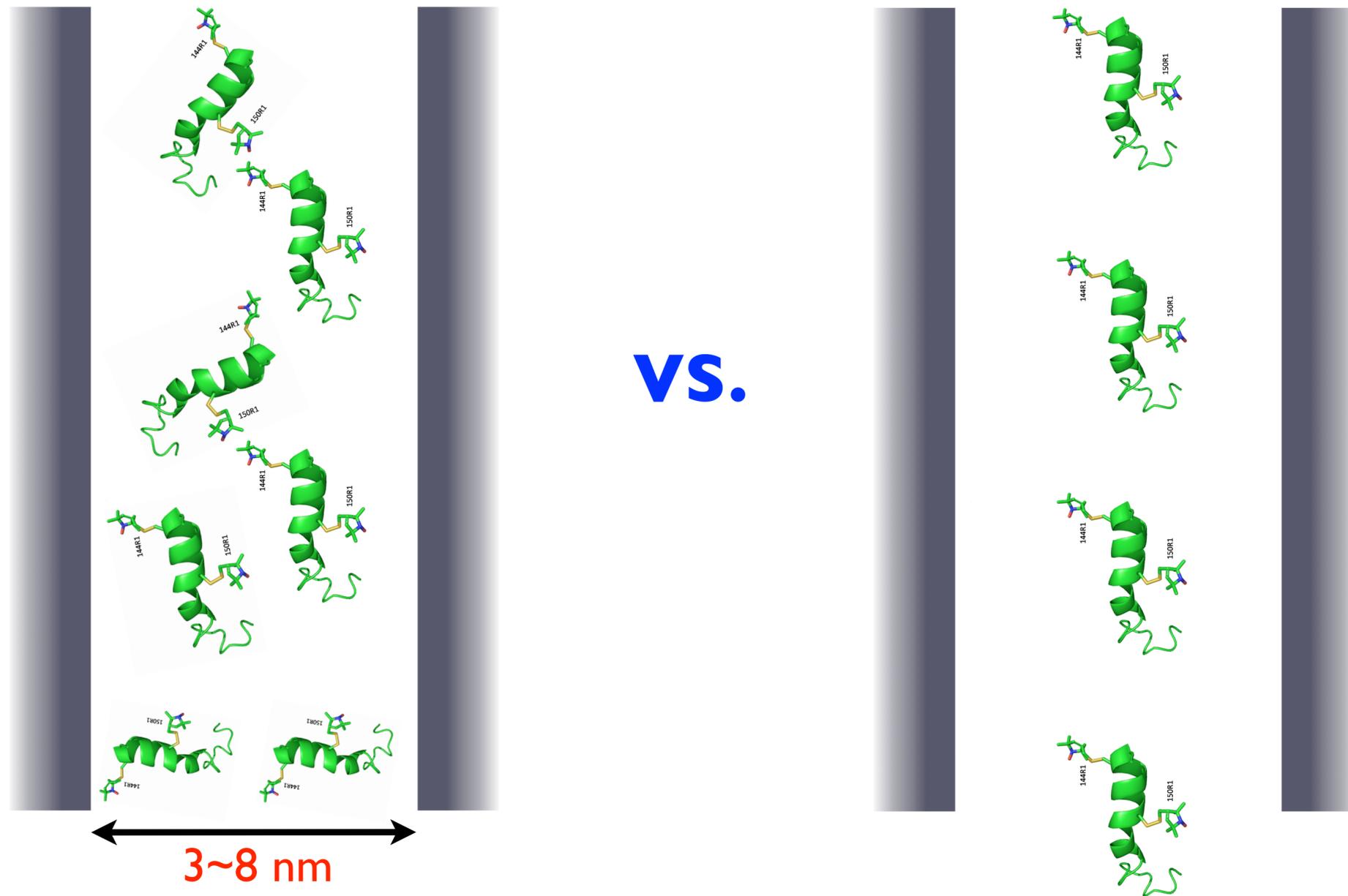


Fig. 1. Dependency of nitroxide spin probe spectra on rotational correlation time, preferential rotation axis, and EPR frequency. Panels from left to right correspond to isotropic rotational diffusion, and preferential rotation about the z , x , and y axis, respectively. Rotational diffusion about the preferred axis is assumed to be ten times faster than about other axes. X-band spectra are centered at 334.8 mT and are 10 mT wide, W-band spectra are centered at 3355 mT and are 30 mT wide. Simulations were performed with the Schneider/Freed suite of programs [21].

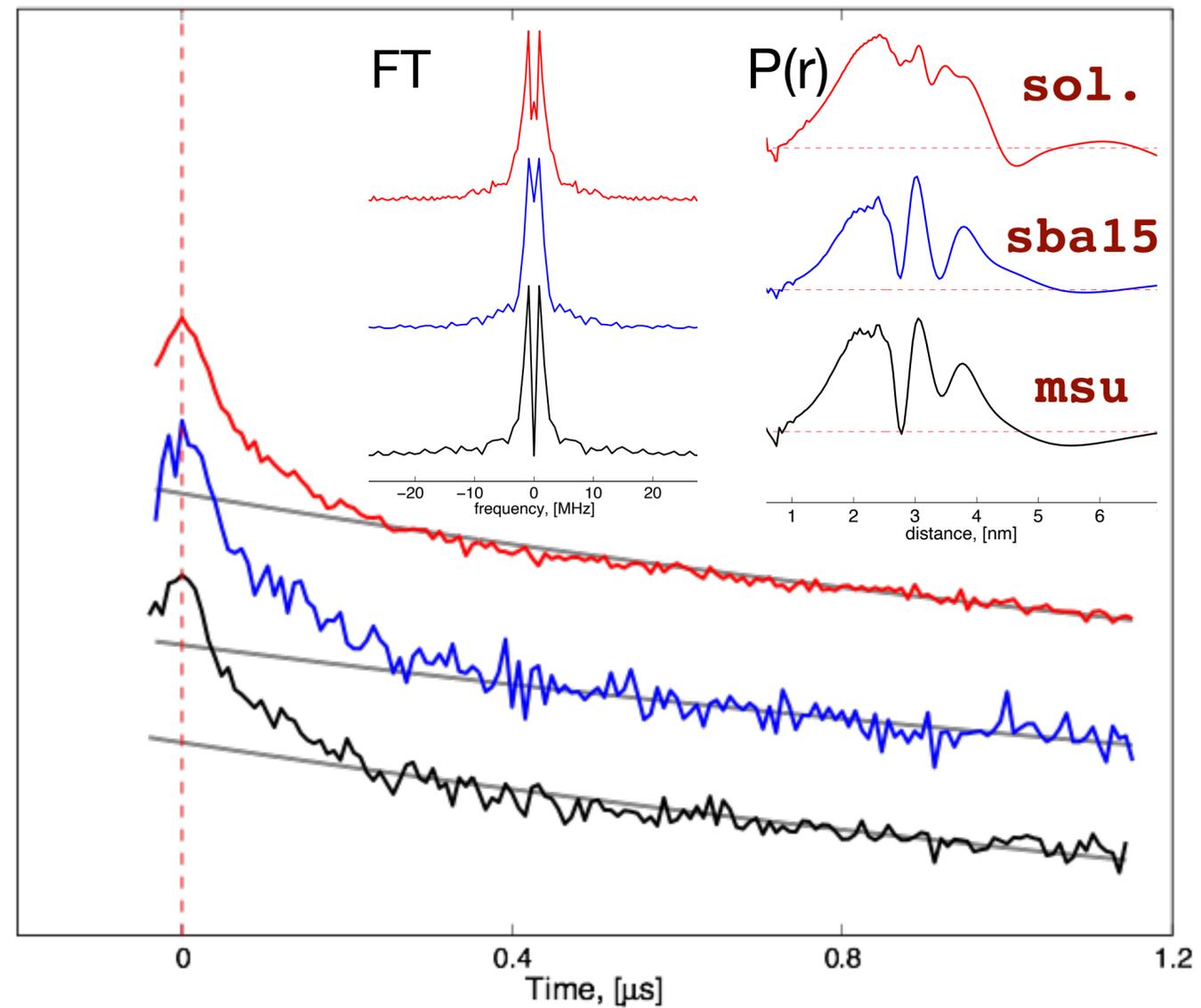
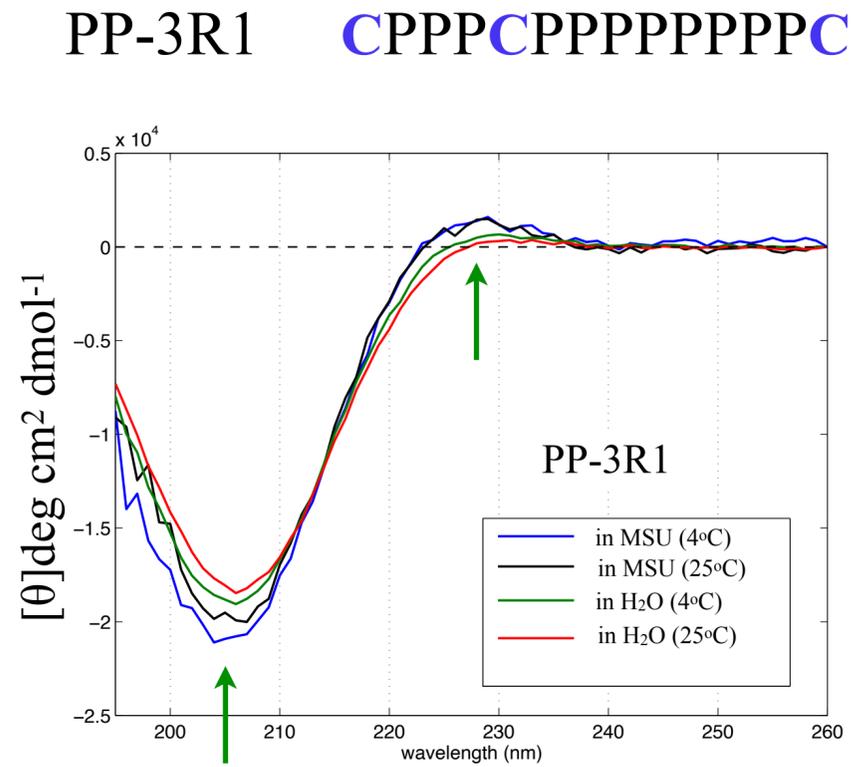
Lineshape depends on
 1) diffusional rates
 (dynamics) 2) anisotropic
 rotations

Nano-confinement Enhances Anisotropic Rotational Dynamics ?

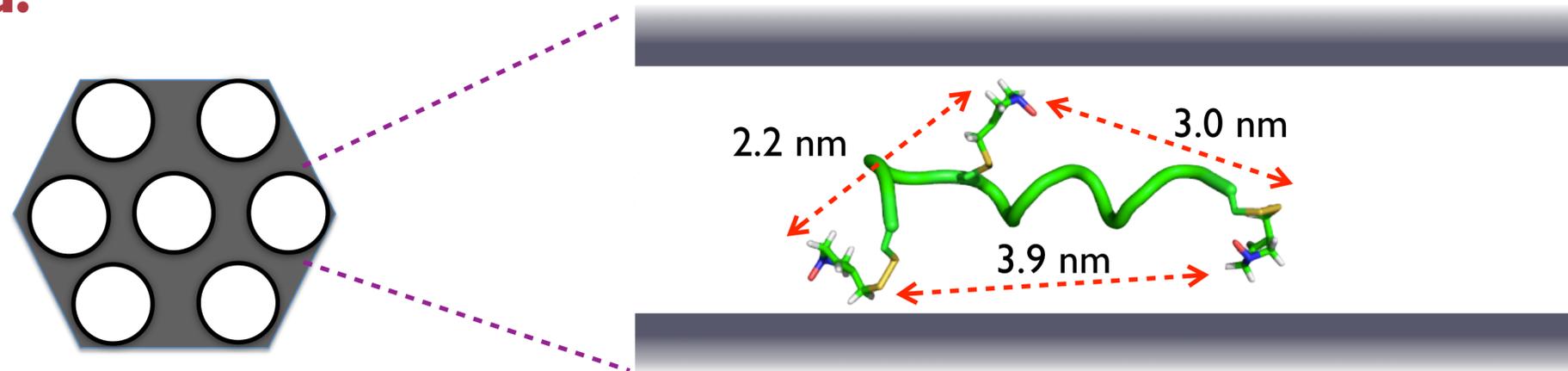


Is ESR useful for probing dynamics of a nanodevice confined deeply within nanostructures?

Peptide Retains its Structure in Nanochannels

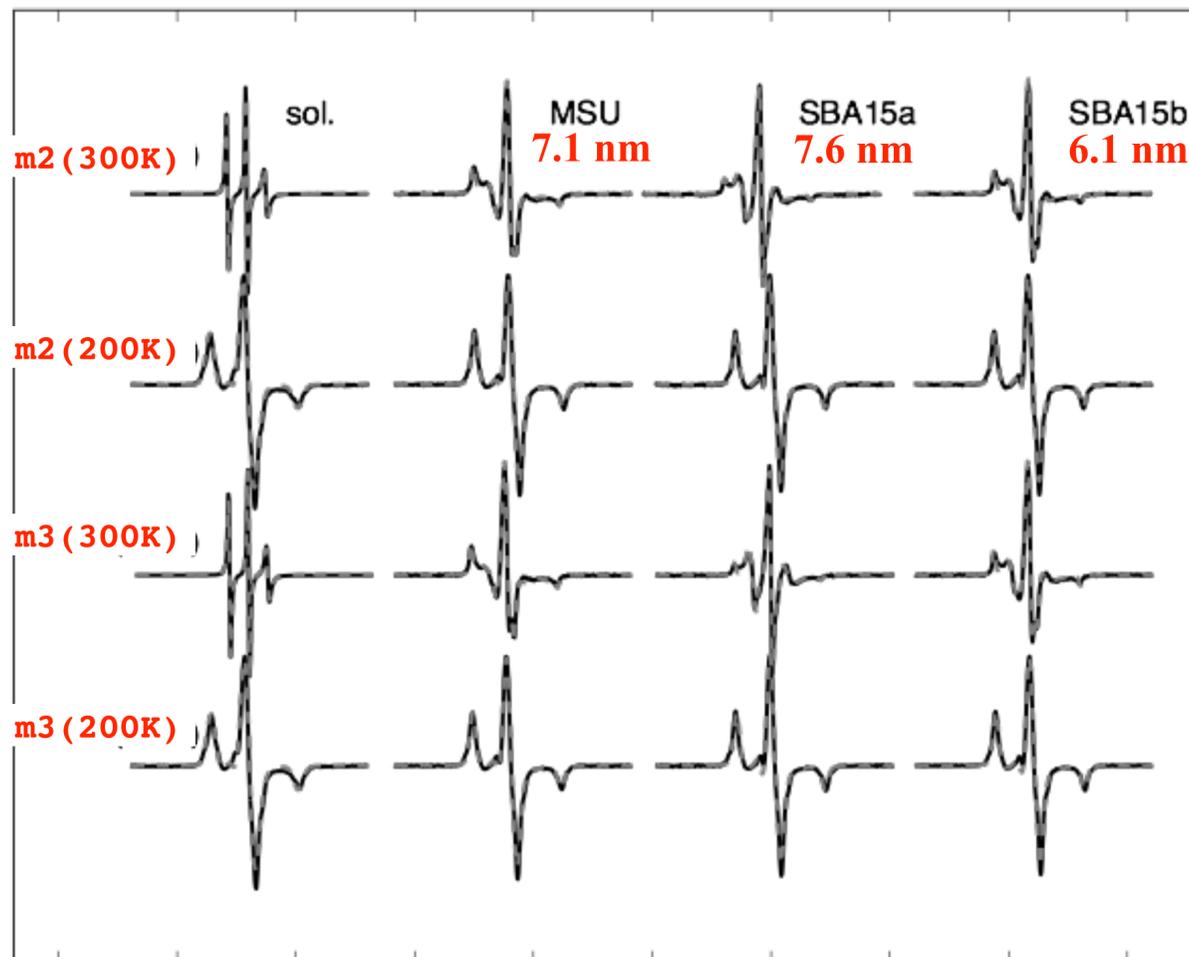


- CD shows PII structure is unchanged.
- ESR demonstrates the peptide structure is approximately the same in all conditions studies.
- **P(r) accuracy improved.**

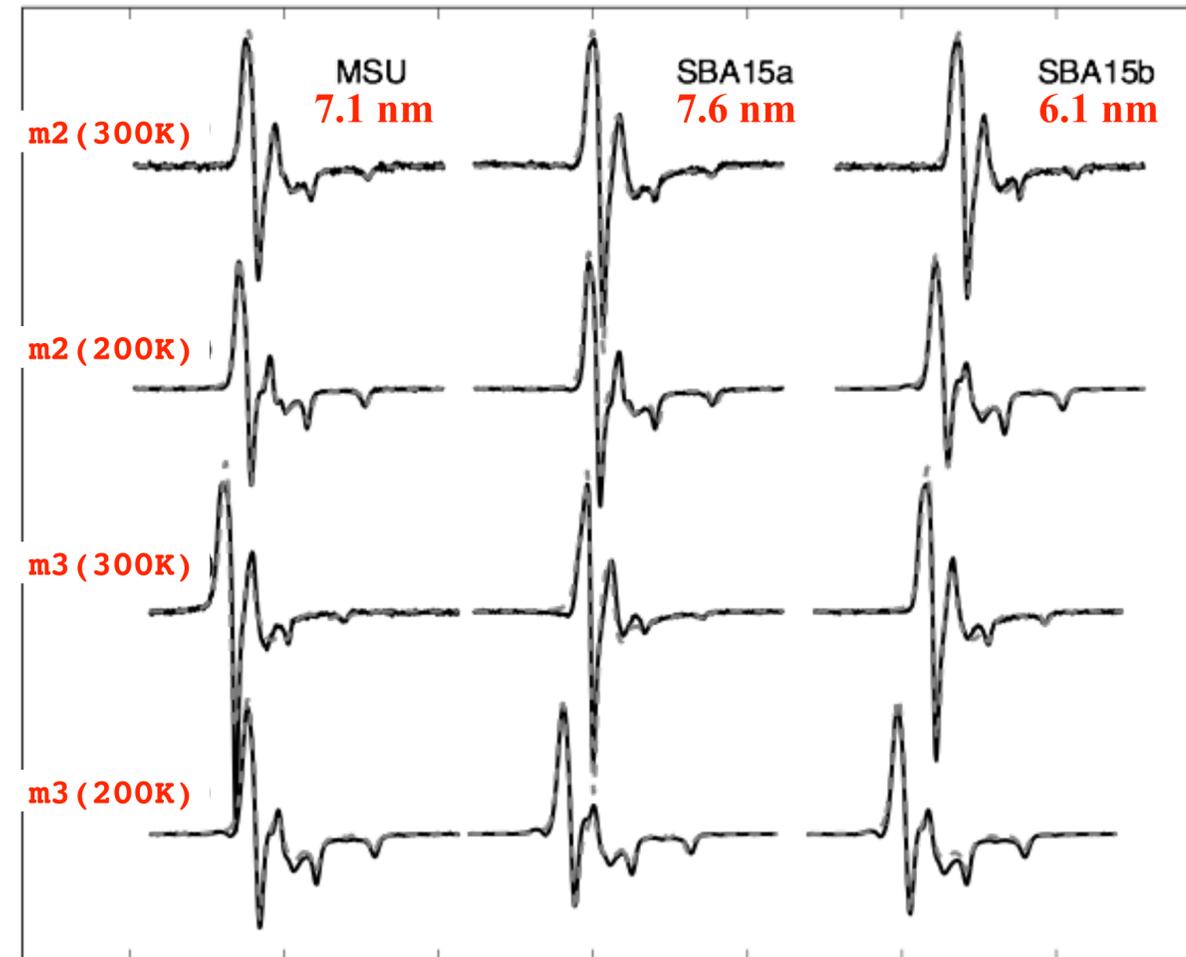


Theoretical Fits to Multifrequency Spectra

X-band (9 GHz)



Q-band (35 GHz)

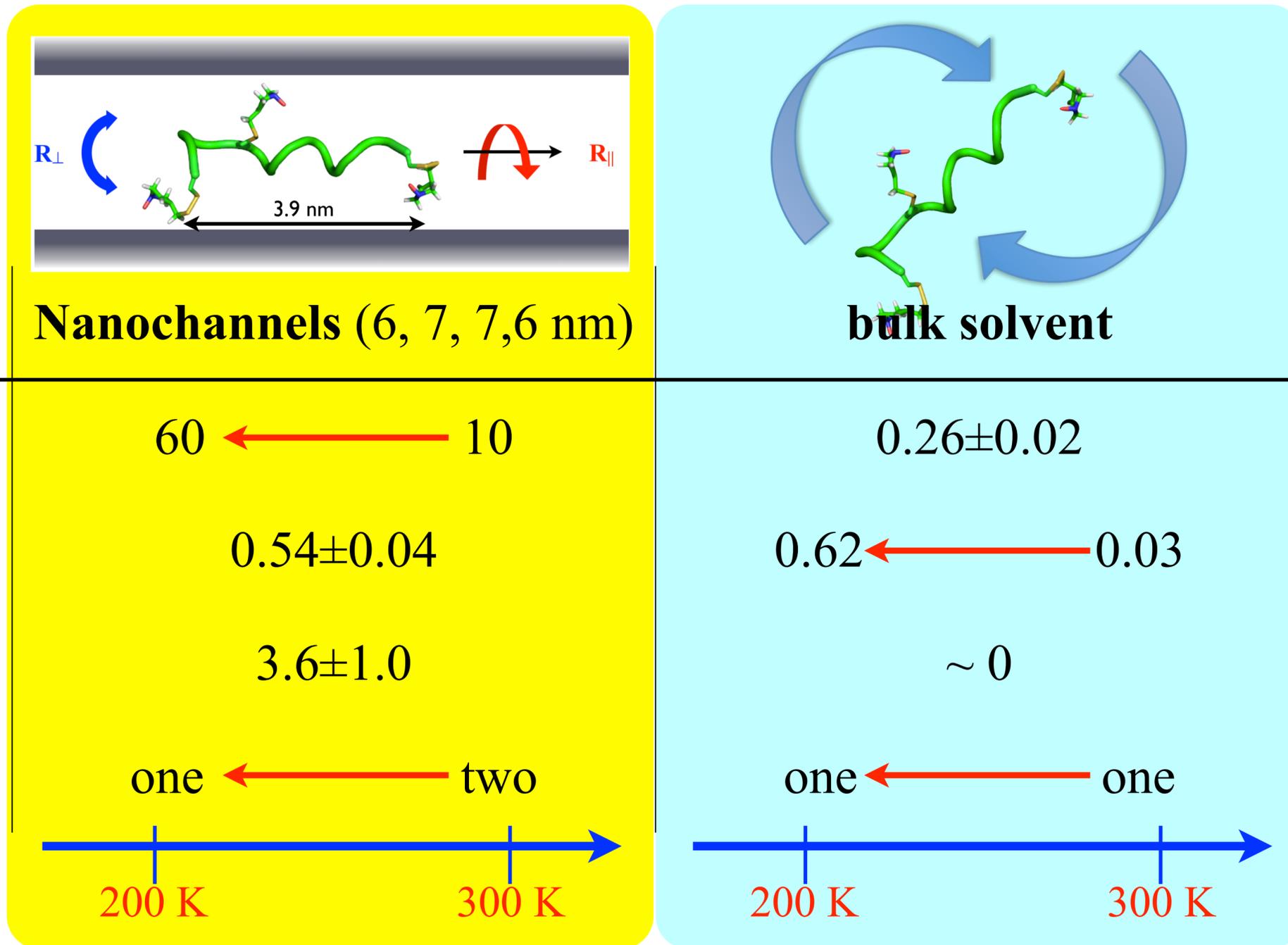


PP-m2 PPPPPPCPPPPPP

PP-m3 PPPPPPPPCPPPP

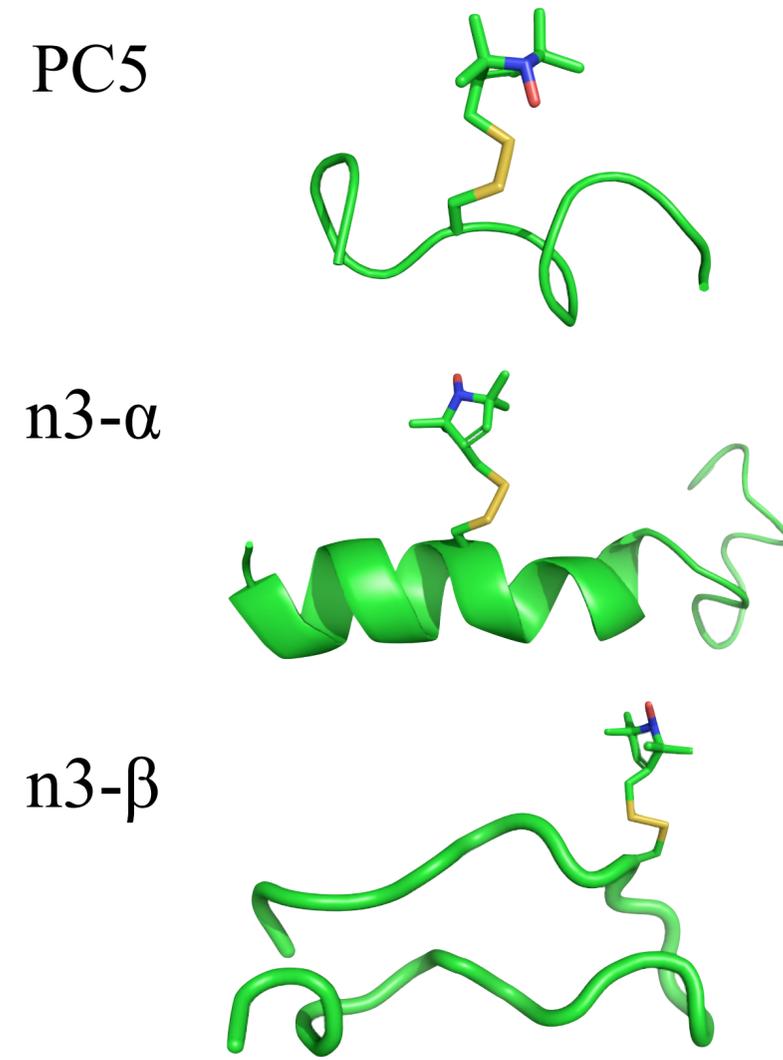
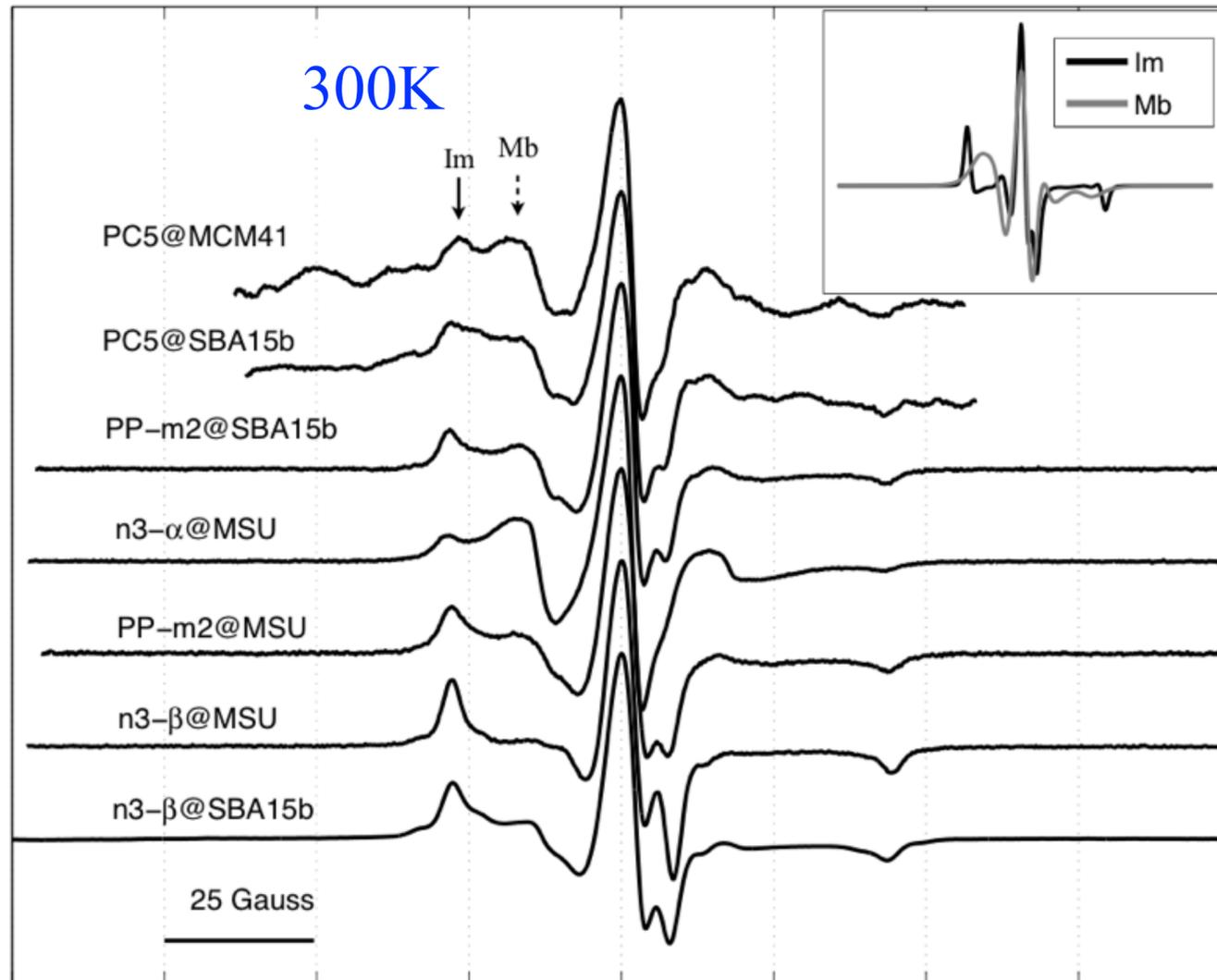
T = 300 K		R_{\perp} (s^{-1})	R_{\parallel} (s^{-1})	R_{\parallel}/R_{\perp}	S_0	$\Delta^{(0)a}$	$[Im]^b$
sol.		2.35×10^8	6.54×10^7	0.28	0.03	0.5	100% (100%)
MSU	Im	1.27×10^6	1.24×10^7	9.76	0.56	2.7	48% (38%)
	Mb	3.82×10^7	3.82×10^7	1.00	0.15	2.1	
SBA15a	Im	1.27×10^6	3.79×10^7	11.22	0.54	3.0	47% (32%)
	Mb	6.39×10^7	6.39×10^7	1.00	0.16	1.7	
SBA15b	Im	1.06×10^6	1.03×10^7	9.72	0.48	2.4	45% (46%)
	Mb	4.39×10^7	4.38×10^7	0.99	0.14	1.4	
T = 200 K		R_{\perp} (s^{-1})	R_{\parallel} (s^{-1})	R_{\parallel}/R_{\perp}	S_0	$\Delta^{(0)d}$	$\Delta^{(2)e}$
sol.		6.81×10^5	1.71×10^5	0.25	0.62	7.5 (7.4)	0 (0)
MSU		$(0.13 \pm 0.03) \times 10^6$	$(8.15 \pm 0.50) \times 10^6$	62.7	0.58 ± 0.05	1.9 (1.2)	4.6 (4.5)
SBA15a		c	c	c	c	1.4 (1.6)	2.6 (3.3)
SBA15b		c	c	c	c	1.4 (1.8)	3.9 (3.7)

Multifrequency Analyses Unravel the Rotational Anisotropy



- Nano-confined molecules possess a greater **ordering** and anisotropy R_{\parallel}/R_{\perp} as compared to the bulk study.
- R_{\parallel}/R_{\perp} barely changes with pore sizes, as the nanoconfinement effects persist.

Significance of the Spectral Components



- Mb reports**
- helical structural types (PPII or α-helix) (X)
 - peptide length (11-, 14, or 26-aa long) (X)
 - solvents (H₂O, PB, or TFE/PB) (X)
 - pore sizes (2.5 ~7.6 nm) (X)
 - backbone dynamics on secondary structures (helix vs. hairpin) (O)

How Do Enzymes Orient When Trapped on Metal–Organic Framework (MOF) Surfaces?

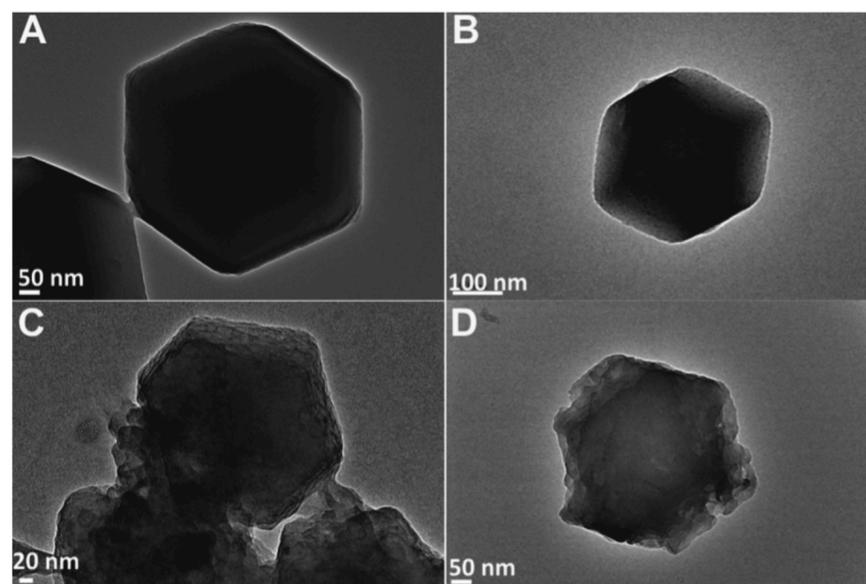


Figure 1. TEM images of ZIF-8 in MeOH (A) and PBS buffer (B) and hL/ZIF-8 composites in MeOH (C) and PBS buffer (D).

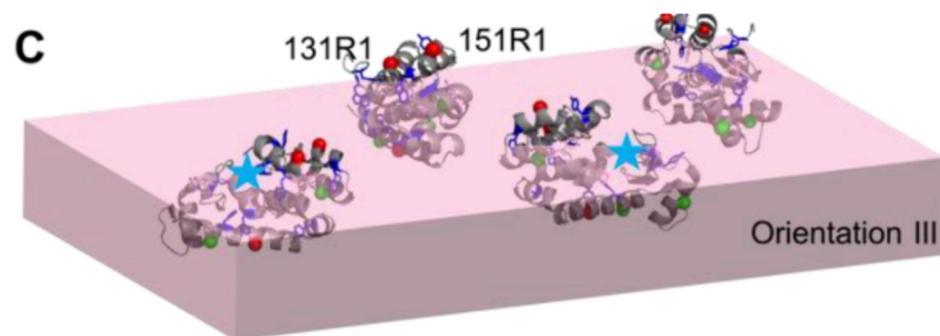
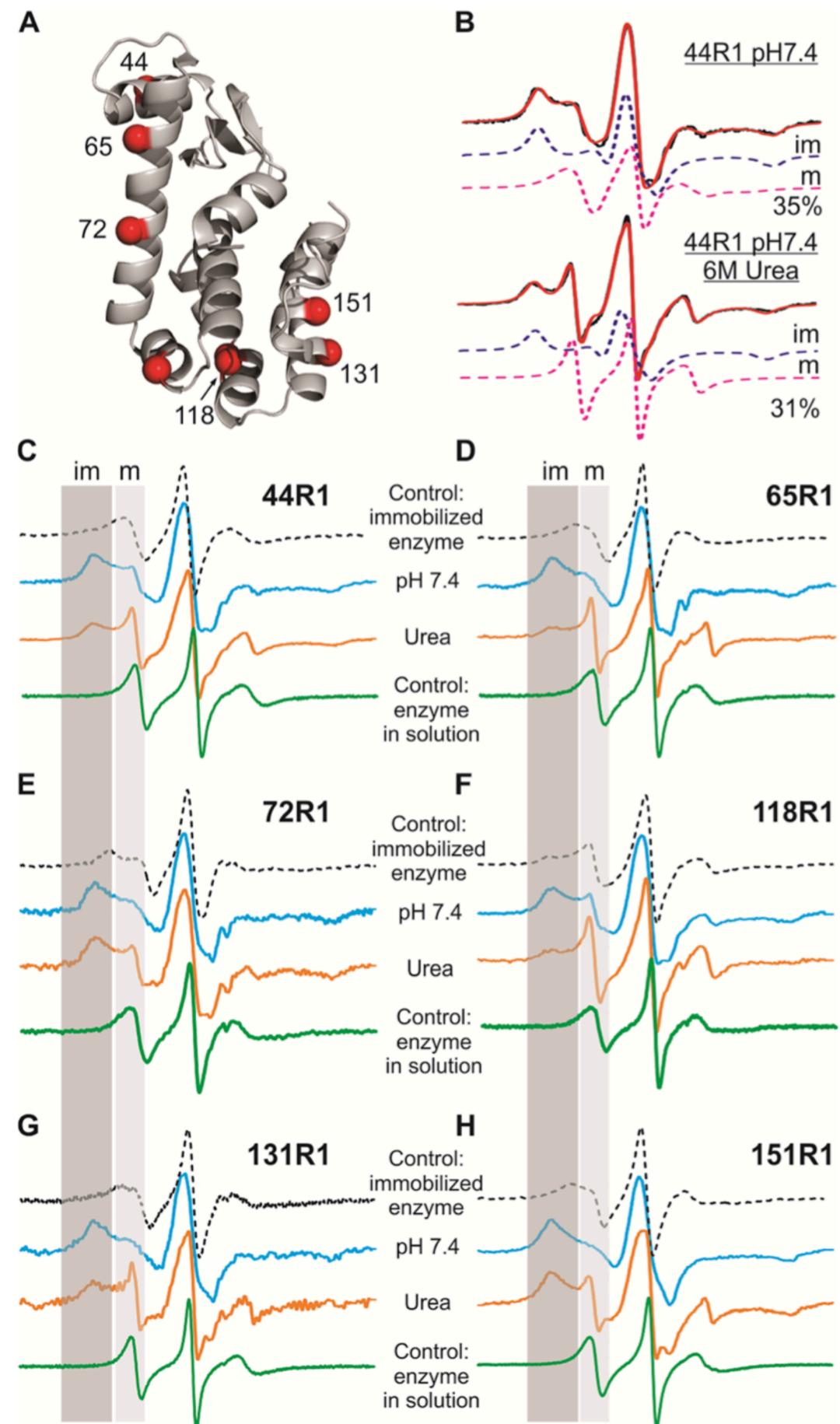
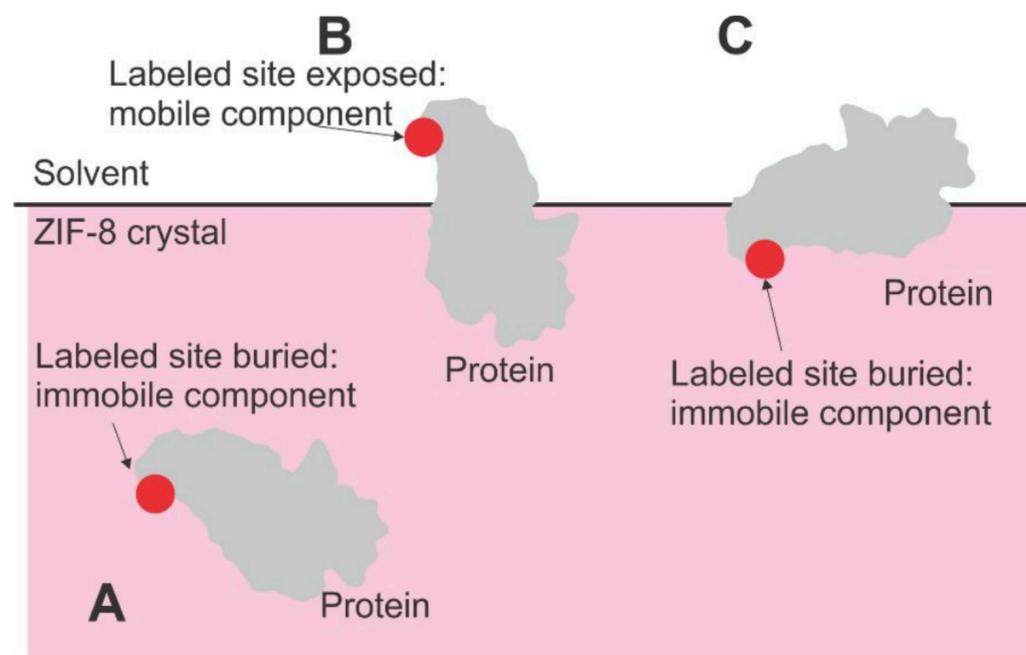


Figure 4. Proposed orientations of T4L on ZIF-8 crystal surface from four angles differing by 90° clockwise. For details of model construction and other possible orientations, see the SI.





immobilized/trapped in MOFs due to the interferences of the MOF background signals. To address such challenge, we demonstrate in this work the utilization of site-directed spin labeling in combination with Electron Paramagnetic Resonance spectroscopy, which allows for the first time the characterization of the orientation of enzymes trapped on MOF surfaces. The obtained insights are fundamentally important for MOF-based enzyme immobilization design and understanding enzyme orientation once

Figure S6. Schematic illustration of EPR signal reporting both buried and solvent-exposed enzymes. Buried sites, either buried deep inside (A) or partially buried below the crystal surface (C) will contribute an immobile component to the EPR spectrum, while an exposed labeled site (B) will show a mobile component in the spectrum.

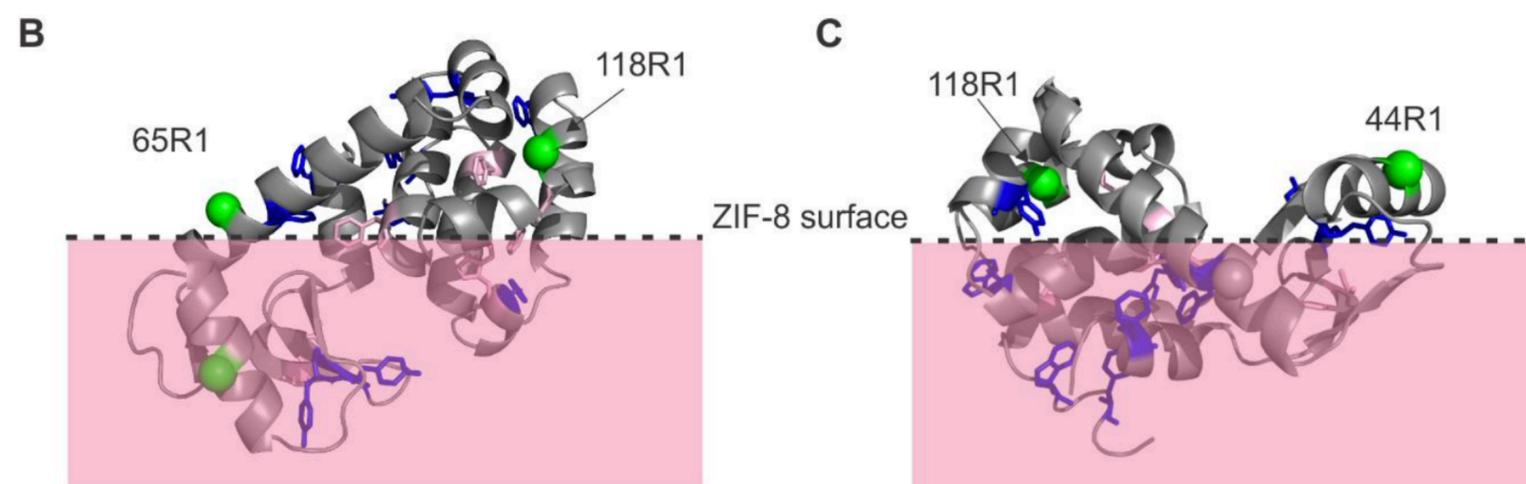


Figure S9. (A) An orientation to expose 44R1, 65R1, and 118R1 simultaneously. The buried portion (below the dotted line) is likely too small to trap the enzyme under the ZIF-8 crystal surface. (B) An orientation to expose 65R1 and 118R1. The buried portion is also too small to trap the enzyme under the ZIF-8 crystal surface. (C) It might be possible to simultaneously expose 44R1 and 118R because the buried portion is dominant.

